Abstract—In order to integrate knowledge in heterogeneous case-based reasoning (CBR) systems, ontology-based CBR system has become a hot topic. To solve the facing problems of ontology-based CBR system, for example, its architecture is nonstandard, reusing knowledge in legacy CBR is deficient, ontology construction is difficult, etc, we propose a novel approach for semi-automatically construct ontology-based CBR system whose architecture is based on two-layer ontology. Domain knowledge implied in legacy case bases can be mapped from relational database schema and knowledge items to relevant OWL local ontology automatically by a mapping algorithm with low time-complexity. By concept clustering based on formal concept analysis, computing concept equation measure and concept inclusion measure, some suggestions about enriching or amending concept hierarchy of OWL local ontologies are made automatically that can aid designers to achieve semi-automatic construction of OWL domain ontology. Validation of the approach is done by an application example.

Keywords—OWL ontology, Case-based Reasoning, Formal Concept Analysis, Knowledge Integration

I. INTRODUCTION

Ontology is formal, explicit specification of a shared conceptualization, and has been applied in many fields, such as Semantic Web, information integration and knowledge management, etc. More and more researchers begin to pay attention to ontology research.

At the same time, case-based reasoning (CBR) as a traditional research domain of artificial intelligence is a problem-solving paradigm that in many respects is fundamentally different from logic-based approaches. CBR is able to utilize the specific knowledge gained from previously experienced, similar problem situations (case) to solve a new problem [1, 2]. Instead of relying on exact reasoning in a well-ordered world, CBR focuses on inexact reasoning by similarity measure between objects. And there are abundant research productions and enterprise applications about CBR.

However, CBR systems just like most of the knowledge-based systems (KBS) have some reusable ontological content but it is often influenced by the specific task, the restrictions of the representation language, and the specific inference procedures employed. So it is difficult to achieve integration between heterogeneous CBR systems.

Compared with so many researches that have been done to achieve integration between heterogeneous CBR systems, ontology-based CBR system has become a hot topic and the trend of development [3, 4]. The reasons are as follows: the structure of domain knowledge is clarified by ontology that lays foundation of knowledge acquisition and knowledge expression and avoids analyzing domain knowledge repeatedly; Unifying domain terminologies and concepts by ontology make knowledge sharing possible. However, research about ontology-based CBR is at the initial stage, which still faces many problems, for example, its architecture is nonstandard, reusing knowledge in legacy CBR is deficient, the so called knowledge acquisition bottleneck (common for every KBS) is still there, and it is time-consuming and labor-intensive even by the aid of ontology editor to construct ontology, etc. To solve the problems above, we propose an approach for semi-automatic construct ontology-based CBR system whose architecture is based on two-layer ontology.

This paper is organized as follows: Section 2 discusses the architecture of ontology-based CBR system. Section 3 illustrates the approach for semi-automatic construction of ontology-based CBR system in detail. Section 4 introduces an application example. Finally, section 5 gives conclusions and the future work.

II. ARCHITECTURE

In nearly all ontology–based integration approaches, ontologies are used for the explicit description of the information source semantics. But there are different ways of how to employ the ontologies. In general, three gradually developing directions can be identified: single ontology approaches, multiple ontologies approaches and hybrid ontology approaches [5]. Single ontology approaches use one global ontology providing a shared vocabulary for the specification of the semantics (see fig.1a). All information sources are related to the global ontology. But if one information source has a different view on a domain, finding the minimal ontology commitment becomes a difficult task. In multiple ontology approaches (see fig.1.b), each information source is described by its own local ontology, and inter-ontology mapping identifies semantically corresponding terms of different local ontologies. When a local ontology
changed, only need to change relevant parts affected. But in practice the lack of a common vocabulary makes it extremely difficult to compare different local ontologies. The inter-ontology mapping is very difficult to define because the many semantic heterogeneity problems may occur. To overcome the drawbacks of the single or multiple ontology approaches, hybrid ontology approaches were developed (see fig.1.c). In order to make the local ontologies comparable to each other they are built upon one global shared vocabulary which contains basic terms (the primitives) of a domain. But the drawback of hybrid ontology approaches is that existing ontologies cannot be reused easily and have to be re-developed from scratch, because all source ontologies have to refer to the shared vocabulary.

In order to make up for the deficiencies of the traditional architectures, we improve hybrid ontology approaches and introduce the architecture based on two-layer ontology approach (see fig.1.d).

In the process of CBR, case retrieval is vital. In traditional view, CBR systems provide a search functionality that makes use of similarity measures for ranking results according to their utility with respect to a given query. And the similarity measure is of critical importance during the retrieval of knowledge items for a new query and it assesses the utility of a knowledge item only based on the characterization. However, based on the architecture of two-layer ontology, the measure of concept similarity can be applied to similarity model of CBR, which makes case retrieval more reasonable and assesses the utility of a knowledge item not only based on the characterization but also based on the concept hierarchy of OWL domain ontology. The practical case retrieval can be achieved by implementation of the case retrieval algorithm that we proposed in reference [6].

III. THE APPROACH FOR SEMI-AUTOMATIC CONSTRUCTION OF ONTOLOGY-BASED CBR SYSTEM

The approach flow of semi-automatic construction of ontology-based CBR system is shown as fig.2, which comprises mainly two parts: OWL local ontologies learned from case bases and semi-automatic construction of OWL domain ontology.

A. OWL Local Ontology Learned from Case Base

1) Acquiring relational database schema and knowledge item about case and rule

The main elements of relational database schema consist of the base table structure design and declaration of integrity constraint. They being the current status message of database are stored in data dictionary. The general relational database schema extraction approach is to use API such as ODBC API, JDBC API to eliminate heterogeneity of different RDBMS. The development of this technology is mature; so we don’t discuss it any more. The knowledge items about case and rule stored in tuples of relational tables can be acquired and operated by SQL sentence directly.

2) Mapping knowledge in case base to OWL local ontology automatically

Source data of mapping is based relational model, which is comprised of relational database schema information and tuples of relational table. The goal of mapping is OWL ontology that is a rich semantic model with more complicated structure.

**Definition 1** Relational database schema is comprised of a set of name and a set of constraint. Thereinto, the name set is comprised of table name set, data type name set and column name set; the constraint set is comprised of primary key constraint, foreign key constraint, domain constraint, unique constraint and not null constraint.

**Definition 2** OWL ontology is comprised of an optional ontology identifier set and a set of axiom. Thereinto, ontology identifier set is comprised of class identifier, object property identifier, data type property identifier and individual identifier; Axiom set is comprised of class axiom, property axiom and individual axiom.

Based on the formal definitions above and reference from correlative researches [7-10], tables are classified as entity tables and relationship tables that are mutually exclusive. There is single primary key in entity table, and there are multiple primary keys in relationship table. Then mapping relationships about source data and mapping goal are as follows: a entity table maps to a OWL class identifier and a class axiom; a relationship table maps to two object property identifiers and two property axioms indicating that they are inverse; a column who is not a foreign key and its domain constraint maps to a data type property identifier and a property axiom; a
column who is a foreign key and its foreign key constraint maps to a object property identifier and its property axioms; data type name maps to data type identifier which is a predefine XML Schema data type identifier used in OWL ontology; each of unique constraints, not null constraints and primary key constraints maps to a property restriction about cardinality constraint; if the primary key of a table is a foreign key referring to another table, then maps to a class axiom which describe that one class is subclass of another; a tuple of table maps to a individual identifier and its individual axiom set.

Based on the mapping relationship above, an automatic mapping algorithm is proposed in this paper; its flow is shown in fig.3. From the angle of function, domain knowledge implied in relational database schema of case base is mapped to the elements of OWL local ontology by step 1 and step 2, the domain knowledge items about cases and rules are mapped to the elements of OWL local ontology by step 3.

![Fig. 3 The Flow of Automatic Mapping Algorithm](image)

Theoretical analysis of this algorithm’s time performance is discussed as follows:

All operations about identifiers construction can be involved in the operations about relevant axioms construction. So the basic operation of this algorithm can be considered an axiom construction. Define the scale of a CBR system as $N = N_T + N_A + N_i$, where $N_T$ is the amount of all tables, $N_A$ is the amount of all columns and $N_i$ is the amount of tuples of all tables. For the first step, the extreme scenario is that all tables in database are entity table, and then the amount of the basic operation about class axioms construction is less than $N_T$. In the second step, there are two different situations; for entity table, the amount of basic operation is less than $4N_A$, and for relationship table, the amount of basic operation is less than $N_T$. For the third step, the amount of basic operation about individual axioms construction is less than $N_A \times N_i$. So in the worst case scenarios, the total amount of basic operations is $T$, where $T = N_T + 4N_A + N_T + N_A \times N_i < N^2$, then the time-complexity is lower than $O(N^2)$.

A. Semi-automatic constructing OWL domain ontology

The OWL local ontologies acquired by the approach above are lightweight and concept hierarchies are too horizontal. It is very difficult to construct domain ontology based on them manually. So we propose an approach for semi-automatic construct OWL domain ontology by using FCA technology and computing concept equation measure and concept inclusion measure.

The semantic relations between concepts are established based on similarity measure. Based on the definitions of similarity in references [11], concept similarity measure is
categorized as concept equation measure and concept inclusion measure in this paper. The definitions are introduced as follows.

**Definition 3** Given two classes C₁ and C₂, a concept equation measure is defined as a real-valued function as follows:

\[ \text{Equ}(C₁ \times C₂) \rightarrow [0,1] \]

(1)

The value of \( \text{Equ}(C₁, C₂) \) indicates the probability that \( C₁ \) and \( C₂ \) represent the same concept. The function of \( \text{Equ} \) ought to be reflexive and symmetric.

**Definition 4** Given two classes \( C₁ \) and \( C₂ \), a concept inclusion measure is defined as a real-valued function as follows:

\[ \text{Sub}(C₁ \times C₂) \rightarrow [0,1] \]

(2)

The value of \( \text{Sub}(C₁, C₂) \) indicates the probability that \( C₁ \) is a subclass of \( C₂ \). In other words, the concept represented by class \( C₁ \) is a sub-concept of represented by class \( C₂ \).

The approach is described in detail as follows.

1) **Initialization and defining similarity matrix**

Not all concepts (OWL classes) in OWL local ontologies are similar, or have semantic relationship. In order to reduce computing concept equation measure and concept inclusion measure and improve the efficiency of recommending concept hierarchy of domain ontology, a set of similar ontology concepts and relevant property sets should be chosen as initial information.

The process of choosing similar concepts is described as follows: To some class \( C₁ \) in OWL local ontology, firstly, find out the most similar OWL class set \( C \) according to the name similarity of OWL classes; secondly, find out the super-class and subclass set about class \( C₁ \) based on concept hierarchy assertion about class \( C₁ \) in OWL local ontology; finally, define the initial class set \( C = C₁ \cup C \). Now the initial information is determined as the class set \( C \) and relevant property sets. Thereinto, we adopt the Levenstein edit distance to compute string similarity measure, because all class names are string.

Construction of the similarity matrix is based on computing similarity between properties. So in the following, computing similarity between properties will be discussed, then an example of similarity matrix will be introduced.

There are some primary elements of OWL property such as name, range and cardinality constraint. So these elements must be considered when the similarity of two properties is computed. The following is the formula of property similarity measure in this paper:

\[ \text{ASim}(a₁, a₂) = \omega₁ \times \text{ASim}_\text{name}\ + \omega₂ \times \text{ASim}_\text{range}\ + \omega₃ \times \text{ASim}_\text{cardinality} \]

where \( \omega₁, \omega₂, \omega₃ \) are weights, which represent the importance degrees for property similarity measure about name, range, cardinality constraint respectively; \( \omega₁ + \omega₂ + \omega₃ = 1 \) and \( \omega₁ > \omega₂ > \omega₃ \). \( \text{ASim}_\text{name} \) measured by Levenstein edit distance is the similarity of property name. \( \text{ASim}_\text{range} \) is the similarity of property range. There are two types of property in OWL ontology. Based on the different property types, different strategies are launched as follows: For two properties \( a₁ \) and \( a₂ \), if types of \( a₁ \) and \( a₂ \) are different, then \( \text{ASim}_\text{range} = 0 \). If both \( a₁ \) and \( a₂ \) are objectproperty, then \( \text{ASim}_\text{range} = \text{Sim}_\text{rangi}(a₁, \text{range}(a₂)) \), in other words, \( \text{ASim}_\text{range} \) is the name similarity between OWL classes which are ranges of \( a₁ \) and \( a₂ \). If \( a₁ \) and \( a₂ \) are datatyproperty, then \( \text{ASim}_\text{range} \) is computed according to data types of \( a₁ \) and \( a₂ \). The match degree between different data types is based on TABLE I. \( \text{ASim}_\text{card} \) is the similarity of property cardinality constraint. If the cardinality constraints of \( a₁ \) and \( a₂ \) are same, then \( \text{ASim}_\text{card} = 1 \), else \( \text{ASim}_\text{card} = 0 \).

Example 1 There are two similar classes \( C₁ \) and \( C₂ \), the relevant property sets are \( A₁ = \{a₁₁, a₁₂, a₁₃, a₁₄\}, A₂ = \{a₂₁, a₂₂, a₂₃, a₂₄, a₂₅\} \). The similarity matrix, \( \text{Matrix} M_{ij} \) of \( C₁ \) and \( C₂ \) is given in table II.

2) **Clustering concept by FCA**

FCA was introduced as a mathematical theory modeling the concept of “concepts” in terms of lattice theory. The basics of FCA theory needed for this paper can be found in references [12, 13]. The process of concept lattice generated from a formal context is a process of concept clustering. In this paper, clustering concept by FCA mainly includes constructing formal context and generating relevant concept lattice.

Different properties of classes can indicate different correlative relations between these classes, so we should construct different formal context for different classes and properties. The process of construction formal context includes two steps:

a. Based on the initialization, construct initial formal context in which the set of classes \( C \) as objects, the set of properties \( A \) as characteristics; The initial formal context is \( \text{K}=(G, M, I) \), where \( G = C, M = A \) and \( I = C \times A \).

b. Based on the similarity matrixes between classes, \( \text{Matrix} \) amend the formal context that has been constructed. In order to determine the relationship of OWL class \( C₁ \) and the properties of another OWL class \( C₂ \), in this step, the possibility of class \( C₁ \) having the characteristics described by the properties of \( C₂ \) should be acquired, and then the formal context should be amended.

For Example 1: In order to decide the relations between class \( C₁ \) (or \( C₂ \)) and \( A₂ \) (or \( A₁ \)), the formal context is amended based on the similarity matrix \( M_{ij} \). The sub-steps of this process include:
Firstly, for each i and j, with i ∈ {1,...,p}, j ∈ {1,...,q}, acquire the similarity between a_{ii} and a_{jj} from Matrix M_{ij}, where a_{ii} ∈ A_1 and a_{jj} ∈ A_2.

Secondly, for each a_{ij} ∈ A_1, find the property from A_2 which has the highest similarity with a_{ij}, named as MaxSimwith_{a_{ij}}. And MaxSimwith_{a_{ij}} = \{a_{jj} | j = arg \max_{j \in \{1,...,q\}} \{\text{Similarity}(a_{ii}, a_{jj}) \neq 0\} \} \subseteq A_2 \quad (4)

And for each a_{ij} ∈ A_2, find the property from A_1 which has the highest similarity with a_{ij}, named as MaxSimwith_{a_{ij}}. And MaxSimwith_{a_{ij}} = \{a_{ii} | i = arg \max_{i \in \{1,...,p\}} \{\text{Similarity}(a_{ii}, a_{jj}) \neq 0\} \} \subseteq A_1 \quad (5)

For Matrix M_{ij}, MaxSimto_{a_{ij}} = a_{2i}, MaxSimto_{a_{ij}} = a_{22}, MaxSimto_{a_{ij}} = a_{23}, MaxSimto_{a_{ij}} = a_{24}, MaxSimto_{a_{ij}} = a_{25}, MaxSimto_{a_{ij}} = a_{11}, MaxSimto_{a_{ij}} = a_{15}, MaxSimto_{a_{ij}} = a_{13}, MaxSimto_{a_{ij}} = a_{14}.

Finally, let P(c, a) means the possibility of class c having the characteristics described by the property a, and according to the possibility, construct amended formal context.

For Example 1, P(c_{1}, a_{12})= Similarity(MaxSimto_{a_{22}}, a_{12}), P(c_{1}, a_{13})= Similarity(MaxSimto_{a_{13}}, a_{13}), and if (c, a) ∈ I, then (c, a)=1. The amended formal context is given in Table III.

Based on the amended formal context, we use the mark “×” to replace every real number that is more than threshold ε, and then acquire a simple value formal context. Here, ε is determined by users according the practical situations. So the existing methods and algorithms can still be used to generate concept lattice [12,13]. We use the tool of ConExp to generate relevant concept lattice [14], and an example will be introduced in section IV.

### 3) Computing concept equation measure and concept inclusion measure

Compared with FCA theory, intention of concept is more important for ontology, so we compute concept similarity according to properties of OWL ontology in this paper. In other words, if the properties of two concepts are same, then the two concepts are same; if the properties of two concepts are similar, then the two concepts are similar. Based on the concept lattice generated above, we can compute the equation measure and inclusion measure. The detailed steps are as follows:

For OWL class c ∈ G, compute the probability that c belongs to the formal concept represented by the node which c is associated with in the foregoing concept lattice, denoted by P(c):

\[ P(c) = \prod_{a_i \in I} P(c, a_i) \]

where

\[ a_i \in \{c\}' \cup \{c\} = \{a \in M | (c, a) \in I\} \]

Based on the generated concept lattice, analyze OWL class c_{1} and c_{2}, if \[ \{c\}' = \{c\}' \], then Sub(c_{1}, c_{2}) = P(c_{1}) \times P(c_{2}) ; analyze OWL class c_{1} and c_{2}, if \[ \{c\}' \subset \{c\}' \], then Sub(c_{1}, c_{2}) = P(c_{1}) \times P(c_{2}) .

### 4) Recommending domain ontology

The semantic relationships between concepts of OWL ontology are mainly described by axioms about subClassOf(), equivalentClasses(), disjointClasses() and disjointUnion()[15]. We mainly discuss automatic recommending axioms about subClassOf() and equivalentClasses() in this paper. The approach is introduced as follows: automatic recommend that the two concepts whose concept equation measure is more than the threshold δ are same; automatic recommend that the two concepts whose concept inclusion measure is more than the threshold η have super-sub relationship; then users determine to weather accept the recommendations of not. For example: if the concept equation measure between OWL class c_{1} and c_{2} is more than δ, then the axiom of equivalentClasses(c_{1}, c_{2}) will be recommended to users; if the concept inclusion measure between OWL class c_{1} and c_{2} is more than δ, then the axiom of subClassOf(c_{1}, c_{2}) will be recommended to users.

At the same time, generated concept lattice can show the super-sub relationship between concepts as Hasse diagram vividly and compactly. It can help designer to analyze the relationship between concepts and find new concept, and then aid designer to construct OWL domain ontology and rich the concept hierarchy of OWL domain ontology.

### IV. IMPLEMENTATION

In order to evaluate the approach proposed above, we take a legacy CBR system about tooling man-hour rationing as an example, and experimental study semi-automatic construction of relevant ontology-based CBR system.

The main task of this legacy CBR system is to aid engineers to rapidly ration a suit of tooling whose structure is complex according to existed experiments, which is empirical and predictive. There are two types of knowledge in this system: tooling cases and tooling characteristic rules. They are stored in relational database. Tooling cases are facts knowledge that were rationed by engineer and proved right. Every tooling case consists of qualitative characteristic description (for example type of accessory processed), quantitative characteristic description (for example the size of die core), relevant quotiety and man-hour value. Tooling characteristic rule knowledge mainly provides extra domain knowledge and vocabulary. They consist of typical descriptions about tooling characteristic information and relevant quotiety that represents the influence degree contrasting current description to the benchmark description about tooling characteristic.

The mapping algorithm has been implemented based on J2SE v 1.4.2 and Jena2 API (mainly based on the interfaces and relevant methods in the packet com.hp.hpl.jena.ontology). In order to validate the automatic mapping algorithm, five sets of cases and relevant rules were mapped to OWL local ontology, and the result show that the relation between the practical running time of the algorithm and the problem scale N is...
consistent with the theoretical analysis (better than $N^2$ curve). Now take the reduced forging-lancing die case table and relevant five rule tables as an example, E-R diagram of them is shown as fig.4.

![Fig. 4 The E-R diagram of the instance](image)

The amount of relevant tuples in forging-cutting die case table, structure type rule table, accessory processed type rule table, type of parting surface rule table, depth and width ratio of cavity rule table and amount of module rule table are 6, 3, 5, 6, 3, 4 respectively. The mapping result is shown as fig.5.

![Fig. 5 The relevant result of automatic mapping](image)

Axioms in the result consist of 6 class axioms, 17 data type property axioms, 5 object property axioms, 22 axioms about cardinality constraint and 124 individual axioms. It can be seen that it is consistent with the theoretical result, and the implementation is correct.

In order to assess the recommendation about concept hierarchy of domain ontology got by the approach of semi-automatic construction OWL domain ontology, we use standard information retrieval metrics \[ r = \frac{\text{correct \ recommendation}}{\text{existing}} \]

\[ p = \frac{\text{correct \ recommendation}}{\text{all \ recommendation}} \]

\[ F = \frac{2rp}{p + r} \]

Here take a set of concepts about metal die cases as an example. There are 31 OWL classes in this set of concepts. According to this set of OWL classes and relevant properties, formal context was constructed as fig.6, and then relevant concept lattice was generated which is shown as fig. 7. Concept count is 32, edge count is 59 and lattice height is 8. Then concept hierarchy was recommended and OWL domain ontology was constructed. It is found: $r=0.571$, $p=0.693$, $F=0.626$.

![Fig. 6 The formal context instance](image)

It can be seen that the approach of FCA-based semi-automatic domain ontology construction is valid and satisfying. Applying it can aid designer to construct OWL domain ontology effectively.

V. CONCLUSION

We have presented a practical approach for constructing ontology-based CBR system semi-automatically. Its advantages are summarized as follows: its architecture is based on two-layer ontology which can make up for the deficiencies of existing methods; knowledge in legacy CBR can be reused by the greatest extent; OWL local ontology can be mapped...
from case base automatically; semi-automatic construction of OWL domain ontology can be aided by recommendations and Hasses diagram of concept lattice that are generated by FCA and computing concept equation measure and concept inclusion measure.

In the next work, we will focus on the research about ontology evolution.

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