Abstract—This paper presents a speed sensorless direct torque control scheme using space vector modulation (DTC-SVM) for permanent magnet synchronous motor (PMSM) drive based on a Model Reference Adaptive System (MRAS) algorithm and stator resistance estimator. The MRAS is utilized to estimate speed and stator resistance and compensate the effects of parameter variation on stator resistance, which makes flux and torque estimation more accurate and insensitive to parameter variation. In other hand the use of SVM method reduces the torque ripple while achieving a good dynamic response. Simulation results are presented and show the effectiveness of the proposed method.

Keywords—MRAS, PMSM, SVM, DTC, Speed and Resistance estimation, Sensorless drive

I. INTRODUCTION

Able motor control has attracted much attention recently in the power electronics field [1]. Permanent magnet synchronous motors (PMSM) have been widely used as servo-machines over the last two decades. In recent years, they are used more in the variable speed applications due to some advantages like: more simplicity, low dependency on the motor parameters, good dynamic torque response, high rate torque/inertia [2] Since the advent of the direct torque control (DTC) for induction machines in the 1980’s as proposed by M. Depenbrock [1] and Takahashi [3], its research has been becoming ever more prevalent in the society. The main advantages of DTC are the simple control scheme, a very good torque dynamic response, as well as the fact that it does not need the rotor speed or position to realize the torque and flux control, moreover DTC is not sensitive to parameters variations (except stator resistor) [1]-[5].

However, it still has some disadvantages that can be summarized in the following points:

• Difficulty variable switching frequency,
• High current and torque ripple;
• High sampling frequency needed for digital
• Implementation of hysteresis comparators.
• High noise level at low speed [3];

To overcome the above drawbacks, some researchers have been trying to propose solution to solve these problems by substitute hysteresis control by fuzzy control [4]. An effective modality for reducing the torque ripple without using a high sampling frequency is to calculate a proper reference voltage vector that can produce the desired torque and flux values, and then applied to the inverter using space vector modulation (SVM) [6]-[9]. This approach is known in the literature as DTC-SVM. Even though this control method provides fast torque response and small torque ripples.

The high performance speed or position control requires an accurate knowledge of rotor shaft position and velocity in order to synchronize the phase excitation pulses to the rotor position. This implies the need for speed or a shaft position sensor such as an optical encoder or a resolver. However, the presence of this sensor (expensive and fragile and require special treatment of captured signals), causes several disadvantages from the standpoint of drive cost, encumbrance, reliability and noise problem [6]-[10].

To achieve sensorless operation of a PMSM drive, several algorithms have been suggested in recent literature. These methods can broadly be classified as:

• Back-emf based estimators with explicit compensation for nonlinear properties, parameter variation and disturbances.
• Estimation based on high frequency signal injection, exploiting the saliency property of a PMSM [3].
• Adaptive or robust observers based on advanced models. The Method of observers is sometimes more favourable due to its robustness to parameter variations and its excellent disturbance rejection capabilities[7]-[9].

This paper proposes the control strategy using space vector modulation (DTC-SVM) based on the MRAS (Model Reference Adaptive System) in the sensorless control of a permanent magnet synchronous motor and stator resistance estimation So that it can overcome the problem of sensitivity in the face of motor parameter variation.

II. PMSM MODEL

The stator and rotor flux equation of PMSM can be written in the reference frame of Park in the following form [2]:

\[
\begin{bmatrix}
\phi_d \\
\phi_q
\end{bmatrix} =
\begin{bmatrix}
L_d & 0 \\
0 & L_q
\end{bmatrix}
\begin{bmatrix}
I_d \\
I_q
\end{bmatrix} +
\begin{bmatrix}
0 \\
0
\end{bmatrix} +
\begin{bmatrix}
\ell_d \\
\ell_q
\end{bmatrix}
\]

(1)

While the equations of the stator voltages are written in this same reference frame in the following form:
The mechanical equation of the motor can be expressed as follows:
\[ J \frac{d\Omega}{dt} = T_e - T_k - f, \Omega \]

### III. CONVENTIONAL DTC

The methods of direct torque control (DTC) as shown in figure 1 consist of directly controlling the turn on or turn off of the inverter switches on calculated values of stator flux and torque from relation (6). The reference frame related to the stator makes it possible to estimate flux and the torque, and the position of flux stator. The aim of the switches control is to give the vector representing the stator flux the direction determined by the reference value.

\[
\begin{align*}
\phi_s = & \int (V_{s-a} - r_s i_s) dt \\
\phi_i = & \int (V_{s-b} - r_s i_s) dt
\end{align*}
\]

The DTC is deduced based on the two approximations described by the formulas (6) and (7) [1],[5]:

\[
\Delta \phi_s = \sqrt{\phi_s^2 + \phi_i^2} \sin (\delta)
\]

The flux and torque are controlled by two comparators with hysteresis illustrated in Figure 3. The dynamics to rque are generally faster than the flux then using a comparator hysteresis of several levels, is then justified to adjust the torque and minimize the switching frequency average [5].

### IV. SPACE VECTOR MODULATION

The Space Vector Modulation (SVM) is not based on separate calculations for each arm of a three-phase voltage inverter but by determination of a reference voltage vector from eight voltage vectors. This is generally calculated and approximated on a modulation period T from a vector average voltage developed by the application of adjacent voltage vectors and zero vectors \( V_0 \) and \( V_7 \). We note with \( T_i \) and \( T_{i+1} \) a two-time application of these vectors; their sum must be less than the period T of the inverter switching. The SVM consists in projecting the reference voltage vector on both \( V_{avg} \) desired voltage vectors \( V_1 \) and \( V_2 \) in the first sector and the application time of each adjacent vector is given by [9]:

A two levels classical voltage inverter can achieve seven separate positions in the phase corresponding to the eight sequences of the voltage inverter.

![DTC control applied for PMSM supplied with a three-phase inverter with PMW](image-url)
The determination of the amount of times of vector application can all be related to the following variables:

\[ V_{x} = \frac{T_{s}}{T} \left| V_{\alpha} \right| + x \cos (30^\circ) \]
\[ V_{\alpha} = \frac{T_{s}}{T} V_{\beta} \]
\[ x = \frac{V_{\alpha}}{\tan (60^\circ)} \]

Finally, with the \((\alpha-\beta)\) component values of the vectors given in the Table 4.2,

**TABLE II**

<table>
<thead>
<tr>
<th>Vectors</th>
<th>(S_{x})</th>
<th>(S_{y})</th>
<th>(S_{z})</th>
<th>(V_{ax})</th>
<th>(V_{az})</th>
</tr>
</thead>
<tbody>
<tr>
<td>(V_{0})</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>(V_{1})</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>(\sqrt{2} U_{c} / \sqrt{3})</td>
<td>0</td>
</tr>
<tr>
<td>(V_{2})</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>(- U_{c} / \sqrt{6})</td>
<td>(U_{c} / \sqrt{2})</td>
</tr>
<tr>
<td>(V_{3})</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>(-\sqrt{2} U_{c} / \sqrt{3})</td>
<td>0</td>
</tr>
<tr>
<td>(V_{4})</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>(- U_{c} / \sqrt{6})</td>
<td>(- U_{c} / \sqrt{2})</td>
</tr>
<tr>
<td>(V_{5})</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>(U_{c} / \sqrt{6})</td>
<td>(- U_{c} / \sqrt{2})</td>
</tr>
<tr>
<td>(V_{6})</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

The amount of times of application of each adjacent vector is:

\[ T_{i} = \frac{T}{2U_{c}} \left( \sqrt{3} V_{ax,ref} - \sqrt{2} V_{\alpha ref} \right) \]
\[ T_{z} = \frac{T_{s}}{U_{c}} V_{\beta z,ref} \]

The rest of the period spent in applying the null-vector. For every sector, commutation duration is calculated. The amount of times of vector application can all be related to the following variables:

\[ X = \frac{T}{U_{c}} \sqrt{2} V_{\alpha ref} \]
\[ Y = \frac{T}{U_{c}} \left( \frac{\sqrt{2}}{2} V_{\alpha ref} + \frac{\sqrt{2}}{2} V_{\beta ref} \right) \]
\[ Z = \frac{T}{U_{c}} \left( \frac{\sqrt{2}}{2} V_{\beta ref} - \frac{\sqrt{2}}{2} V_{\alpha ref} \right) \]

In the previous example for sector 1, \(T_{1} = -Z\) and \(T_{2} = X\).

Extending this logic, one can easily calculate the sector number belonging to the related reference voltage vector. Application durations of the sector boundary vectors are tabulated as:

**TABLE III**

<table>
<thead>
<tr>
<th>Sectors ((S_{i}))</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>(T_{1})</td>
<td>(-Z)</td>
<td>(Y)</td>
<td>(X)</td>
<td>(Z)</td>
<td>(-Y)</td>
<td>(-X)</td>
</tr>
<tr>
<td>(T_{2})</td>
<td>(X)</td>
<td>(Z)</td>
<td>(-Y)</td>
<td>(-X)</td>
<td>(-Z)</td>
<td>(Y)</td>
</tr>
</tbody>
</table>

The third step is to compute the three necessary duty cycles as:

\[ T_{con} = \frac{T_{con} - T_{con} + T_{con} + T}{2} \]

**V. DIRECT TORQUE CONTROL SCHEME USING SPACE VECTOR MODULATION (DTC-SVM)**

The strategy of the DTC-SVM uses a switching SVM vector and imposed constant frequency. This DTC- fixed frequency does not use the controller hysteresis; it significantly relaxes the constraints of computing time. Furthermore, this methodology is based on an explicit calculation of the control to achieve the objective of torque, and the oscillations of the latter are considerably reduced [11].

This is a strategy for generating a stator reference voltage which should be applied to PMSM and it can be inserted into a block PWM inverter (see Fig. 6).

In DTC-SVM, the generation of command pulses \((S_{a}, S_{b}, S_{c})\) applied to control the inverter switches is usually based on the use of a predictive controller. The error of torque \(\Delta C_{\phi} = C_{\phi,ref} - C_{\phi}\), the reference amplitude stator flux \(\phi_{*}\) determined by predictive controller. It can receive information about the module and the position of estimated stator flux \(\phi\) and measured stator current vector, then the predictive controller determinate the stator voltage reference vector in polar coordinates \(V_{ax,ref} = [V_{ax,ref}, \Delta V_{ax,ref}]\) for space vector modulator (SVM), which finally generates the pulses \((S_{a}, S_{b}, S_{c})\) to control the inverter [9].

From the vector diagram of Figure 5 and equation (1) one can obtain the following expression for the torque [11]:
\[ T_s = \frac{3}{2} \phi_s^2 \left[ q_s l_p \sin(\delta) + \frac{1}{2} \phi_s^2 (l_q - l_p) \sin(2\delta) \right] \]  

(13)

Where \( \delta \) is the angle between the stator and rotor flux linkage when the rotor resistance is neglected.

From equation (13), we note that for constant amplitude of the stator flux and flux produced by permanent magnet, the electromagnetic torque can be changed by control on the torque angle \( \delta \) which can be varied by changing position of the stator flux vector in respect to PM vector using voltage vector delivered by the inverter. In steady state, the stator flux and rotor flux rotate at synchronous speed, \( \delta \) is constant and corresponds to the torque angle. In transient state, \( \delta \) varies and the stator flux and rotor flux rotate at different speeds.

![Fig. 5 Vector diagram illustrating the conditions of torque control](image)

The error torque and the amplitude of the reference stator flux are delivered to the predictive controller. The relation between the torque error and the increment of the load angle \( \Delta \delta \) can minimize the error instantaneous torque. The reference \( \Delta \delta \) value of the stator voltage vector, is calculated based on the stator resistance, the signal \( \Delta \delta \), the measured stator current, the flux stator magnitude and its estimated position as follows: [11]

\[
\begin{align*}
V_{as \_ref} &= \frac{\phi_s \cos (\phi_s + \Delta \delta) - \phi_s \cos (\phi_s)}{T_s} + r_s i_{su} \\
V_{bs \_ref} &= \frac{\phi_s \sin (\phi_s + \Delta \delta) - \phi_s \sin (\phi_s)}{T_s} + r_s i_{su} \\
\phi_{s \_ref} &= \arctan \left( \frac{V_{bs \_ref}}{V_{as \_ref}} \right)
\end{align*}
\]

(14)

where

\[
V_{s \_ref} = \sqrt{V_{as \_ref}^2 + V_{bs \_ref}^2}
\]

(15)

For constant flux operating region, the value of reference stator flux amplitude is equal to the flux amplitude produced by permanent magnet \( q_s \). [11]

![Fig. 6 Diagram of DTC-SVM control applied for PMSM supplied with a three-phase inverter](image)

**VI. MODEL REFERENCE ADAPTIVE SYSTEM**

The presence of sensors measuring these quantities implies several disadvantages in addition to the extra cost; a greater number of connections between the motor and the control board and reduced robustness. For these reasons several strategies to detect the speed and position without sensors have been developed over the last twenty years. Multitude observers have been proposed, but only a few [7]-[12] are able to sustain persistent and accurate wide speed range sensorless operation.

The model reference adaptive system (MRAS) is an important adaptive controller [10]. The MRAS for estimating rotor position angle and speed is based on a stator current estimator using discontinuous control. Due to the fact that only stator currents are directly measurable in a PMSM drive. In this way, when the estimated currents, i.e., state, reach the manifold. Comparing to other adaptation techniques, this method is simple and needs a low computation power and has a high speed adaptation even at zero speeds. This method because eliminates the produced error in the speed adaptation, is more stable and robust.

The rotor speed and the stator resistance are reconstructed using the model reference adaptive system (MRAS). The MRAS principle is based on the comparison of the outputs of two estimators. The first is independent of the observed variable named as model reference. The second is the adjustable one. The error between the two models feed an adaptive mechanism to turn out the observed variable.

In this work, the actual system is considered as the model reference and the observer is used as the adjustable one. The rotor speed is included in the (16) that present current model are relevant to rotor speed. So the stator current model is chosen as the state variable:

\[
\begin{align*}
\frac{d}{dt} i_{d} &= \frac{v_{sd}}{l_d} - \frac{r_{sd}}{l_d} + p \hat{\omega} i_{qd} \\
\frac{d}{dt} i_{q} &= \frac{v_{sq}}{l_q} - \frac{r_{sq}}{l_q} - p \hat{\omega} i_{dq} - p q \frac{\hat{\omega}^2}{l_d} + k \frac{\hat{\omega}}{l_d}
\end{align*}
\]

(16)

The stator resistance and the rotor speed are built around the following adaptive mechanisms:
\[
\begin{align*}
\dot{\bar{r}}_q &= -\frac{1}{L_{ds}} \int_0^t (e_{qs} \bar{I}_{ds} + e_{qs} \bar{I}_{qs}) \, dt \\
\dot{\bar{Q}}_r &= \frac{1}{P} (k_p e + k_i \int_0^t e dt)
\end{align*}
\]  
(17)

\[
e = i_{qs} \dot{i}_{ds} - i_{qs} \dot{i}_{qs} - \frac{dL_q}{d_e} e_{qs}
\]  
(18)

\[
e_{ds} = \dot{i}_{ds} - \bar{i}_{ds}; e_{qs} = i_{qs} - \bar{i}_{qs}
\]  
(19)

Where \( k_p \) and \( k_i \) are the proportional and integral constants respectively. The tracking performance of the speed estimation and the sensitivity to noise are depending on proportional and integral coefficient gains. The integral gain \( k_i \) is chosen to be high for fast tracking of speed. While, a low proportional \( k_p \) gain is needed to attenuate high frequency signals denoted as noises [12].

\[
\begin{array}{c}
\text{Reference Model} \\
\text{Adjustable Model} \\
\text{Adaptation Mécanisme}
\end{array}
\]

Fig. 7 Basic MRAS structure

V. Results of Simulation

Table (IV), summarizes the PMSM parameters used in this simulation [7].

<table>
<thead>
<tr>
<th>TABLE IV</th>
<th>PMSM PARAMETERS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pole pairs</td>
<td>3</td>
</tr>
<tr>
<td>Rated power ( kW ) (at 50 ( Hz ))</td>
<td>1.5</td>
</tr>
<tr>
<td>Rated voltage ( V )</td>
<td>220/380</td>
</tr>
<tr>
<td>Rated Flux ( Wb )</td>
<td>0.30</td>
</tr>
<tr>
<td>Rated torque ( Nm )</td>
<td>5</td>
</tr>
<tr>
<td>( R_s ) (( \Omega ))</td>
<td>1.4</td>
</tr>
<tr>
<td>( L_d ; L_q (H) )</td>
<td>0.0066; 0.0058</td>
</tr>
<tr>
<td>Flux magnet ( Wb )</td>
<td>0.15</td>
</tr>
<tr>
<td>( J(Kg.m^2) )</td>
<td>0.00176</td>
</tr>
<tr>
<td>( f_e (Nm/(rad/s)) )</td>
<td>0.0038</td>
</tr>
</tbody>
</table>

We simulated the system drive for a reference speed of 100 (rd / s) load at startup, then from \( t = 0.08 \) (s), we assumed a variation of the stator resistance (see Fig. 5). At \( t = 0.15 \) (s), the PMSM is tracking load equal to 5 (Nm). The results are obtained using a PI speed controller.

Figure 8 illustrates the evolution of stator resistance, actual and estimated (delivered by the propose MRAS proposed for DTC/ DTC-SVM). The two quantities (estimated and actual resistances) are combined in practice, in steady state. As in Figure 9, it illustrates estimated speed (rad / s) issued by MRAS, the speed response is achieved without dip and with a shorter recovery time which is almost similar with the actual speed motor.

Figure 10, shows the stator flux estimation using the MRAS. We notice that it is not affected by these changes. Electromagnetic torque follows his rate as shown in Figure 12. Also, the flux and torque ripples are significantly suppressed due to the SVM modulation scheme as shown in Figure 11 and Figure 13.
In this paper, a robust MRAS for speed sensorless DTC-SVM scheme based on stator resistance estimator has been introduced. According to this control approach, the PWM inverter reference voltage vector is generated by a conventional PI predictor. The reference voltage vector is synthesized with the SVM technique as opposed to the switching table in the conventional DTC. The DTC-SVM scheme has lower harmonic current and consequently lower torque ripple than conventional hysteresis based DTC. Using of a model reference adaptive system for estimating the speed and stator resistance of a PMSM, compensate the effect of the variations of motor parameters and replace the position encoder. The obtained simulation results were satisfactory in terms of estimation errors, robustness and global stability of the drive electrical system for different operating conditions.

REFERENCES


