Magnetic End Leakage Flux in a Spoke Type Rotor Permanent Magnet Synchronous Generator

Petter Eklund, Jonathan Sjölund, Sandra Eriksson, Mats Leijon

Abstract—The spoke type rotor can be used to obtain magnetic flux concentration in permanent magnet machines. This allows the air gap magnetic flux density to exceed the remanent flux density of the permanent magnets but gives problems with leakage fluxes in the magnetic circuit. The end leakage flux of one spoke type permanent magnet rotor design is studied through measurements and finite element simulations. The measurements are performed in the end regions of a 12 kW prototype generator for a vertical axis wind turbine. The simulations are made using three dimensional finite elements to calculate the magnetic field distribution in the end regions of the machine. Also two dimensional finite element simulations are performed and the impact of the two dimensional approximation is studied. It is found that the magnetic leakage flux in the end regions of the machine is equal to about 20% of the flux in the permanent magnets. The overestimation of the performance by the two dimensional approximation is quantified and a curve-fitted expression for its behavior is suggested.

Keywords—End effects, end leakage flux, permanent magnet machine, spoke type rotor.

I. INTRODUCTION

POKE-TYPE permanent magnet (PM) rotors are typically used with magnetic flux concentration. The magnetic flux concentration makes them useful when it is desirable for the air gap flux density to exceed the remanent flux density of the PMs. This can be the case either when a very high air gap magnetic flux density is needed, or when using low remanence PMs such as hard ferrite PMs.

The rapid price increase of neodymium-iron-boron PMs in 2011 [1] led to a large increase in research on alternatives, such as using ferrite PMs for instance. There are many studies of various variations of the spoke-type PM rotor. Most, however, choose to neglect the impact of end effects, whether in the form of end winding reactance or magnetic leakage flux. Those who do take the end effects into account do so by 3D finite element analysis [2], [3], which is time consuming, both to set up and run.

In this paper the magnetic field in the end regions is investigated, and an attempt to account for the impact of the end effects in a two dimensional approximation is made.

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II. THE STUDIED MACHINE

The machine used in the experimental work is a PM generator with a rated power of 12 kW at 127 rpm and is shown in Fig. 1.

The generator is a research prototype intended for use in an experimental wind turbine. It features a cable wound stator and have been retrofitted with a spoke type ferrite PM rotor. The design of the rotor used is described in [4] and the design of the stator and reminder of the original design is described in [5]. Some data about the design are given in Table I.

The PMs are slightly longer than the pole pieces in the axial direction. This overhang is to ensure that the PMs are as least as long as the pole pieces even when at the lower bound of the tolerance. All of this overhang occurs at the end shown in Fig. 1, at the other end both the PMs and the pole pieces have their faces flush against the aluminum rotor bottom plate.

The generator end boards are made from fiberglass

Fig. 1 Photograph of the generator used in the experimental work. Inset shows close up of pole ends and air gap. The octagonal end board is 1 m from side to side

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated speed</td>
<td>127</td>
<td>rpm</td>
</tr>
<tr>
<td>Rated power</td>
<td>12</td>
<td>kW</td>
</tr>
<tr>
<td>Number of poles</td>
<td>32</td>
<td>–</td>
</tr>
<tr>
<td>Number of slots per pole and phase</td>
<td>5/4</td>
<td>–</td>
</tr>
<tr>
<td>Stator inner diameter</td>
<td>760</td>
<td>mm</td>
</tr>
<tr>
<td>Air gap length (narrowest part, average for all poles)</td>
<td>6.6</td>
<td>mm</td>
</tr>
<tr>
<td>Stator stack length</td>
<td>224</td>
<td>mm</td>
</tr>
<tr>
<td>Rotor pole piece length</td>
<td>224</td>
<td>mm</td>
</tr>
<tr>
<td>PM size</td>
<td>$224^{+5}_{-0} \times 122 \times 38$</td>
<td>mm</td>
</tr>
<tr>
<td>PM material</td>
<td>Hard ferrite</td>
<td>–</td>
</tr>
<tr>
<td>PM remanence (measured average)</td>
<td>0.38</td>
<td>T</td>
</tr>
</tbody>
</table>
composite that is both non-magnetic and non-conductive.

The generator has previously been investigated with respect to manufacturing tolerances and it was found that the PMs have remanence below the tolerance [6]. The remanence measured in [6] is used in the calculations for this study.

III. MEASUREMENT OF MAGNETIC FIELD IN THE END REGIONS

The magnetic field in the end region of the machine is measured at standstill using a Hall-probe. Measurements are made of the magnetic field component normal to the radial plane bisecting the PM, and of the axial component in the radial plane bisecting the pole. The locations of the measurements are indicated in Fig. 2.

The measurements are repeated for each pole and PM of the machine. A 3D-printed plastic probe holder is used to ensure that the probe is held in the same position relative to the pole or PM measured.

For each PM the tangential component of the magnetic field is measured at ten different positions. Five measurements each for two lines placed 13.25 mm and 31.25 mm in the axial direction, from the end surface of the pole pieces. For each pole the axial component is measured at four points on a line 25.25 mm from the end of the pole piece. These locations and directions are chosen to reduce the impact of probe misalignment. At the selected measurement points the field is expected to be mostly parallel to the measuring direction, because of symmetry.

The radial component of the magnetic field near the end of the air gap is also measured. The probe is held in place by a fixture allowing it to be slid up and down in the axial direction of the machine. The fixture is mounted so that the field is measured about 2 mm from inner side of the stator and in front of a stator tooth. The rotor is positioned so that a rotor pole faces the stator tooth. This relative position between rotor and stator is also used in the simulations. The probe is then moved from about 20 mm outside the machine to 40 mm into the air gap.

The Hall-probe instrument used is an FW Bell 5180 Gauss/Tesla Meter with an STD-18-0404 transversal probe. It is the same instrument that was used to measure the remanence in [6].

IV. SIMULATION OF THE MAGNETIC FIELD IN THE END REGIONS

The magnetic field in the end regions is simulated using the Finite Element Method (FEM). Scalar magnetic potential can be used since the machine is simulated at standstill and there are no free currents. Non-linear B-H-curves are used to model magnetic saturation of the iron in the rotor and stator. Periodic boundary conditions are used so that only a repeating 45° sector of the geometry needs to be simulated, reducing the computational effort. The lower half of the geometry is mirrored. This is done by removing the lower half and using magnetic insulation at the boundary, that is a zero normal component of the magnetic field on the boundary. The geometry of the 3D FEM-model can be seen in Fig. 3.

Most of the geometry of the machine is parametrically defined. A 2D approximation of the model is created by taking a cross section of the 3D model geometry. The magnetic field is then assumed to be in the plane of the cross section, and not to change in the axial direction. The remanence, 0.38 T, and recoil permeability, 1.08, of the PM are taken from [6]. The 3D model is validated using measurements of the magnetic field in the prototype.
To investigate the influence of the machine length, $l_{\text{machine}}$; air gap length, $l_{\text{ag}}$; width of the PM, across magnetization; and length of the PM, along magnetization, on the difference between the 2D approximation and the 3D model scaling factors are added. The scaling factors are then changed once at a time so that each of the lengths are scaled by a factor $2 \pm 1$ and $2 \pm 1/2$ if possible, otherwise the extreme and the square root of the extreme are used. When changing the geometry of the PMs the surrounding iron is changed correspondingly.

The radial plane bisecting the PM is divided into different flux paths, one for the magnetic flux trough the PM and the rest for the returning flux. The returning flux paths correspond to the useful flux passing the stator and different leakage flux paths. The integration surfaces used in the 3D model are shown in Fig. 4.

In the 2D model line segments multiplied by the machine length are used to form the integration surfaces. The integration line segments are shown in Fig. 5.

For both cases the component of the magnetic field normal to the integration surface is integrated to get the magnetic flux.

V. THE MAGNETIC FIELD IN THE END REGIONS

The simulations of the magnetic field are compared to measurements in Figs. 6 and 7. Fig. 6 shows the tangential component above the PM, at two different distances from the rotor end. Fig. 7 shows the axial component above the pole. The components of the field tangential to the direction shown in the graphs are checked and confirmed to be small compared to the measured values.

The measurements of the tangential component of the magnetic field above the PM show good agreement with the simulation. The simulated field lies near the middle of the span of the measured values in all the measurement points. Some variation between poles is to be expected due to magnetic tolerances of the components; earlier investigation of the machine revealed some variation of PM remanence between poles [6].
For the measurements of the axial component above the pole the simulation underestimates the field component. The simulated values are close to the lowest measured values. The field in this region is, however, very dependent on the location in the axial direction. The discrepancy is roughly equivalent to an error of 1 mm to 1.5 mm in axial position, or roughly the thickness of the Hall probe used for the measurements.

The radial component of the magnetic field in the air gap and some distance outside the machine end is shown in Fig. 8. Agreement is good considering there is some uncertainty in the position of the probe and rotor angle during measurement. The dent in the simulated magnetic flux density curve at around \(-7\) mm is most likely caused by a problem with the mesh.

Numerically computed field lines of the simulated magnetic field are shown in Fig. 9. The field lines show that the axial component of the magnetic field grows toward the end of the machine. Further, it shows that the axial component mainly is present in the pole pieces, while the magnetic field in the PM is mostly in the plane of rotation.

When planning the measurement it was assumed that the magnetic field was mostly normal to the radial plane bisecting the PM, this assumption is confirmed by Fig. 9. The figure also support the assumption that the magnetic field in the end region is mostly axial in the plane bisecting the pole.

The simulated magnetic field in a radial plane bisecting a PM is shown in Fig. 10. The component of the magnetic field normal to the plane dominates, as expected from symmetry. The field outside the machine decays exponentially, which can be expected from a magnetic field when moving away from the sources.

The simulated magnetic field in a radial plane bisecting a rotor pole is shown in Fig. 11. The field lies mostly in the plane, and outside the machine end it is approximately axial over the pole piece, as expected from symmetry and confirmed by measurements. While the axial component of the magnetic field in the pole piece increases when moving...
from the mid-plane to the machine end, the main change of the norm of the magnetic field is in the radial direction.

The total magnetic flux through the PM is 4.7 mWb, of this 58% will cross the air gap and pass through the stator according to simulations. The end leakage flux is equal to 20% of the magnetic flux from the PMs, making it the largest leakage flux. Another 16% of the total flux through the PM will pass through the interior of the rotor and the last 0% will pass between the poles in the air gap. Since the machine have a low length to diameter ratio it can be expected that the end leakage flux path will carry a large part of the total magnetic flux provided by the PMs.

VI. END EFFECT CORRECTIONS FOR 2D SIMULATIONS

The magnetic fluxes for the 3D and 2D simulations are compared in Table II. The 2D approximation removes the end leakage flux path, which is of significant permeance. The removal of this flux path mean that the PM sits in a magnetic circuit with lower permeance. This shifts the PMs working point on the BH-curve further from the B-axis, which corresponds to a smaller \( \Phi_{\text{PM}} \). The increased magnetic flux from the PM, and redistribution of magnetic flux from the \( \Phi_{\text{in}, \text{rotor}} \) to the end leak paths reduces the difference in \( \Phi_{\text{stator}} \) between the 2D and 3D case.

To compare the 3D and 2D simulations the ratio of \( \Phi_{\text{stator}} \) for 3D over the same for 2D is

\[
\frac{\Phi_{3D/2D}}{} = \frac{\Phi_{3D}}{\Phi_{2D}}
\]

where superscripts indicate 3D and 2D, respectively, is used. Using \( \Phi_{3D/2D} \) for the comparison between 3D and 2D is done because the magnetic flux through the stator reflects the induced voltage of the machine. Therefore \( \Phi_{3D/2D} \) should give the ratio of the induced voltages for 3D over 2D. The ratio \( \Phi_{3D/2D} \) can also be computed easily from a static simulation which is an advantage. One issue is how much of the stator cross section to consider carrying useful magnetic flux. Here the whole stator cross section is used when computing \( \Phi_{\text{stator}} \). This may include some of the slot leakage flux in \( \Phi_{\text{stator}} \) but this inclusion should be approximately the same in both the 2D and 3D case, not affecting the comparison.

The ratio \( \Phi_{3D/2D} \) versus the relative change of the selected geometry parameters are shown in Fig. 12.

The machine length and air gap length show clear trends while trends of the length and width of the PM are inconclusive. A possible reason why the PM shape parameters show no clear trends for \( \Phi_{3D/2D} \) is that the possible variation of them are narrowly constrained geometrically. This prevents large changes in the parameter values without altering the topology of the rotor. This in turn makes it hard to tell the difference between modeling errors and changes in dependent values. Changes in the width of the PM give very little change in \( \Phi_{3D/2D} \) compared to what changes in the other parameters cause and only a very slight increasing trend. Changes of the length of the PM cause more change in \( \Phi_{3D/2D} \) but it appears highly irregular.

The value of \( \Phi_{3D/2D} \) asymptotically approaches unity as the machine length increases, which reflect a decreasing impact of end effects as the machine grows longer. For decreasing machine length the rate of change in \( \Phi_{3D/2D} \) grows more negative.

Using curve fitting techniques an approximation for \( \Phi_{3D/2D} \) in terms of machine geometry parameters can be found. The approximation is

\[
\Phi_{3D/2D} = \frac{l_{\text{machine}}}{l_{\text{machine}} + \frac{D}{p} \tanh \left( \frac{l_{\text{ag}}^2}{2D} \right) \left( \frac{\pi}{p} \right)^{2/3}}
\]

where \( p \) is the number of poles, \( D \) the diameter of the stator bore, \( l_{\text{machine}} \) the length of the machine and \( l_{\text{ag}} \) the length of the air gap. The approximation is compared to the simulation data in Fig. 13.

The fit is reasonable and the asymptotic behavior in \( l_{\text{machine}} \) is correct, vanishing at \( l_{\text{machine}} = 0 \) and approaching unity as \( l_{\text{machine}} \) grows large. Agreement is better for small \( l_{\text{ag}} \) than for large but this should not pose a problem as \( l_{\text{ag}} \) is relatively large for the size of the machine. It should be noted that (2) is not derived from first principles but fitted to a limited set of data points. A limitation of the dataset is that the ratio \( \frac{D}{p} \) is not changed, reducing the generality of the obtained fit.

Once a value of \( \Phi_{3D/2D} \) is obtained, either by use of 3D FEM, (2) or other means, it can be used to apply corrections to a 2D FEM simulation. The simplest way to do this is
to multiply the machine length by $\bar{\phi}_{3D/2D}$ when computing induced voltage and inductance. A more complicated way is to adjust the remanence of the PM until $\Phi_{2D_{\text{stator}}} = \Phi_{3D_{\text{stator}}}$. The former is preferable both from a physical standpoint and a computational. The magnetic field component in the plane of rotation is slightly decreased in the 3D case compared to the 2D case but the norm of the magnetic field will be more or less the same due to the axial component which is not present in the 2D simulation. This means that the magnetic saturation of the steel is more accurately described by scaling the machine length.

VII. Conclusion

The magnetic end leakage fluxes in a spoke type rotor has been measured and simulated with good agreement. The magnetic end leakage flux in the studied machine is about one fifth of the total magnetic flux passing through the PMs and the largest leakage flux. It increase the permeance of the magnetic circuit, that increases the magnetic flux in the PM meaning that the impact on the main flux is reduced.

The relative impact of the end leakage flux decreases as the machine length increases and it decreases as the air gap length shrinks. To compensate a 2D simulation the machine length can be scaled by the ratio of magnetic flux passing through the stator for the 3D case over the 2D case. This ratio can either be obtained from the curve fitted expression (2) or from static 3D FEM with magnetic scalar potential at standstill.

References