Abstract—In this paper, a methodology for physically modeling the intrinsic MOS part and the drift region of the n-channel Laterally Double-diffused MOSFET (LDMOS) is presented. The basic physical effects like velocity saturation, mobility reduction, and nonuniform impurity concentration in the channel are taken into consideration. The analytical model is implemented using MATLAB. A comparison of the simulations from technology computer aided design (TCAD) and that from the proposed analytical model, at room temperature, shows a satisfactory accuracy which is less than 5% for the whole voltage domain.

Keywords—LDMOS, MATLAB, RESURF, modeling, TCAD.

I. INTRODUCTION

THE LDMOS acts as an important component in intelligent power integrated circuits for the properties of superior isolation, low leakage current, and easy integration [1]-[3]. Optimal design of RF power amplifiers requires physical LDMOS models that should describe the device characteristics accurately over a wide range of biases and temperatures.

Several LDMOS models have been proposed [4]-[6], but a complete physical model is still missing. A frequently approach in modelling the LDMOS transistor on a circuit level is achieved by either a sub-circuit model [4], [7] or a semi-numerical model [8], [9]. The disadvantage of this approach is that, during circuit simulation, these models may increase the computation time, or may have convergence problems. Furthermore, most of these models lack an accurate description of one or more specific device characteristics. For instance, in the models of [8], a conventional low-power MOS model with uniform doping has been taken for the graded channel, while in the sub-circuit model of [7], the drift region is only described by a linear resistor. The drawback of the models [9] is that the potential drop over the channel varies only linearly with position.

For the development of power semiconductor device models, several effects have to be considered since they dominate the static and dynamic device characteristics. These effects are not described correctly by standard device models because their influence on low-power devices is less important or negligible [10]-[12]. So, better investigation of the physics of the HV devices and clear understanding of the special effects are needed.

The modeling of the lateral structures came into play as these devices were integrated in standard technologies. Remarkable progress in the modeling field is conducted to geometrical approximations of the drift zone (regional approach), which seems to be the most promising approach.

In the first part of this paper, an approach for physically modeling of the intrinsic MOS part and the drift region is presented. In the proposed model, all the physical effects are considered. The device charges are calculated and integrated to provide analytical expressions for the currents. The second part of the paper presents implementation of the model. Finally, the DC characteristics using the model are compared with the results of TCAD simulations showing good accuracy.
II. ANALYTICAL MODELLING OF LDMOS

Some critical points are encountered in the attempt to analytically model a HV LDMOS. This is mainly related to the fact that a typical HV LDMOS structure is made of intrinsic MOS part and the extension of the drain, the architecture of which dictates the high voltage capabilities (see Fig. 1).

The drift region of the device is divided into two distinct parts as shown in Fig. 2. The first zone is a depleted area in which the carriers are injected by the intrinsic MOSFET, and the second zone is the non-depleted area at the drain side [13], [14].

Fig. 2 Drift region functional partition

The technological parameters are indicated in Table I whereas the optimum geometrical parameters are shown in Table II.

TABLE I

<table>
<thead>
<tr>
<th>THE TECHNOLOGICAL PARAMETERS OF THE N-CHANNEL LDMOS</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>P-WELL</strong> (1.25 x 10^{17} cm^{-3})</td>
</tr>
<tr>
<td>PBL (2.5 x 10^{17} cm^{-3})</td>
</tr>
<tr>
<td>NBL (3.5 x 10^{18} cm^{-3})</td>
</tr>
</tbody>
</table>

TABLE II

<table>
<thead>
<tr>
<th>THE OPTIMUM GEOMETRICAL PARAMETERS OF NLDMOS</th>
</tr>
</thead>
<tbody>
<tr>
<td>( L_{CH} = 1.00 \mu m )</td>
</tr>
<tr>
<td>( L_{ACC} = 0.40 \mu m )</td>
</tr>
<tr>
<td>( L_{DPP} = 1.50 \mu m )</td>
</tr>
<tr>
<td>( L_{DFP} = 0.50 \mu m )</td>
</tr>
</tbody>
</table>

By using these parameters, the breakdown voltage of the nLDMOS and the impact ionization distribution are shown in Fig. 3. It is obvious that \( BV = 60V \) and the avalanche breakdown is occurred at the Pwell / N-buried junction far from the surface. In Fig. 4, the electric field and potential lines distributions are illustrated at the breakdown condition. The potential lines are uniformly distributed over the drift region with surface electric field smaller than 3 x 10^5 V/cm.

A. Channel Region Model

The model is derived based on the following basic assumptions:

1. The laterally non-uniform channel (P-body) doping density can be approximated as a simple exponential function,
2. The gradual channel approximation is valid,
3. The surface potential of the graded-channel varies linearly with position, and
4. A simple relationship between the inversion charge density \( Q_i \) and the local potential \( \phi(x) \).

The non-uniform doping density along the channel can be approximated as an exponential function \( N_d(x) = N_{d0} \exp(-\eta x / L_{ch}) \), where \( N_{d0} \) is the concentration near the source and \( \eta \) is the doping gradient, chosen to be \( \ln(N_{d0} / N_p) \), so that \( N_d(L_{ch}) = N_D \) [14]–[17]. We use a piecewise-continuous electron velocity model [18].
Fig. 4 (a) Electric field, and (b) potential distributions, of nLDMOS

\[ v = \frac{\mu_{\text{sat}} E_x}{1 + (\mu_{\text{sat}} E_x / 2v_{\text{sat}})}, \quad v \leq v_{\text{sat}} \]
\[ = v_{\text{sat}}, \quad \text{otherwise} \]

where \( E_x \) is the longitudinal electric field, \( v_{\text{sat}} \approx 10^7 \text{ cm/s} \) is the saturated drift velocity, and, where \( \mu_{\text{sat}} \) is the low field mobility, \( \theta \) is the fitting parameter that defines the transverse-field dependence.

1) Channel Region Model

The threshold-voltage is defined as the gate-voltage at which the semiconductor surface is at the onset of strong inversion. Hence, the concentration near the source is higher than the concentration near the drain, so the semiconductor surface near the drain is inverted before that near the source. So, to obtain an expression of \( V_{TH} \), we use the bulk doping concentration at the source side \( N_{A0} \).

\[ I_n = -WvQ_n \quad (W \text{ is the device width and } Q_n \text{ is the inversion charge density) from source to drain, and by using } \]
\[ \frac{dQ_n}{dv} = C_{x0} + C_x, \quad \text{the Channel current in the linear region is} \]

\[ I_n = \frac{W\mu_{\text{sat}}}{L_{x0} \left[ 1 + \left( \frac{\mu_{\text{sat}}}{2v_{\text{sat}}} L_{x0} \right) V_{K} \right]} \left[ \left( C_{x0} (V_{gs} - V_{T}) + (C_{x0} + C_x) \phi_0 \right) - 0.5 \left( C_{x0} + C_x \right) V_{K} \right] V_{K} \]

where \( V_{K} \) is the intrinsic drain voltage. \( C_{x0} = \varepsilon_{x0} / t_{x0} \) is the capacitance of the of the oxide layer with permittivity \( \varepsilon_{x0} \) and thickness \( t_{x0} \). \( C_x \) is the average depletion capacitance which assumed to be invariant along the channel.

\[ C_x = C_{x0} \left( 1 - \frac{2\phi_0}{V_{gs}} \right) \quad \text{where, } C_{x0} = \sqrt{-\left( \varepsilon_{x0} N_{x0} / 4\phi_0 \right)} \]

2) Channel Current

The quasi-static channel current is described by

\[ V_x = V_{gs} + 2\phi_0 + \frac{\sqrt{4q\varepsilon_{x0} N_{x0} \phi_0}}{C_x}, \quad (2) \]

where \( \phi_0 \) is the Fermi-potential \( \phi_0 = \frac{KT}{q} \ln \frac{N_{x0}}{n_i} \).

In saturation, the current is saturated due to the electron velocity saturation at the source end of the channel. However, velocity saturation at the source and the drain side both can occur depending on the channel length and the channel region doping gradient.

If the channel is very long or the doping gradient is very
small, the electron velocity saturation occurs at the drain end of the channel. On the other hand, if the gradient is very high, the inverted electron concentration is much higher at the drain end than the source end and the velocity will saturate there. Generally, to get an expression for the saturation current, the following differential equation is used:

$$0 = \frac{\partial I_{ds}}{\partial V_K} \bigg|_{V_K = V_{sat}}$$

(5)

where \(V_{sat}\) is the value of the intrinsic drain voltage at the onset of current saturation.

$$V_{sat} = \frac{C_{ox}(V_{gs} - V_T) + (C_{eq} \eta \phi_s)}{C_{ox} + C_{eq}}$$

(6)

Substituting (6) into (3), one gets;

$$I_{sat} = \frac{W \mu_{sat} E_s}{2L_{ch} [1 + (\mu_{sat}/2V_{sat}L_{ch}) V_{sat}]}$$

$$0.5 [C_{sat}(V_{gs} - V_T) + (C_{eq} \eta \phi_s)]^2$$

$$\left( C_{ox} + C_{eq} \right)$$

(7)

This saturation current is general and independent on the location at which \(v = v_{sat}\) (source side or \(K\)-point).

III. DRIFT REGION MODEL

The flow chart of the modelling methodology, which represents the various cases, is shown in Fig. 5:

![Fig. 5 Modeling flow chart](image_url)

The model is split into two cases:

Case 1. The accumulated case, \(V_G - V_{FBdr} > V_K\).

Case 2. The non-accumulated case, \(V_G - V_{FBdr} < V_K\).

where \(V_{FBdr}\) is the flat band voltage, \(V_G\) is the gate voltage, \(V_K\) is the surface potential of the intrinsic MOS drain, and \((V_G - V_{FBdr})\) is the limit of the accumulation layer.

A. The Accumulated Case, \(V_G - V_{FBdr} > V_K\)

1. Case of \(V_{GS} - V_{FBdr} < V_{K1}\)

   i. Zone I

   The accumulation charge can be computed by using simple capacitance equivalence [4], [13], [15].

   $$Q_{acc} = -C_{ox} (V_{GS} - V_{FBdr} - \psi_s)$$

   (8)

   where \(C_{ox}\) is the oxide capacitance, \(\psi_s\) is the surface potential.

   The integration of the accumulation charge with the position leads to the current component given by the accumulation layer.

   $$I_{acc} = -WQ_{acc} v$$

   (9)

   where \(v\) is the carrier velocity, defined as in (1).

   where \(v\) is the carrier velocity, defined as in (1).

   $$I_{acc} = \frac{-WQ_{acc} \mu_{sat} E_s}{1 + (\mu_{sat}/2V_{sat}L_{ch}) V_{sat}}$$

   (10)

   where \(E_s = dy/\psi_s\), and \(\mu_{sat}\) is the effective electron mobility in the accumulation region.

   $$I_{acc} = 2 \left[ \frac{W \mu_{sat} C_{ox}}{1 + (\mu_{sat}/2V_{sat}L_{ch}) V_{sat}} \right]$$

   (11)

   $$\int_V^{V_{FBdr}} (V_G - V_{FBdr} - \psi_s) d\psi_s$$

   $$\Rightarrow I_{acc} = \frac{W \mu_{sat} C_{ox}}{2L_{acc} \left[ 1 + (\mu_{sat}/2V_{sat}L_{ch}) V_{sat} \right]}$$

   (12)

   \((V_G - V_{FBdr} - V_K)\)

   The second type of charge present in zone I is the drift charge. The drift charge concentration is approximated constant for the drift zone.
\[ Q_b = -qN_{dr}y_{path} \]  \hspace{1cm} (13)

where \( y_{path} \) is the depth of the current path. As for the accumulation current, the integration of the drift charge provides the expression for the drift current.

\[ I_s = -WQ_bV. \]  \hspace{1cm} (14)

where \( v \) is the carrier velocity, defined in (1).

\[ I_{L_{acc}} = \frac{qW\mu_{sat}N_{dr}}{2} \left( V_G - V_{FB,dr} - V_K \right) \left[ \frac{y_{path}}{1 + \mu_{eff} \frac{V_G - V_{FB,dr} - V_K}{2L_{acc}V_{sat}}} \right] \]  \hspace{1cm} (15)

\[ I_s = \frac{qW\mu_{sat}N_{dr} \tan \alpha}{2} \left( V_G - V_{FB,dr} - V_K \right) \left[ \frac{y_{path}}{1 + \mu_{eff} \frac{V_G - V_{FB,dr} - V_K}{2L_{acc}V_{sat}}} \right] \]  \hspace{1cm} (16)

where \( \tan \alpha \) is the slope of the current path at the K-point.

\[ I_s = I_{acc} + I_b \]  \hspace{1cm} (17)

where \( I_s \) is the total current through the drift region.

\[ I_{acc} = \frac{qW\mu_{sat}N_{dr}}{2} \left( V_G - V_{FB,dr} - V_K \right) \left[ \frac{y_{path}}{1 + \mu_{eff} \frac{V_G - V_{FB,dr} - V_K}{2L_{acc}V_{sat}}} \right] \]  \hspace{1cm} (18)

\[ I_{b} = \frac{qW\mu_{sat}N_{dr} \tan \alpha}{2} \left( V_G - V_{FB,dr} - V_K \right) \left[ \frac{y_{path}}{1 + \mu_{eff} \frac{V_G - V_{FB,dr} - V_K}{2L_{acc}V_{sat}}} \right] \]  \hspace{1cm} (19)

where \( Q_{dr} \) is the drift region charge density, which is uniform \( Q_{dr} = qZ_{dr} \), \( n_{dr} = N_{dr} \), where \( N_{dr} \) is the drift region doping concentration, and \( v \) is the carrier velocity defined in (1).

\[ I_{dr} = qN_{dr}WZ_{dr} \frac{\mu_e E_s}{1 + \left( \mu_e E_s / 2V_{sat} \right)} \]  \hspace{1cm} (20)

where \( E_s = dV(x)/dx \)

By integrating the above current relation over the drift region, an expression for the current in the drift region is obtained as follows:

\[ I_{dr} = \frac{qN_{dr}WZ_{dr} - I_{dr}}{2V_{sat}} \mu_n \frac{dV(x)}{dx} \]

\[ \Rightarrow \int I_{dr} dx = \frac{qN_{dr}WZ_{dr} - I_{dr}}{2V_{sat}} \mu_n \int dV(x) \]

\[ \Rightarrow I_{dr} = \frac{qN_{dr}WZ_{dr} \mu_n}{L_{dr} \left[ 1 + \mu_{eff} \frac{V_D - V_{FB,dr}}{2V_{sat}L_{dr}} \right]} \left( V_D - V_{FB,dr} \right) \]  \hspace{1cm} (21)

As, \[ R_{dr} = \frac{L_{dr}}{qN_{dr}WZ_{dr} \mu_n} \]  \hspace{1cm} (22)

where, \( L_{dep} = L - d_{dep} \) and, \( Z_{dep} = T_{Drift} - Z_{dep} \)

We notice that the expression of the drift resistance consists of two terms, the first one represents the drift resistance at low voltage conditions \( R_{dr0} \), and the second term represents the drift region resistance due to high voltage and current conditions \( R_{drsat} \).

\[ R_{dr} = R_{dr0} + R_{drsat} \]

2. Case of \( V_{GS} - V_{FB,dr} > V_{K1} \)

i. Zone I

This area is modelled as a depletion resistance, which is associated with the so called JFET pinch-off. The starting point is Poisson's equation.

\[ I_{acc} = -WQ_bV. \]  \hspace{1cm} (23)

\[ 2d_{dep} \left[ 1 + \mu_{eff} \frac{V_{K1} - V_K}{2d_{dep}V_{sat}} \right] \]  \hspace{1cm} (24)

where \( d_{dep} \) is the depletion layer width.

\[ I_{b} = \frac{qW\mu_{sat}N_{dr}I_{L_{acc}} \tan \alpha}{2} \left( V_{K1} - V_K \right) \]  \hspace{1cm} (25)

ii. Zone II

Zone II is represented by a drift resistance \( R_{dr} \).

B. The Non-Accumulated Case

The accumulated case, \( V_{G} - V_{FB,dr} < V_{K1} \).

i. Zone I

This area is modelled as a depletion resistance, which is associated with the so called JFET pinch-off. The starting point is Poisson's equation.
\[
\frac{dE}{dx} = \frac{D}{\varepsilon_s}
\]

where \( E \) is the electric field and \( \rho \) is the charge density.

\[
-\frac{d^2 \psi_s}{dx^2} = \frac{\rho}{\varepsilon_s} \quad \rho = qN_0
\]

\( \psi_s \) is the potential function of position which depends only on the lateral position. After the double integration of (26) between the limits \( \psi_{SL} \) and \( \psi_{D} \), the following expression is obtained for the potential,

\[
\psi_s(x) = \frac{qN_0}{2\varepsilon_s} x^2 + \left[ \frac{\psi_{SL} - \psi_{D}}{d_{dep}} \frac{qN_0}{2\varepsilon_s} d_{dep} \right] x + \psi_{SL}
\]

To link the potential variation with the position on the resistance of the depleted area, the simple formulation for the mobile charge can be used in conjunction with the conductance of a depleted zone.

\[
n(x) = n_i \exp \left( \frac{q\psi_s}{kT} \right)
\]

\[
R_{dep} = \int_0^{d_{dep}} \frac{q\mu N_0 W T}{q\mu N_0 W T}
\]

\( \text{ii. Zone II} \)

Zone II is represented by a drift resistance \( R_{dep} \).

### IV. Simulation of the Analytical Model

The analytical model was simulated using MATLAB. Before proceeding, the physical key constants and parameters are stated below in Table III.

In the current relations of the implemented analytical model, the mobility is taken as 1025 cm²/V.sec, which has excellent correspondence with the TCAD simulation results in Fig. 6(a). The current density distribution is also shown in Fig. 6(b). The distribution shows the slope of the current path at the K-point which is considered in our proposed model.

By using the above key constants and parameters, the threshold voltage of the device is equal to 0.576 V. The capacitances \( C_{ds} \) and \( C_{gd} \) are equal to 6.3×10⁻¹⁵ F and 1.8×10⁻¹⁵ F, which are approximately matched with the value obtained from TCAD simulation.

### Table III

<table>
<thead>
<tr>
<th>Physical Key Constants and Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>( T ) = 1.8×10⁻⁴ cm</td>
</tr>
<tr>
<td>( \varepsilon ) = 4.5435×10⁻⁷ F/cm²</td>
</tr>
<tr>
<td>( N_{0} ) = 9.5×10¹⁷ cm⁻³</td>
</tr>
<tr>
<td>( C_{ox} ) = 4.5435×10⁻⁷ F/cm²</td>
</tr>
<tr>
<td>( N_{10} ) = 9.5×10¹⁷ cm⁻³</td>
</tr>
<tr>
<td>( N_{A0} ) = 9.5×10¹⁷ cm⁻³</td>
</tr>
<tr>
<td>( T_{temp} ) = 300 K</td>
</tr>
<tr>
<td>( \phi_{v} ) = 0.46513 V</td>
</tr>
<tr>
<td>( n_i ) = 1.482×10¹⁰ cm⁻³</td>
</tr>
<tr>
<td>( L_{o} ) = 6.0×10⁻⁴ cm</td>
</tr>
<tr>
<td>( V_{Gm} ) = -0.95 V</td>
</tr>
<tr>
<td>( P_{ox} ) = 1.5×10⁻¹⁷ cm⁻³</td>
</tr>
<tr>
<td>( V_{R} ) = -0.2 V</td>
</tr>
<tr>
<td>( T_{pwell} ) = 2.15×10⁻⁴ cm</td>
</tr>
<tr>
<td>( V_{sat} ) = 4.5×10⁻⁴ cm/sec</td>
</tr>
<tr>
<td>( L_{s} ) = 1.65×10⁻⁴ cm</td>
</tr>
<tr>
<td>( V_{ther} ) = 0.025875 V</td>
</tr>
</tbody>
</table>

The \( I_D - V_{DS} \) characteristics of the nLDMOS are shown in Fig. 7. It is observed that the model approximately follows the behaviour of the TCAD simulated device, as \( V_{GS} \) is increased. The deviation of the analytical model from the TCAD simulation is due to the injection of carries in the drift region and the accumulation layer formation under the gate oxide. These phenomena are not taken into account in the analytical model, as their addition complicates the model.
Fig. 6 (a) Mobility distribution, and (b) Current density distribution

Fig. 7 Comparison of the TCAD simulation (Black solid curves) and the model simulation (Red dashed curves) for nLDMOS (V GS = 0 – 3.3 V)

V. CONCLUSION

A methodology for physically modeling the LDMOS is presented. The physical effects of velocity saturation and mobility reduction in the channel and the drift region are included in the proposed analytical model. The proposed compact model is implemented by using MATLAB as a numerical computing environment. The comparison of the simulation results using SENTAURUS TCAD and the analytical model at room temperature shows a good agreement along the whole voltage domain.

REFERENCES


