A Fault Tolerant Token-based Algorithm for Group Mutual Exclusion in Distributed Systems

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Abstract—The group mutual exclusion (GME) problem is a variant of the mutual exclusion problem. In the present paper a token-based group mutual exclusion algorithm, capable of handling transient faults, is proposed. The algorithm uses the concept of dynamic request sets. A time out mechanism is used to detect the token loss; also, a distributed scheme is used to regenerate the token. The worst case message complexity of the algorithm is $n+1$. The maximum concurrency and forum switch complexity of the algorithm are $n$ and $\min(n, m)$ respectively, where $n$ is the number of processes and $m$ is the number of groups. The algorithm also satisfies another desirable property called smooth admission. The scheme can also be adapted to handle the extended group mutual exclusion problem.

Keywords—Dynamic request sets, Fault tolerance, Smooth admission, Transient faults.

I. INTRODUCTION

The mutual exclusion is a classical problem of distributed systems. Joung [1] proposed the group mutual exclusion (GME) problem, a generalization of the mutual exclusion problem, and modeled it as the congenial talking philosophers (CTP) problem. In group mutual exclusion, a process requests a resource type (group) before entering its critical section (CS). Processes requesting the same group are allowed to be in their CS simultaneously. However, processes requesting different groups, must execute their CS in mutually exclusive way. The time interval in which all critical sections executed are of the same type is called a ‘session’. An interesting application of GME is, when several users share large data objects stored in some secondary storage (such as CD’s), and only one data object can be loaded in the buffer at a time. A solution of group mutual exclusion problem must satisfy the following requirements:

Safety: No two processes, requesting different groups, can be in their critical sections concurrently.

Starvation Freedom: A process attempting to attend a session will eventually succeed.

Concurrent Occupancy: If some process $P$, has requested a group $X$, and no philosopher is currently attending or requesting a different group, then $P$ can attend $X$, without waiting for any other process to leave the CS. The term ‘concurrent occupancy’ was first used by Kean and Moir in [2].

Joung solved the GME problem for shared memory systems in [1]. Later on, a number of solutions were proposed using different approaches like, permission-based algorithm [3], token-based algorithms [4-10], and non token-based solutions [11-13]. Out of them, there are only three token-based algorithms for fully connected networks: Mittal-Mohan’s TokenGME [8], Mamun-Nazakato algorithm [6] and Swaroop-Singh algorithm [10]. Mittal-Mohan’s TokenGME, which is based upon Suzuki-Kasmi algorithm [14], uses two types of tokens, primary token and secondary tokens. The algorithm uses static request sets and its message complexity is $2^\frac{n}{n-1}$. In Mamun-Nazakato algorithm, a session is opened for a predefined time and processes are made aware about it, through broadcast. The processes interested in the currently open session, may join it without incurring any message overhead. However, the algorithm needs that the processes maintain synchronized logical clocks. In [10] Swaroop and Singh presented a token-based algorithm in which each process announces a priority level along with its request. The worst case message complexity of the algorithm is $n+1$. The algorithm favors the request with higher priority levels. This feature makes the algorithm suitable for soft real time distributed systems. The concept of aging is used to remove the possibility of starvation. The algorithm presented in [10] assumes that all channels and processes are reliable.

The token-based algorithms are susceptible to token loss and token has to be regenerated in case token is lost in transit or the site holding the token fails. In the present paper, we propose a token-based algorithm, called DRS_GME henceforth, to solve the group mutual exclusion problem. Our algorithm uses the concept of dynamic request sets. Chang, Singhal, and Liu [15] used the dynamic request sets in their algorithm to solve the classical mutual exclusion problem. The proposed algorithm is capable of handling transient faults [16]. The algorithm also satisfies a desirable property called smooth admission [17], which ensures that when captain is in its critical section, a process requesting for the same group is
allowed to enter in its CS immediately by the captain. The use of dynamic request sets reduces the number of messages per CS request considerably, when the system is lightly loaded. The reason is that the cardinality of request sets will be far less than \( n-1 \) in that case. In the proposed scheme, a captain process is responsible for the session initiation and sending ‘start’ message to other processes requesting the same resource type as requested by the captain, in order to allow them to enter in CS as follower. The algorithm uses a distributed scheme, adapted from Manivannan and Singhal [18], for the token regeneration. A timeout mechanism detects message losses due to site failure and (or) communication link failure.

II. SYSTEM MODEL

We assume that the system has \( n \) sites, numbered as 1,2,3,…,\( n \). The only way of communication between sites, is through message passing. The system is fully logically connected. We assume that, at each site \( i \), there exists exactly one process \( P_i \). Hence, we can use site and process interchangeably. The maximum message delay and the time for which a process can be in its CS are bounded. We also assume that only transient faults occur in the system, and failed sites and (or) communication links will eventually recover. The sites have stable storage (which survives failure), to store local variables.

III. THE DATA STRUCTURES

In our algorithm, the token is a message, which contains an FCFS queue, namely \( \text{token.queue} \), in order to store all pending requests. The token stores the number of the last completed session in \( \text{token.session} \). The token contains two more variables (a) \( \text{token.type} \) that stores the type of current session and (b) \( \text{token.followers} \) that stores the number of follower processes. The requests for the same resource are grouped together and treated as one entry in the \( \text{token.queue} \).

Each process may be in any one of the following six states: \( N \) (Not requesting), \( R \) (Requesting), \( EC \) (Executing in CS as captain), \( EF \) (Executing in CS as follower), \( HS \) (Captain but not in CS), and \( HI \) (Holding token because no request is pending).

The process \( P_i \) at site \( i \), has the following local variables:

- \( \text{state} \) - the current state of \( P_i \)
- \( \text{captain} \) - stores the \( id \) of its captain.
- \( SN \) - is an array of sequence numbers.
- \( RS \) - request set of site \( i \).
- \( \text{old_token} \) - a copy of the token is stored in it.
- \( \text{TGI} \) - indicates whether the token regeneration process has been initiated by site \( i \).
- \( \text{follower} \) - is the set of follower

IV. THE ALGORITHM

The pseudo code of the algorithm is given in Appendix A; however, for reader’s convenience a high level description of the algorithm is presented in this section. Our algorithm uses the dynamic request sets technique and each site stores in its request set the process identifiers, called \( id \) henceforth, of sites which are possibly holding the token. This request set changes dynamically as the execution progresses. The sequence numbers are used to differentiate between old delayed requests and new requests. There exists a unique valid token and the process, holding this token only, may initiate a session and may work as captain. Initially the process \( P_i \) holds the token. A process \( P_j \) requesting a resource sends its request to all members in its request set, if it is not holding the ‘valid’ token. However, if it is holding the valid token in state \( HI \), it immediately enters in its CS as captain. If \( P_i \) is in state \( HS \), it enters in its CS only if the requested resource type is the same as the \( \text{token.type} \) and the \( \text{token.queue} \) is empty; otherwise, the request is added in \( \text{token.queue} \).

When a process \( P_i \) holding the valid token receives a request from \( P_j \) for the resource type \( X \), it transfers the token to \( P_j \) immediately, if \( \text{state} \) is \( HI \). If \( P_i \) is in state \( N, R \), or \( EF \) it adds \( P_j \) in its request set if \( P_j \) is not already there. Furthermore, \( P_i \) also sends a request message to \( P_j \), if \( P_j \) is not in \( RS \); and \( \text{state} \) is \( R \). When the request of a process reaches the captain which is executing in its CS, It issues a ‘start’ message to all of its followers, if \( X \) is the same resource as \( \text{token.type} \). However, if the request is conflicting, it is added in the \( \text{token.queue} \). Furthermore, in order to remove the possibility of starvation, if the captain is in state \( HS \), it issues a ‘start’ message only if the request is of the same type and there are no conflicting pending requests.

A process upon receiving a ‘start’ message enters in its CS as follower and sends a ‘complete’ message to its captain upon exiting from its CS. When a captain process comes out of its CS, it waits till all its followers have come out of CS and only then it selects next captain from the front of the \( \text{token.queue} \) and passes the token to the next captain if any; otherwise, it holds the token in state \( HI \). Whenever a captain process transfers the token to new captain the copy of the token is stored in a local variable \( \text{old_token} \), which is used in token regeneration process. Furthermore, the \( \text{id} \) of processes, which can work as future captain, are added in the request set of current captain before transferring the token to the new captain. As soon as a process \( P_i \) receives a valid token (\( \text{old_token}, \text{session}<\text{token.session} \)) it empties its request set, delete entry at the front of the \( \text{token.queue} \), sends an start message to all of its followers, and enters in its CS.

In our algorithm Timer \( T1 \) is used for detection of loss of a token or request message and timer \( T2 \) is used for detection of loss of a start or complete message. When timer \( T1 \) exceeds the value \( T_{req} \) the requesting process \( P_i \) suspects token loss and it sends the message \( \text{gen_token} \) (\( i, SN, X, \text{session} \) for token regeneration to all processes including itself and sets a boolean flag \( \text{TGI} \) to indicate that a token regeneration process has been initiated by site \( i \). This flag is reset, when \( P_i \) receives a token or ‘start’ message. When a process \( P_j \) holding token receives a request for token regeneration it treats it as a CS request and takes action accordingly. However, if \( P_j \) is not holding token and \( P_j \) has executed in its CS as captain at least
once after \( P_i \) has executed in its CS as captain then \( P_j \) generates a new token with the help of \( old_token \). \( P_j \) selects new captain from \( old_token,queue \) and sends the newly generated token to it. When a process \( P_j \) receives a token, it checks whether the session number of new token is greater then that of older one. If so, it accepts the newly received token as valid token; otherwise, the token is deleted.

When timer \( T_2 \) of the captain node expires, it suspects the loss of message ‘complete’ or ‘start’ and sends the message \( is\_complete(j,X) \) to all its follower sites from where it has not yet received the message ‘complete’. Upon reception of ‘is_complete’ message, there could be three possibilities: (a) if \( P_j \) is in state \( EF \) then \( P_j \) ignores it, (b) if \( P_j \) is requesting for session \( X \), it enters in its CS, and (c) otherwise, process \( P_j \) sends a ‘complete’ message to the captain.

The value of \( T_{req} \) should be chosen carefully so that a token loss is detected well in time and the false token losses go undetected. Let \( t_m \) be the maximum message delay and \( t_c \) be the maximum time period a process will be executing inside its CS. A reasonable value of \( T_{req} \) would be \((n+1)^*t_m + (n-1)^*t_c \). The suggested value for \( T_{req} \) is \( 2^t_m+ t_c \) because in \( 2^t_m+ t_c \) time the captain must have received a complete message from a follower.

**Example:** In order to provide convenience to the reader, we consider the following example. Let \( P_1, P_2, P_3 \) and \( P_4 \) be the four processes in the system and let \( g_1, g_2 \) and \( g_3 \) be the three groups. Initially \( token,queue \) is empty, \( RS_1=\emptyset, RS_2=\{1,3,4\}, RS_3=\{1,2,4\} \) and \( RS_4=\{1,2,3\} \). We consider following sequence of events:

(a) \( P_2 \) sends request for group \( g_2 \) to \( \{1,3,4\} \). \( P_2 \)’s request for \( g_2 \) reaches at sites \( \{1,3,4\} \). \( P_1 \) transfers token to \( P_2 \) and \( P_2 \) enters in its CS as captain.

(b) \( P_1 \)’s request for \( g_3 \) reaches at \( P_2 \) which is in CS.

(c) \( P_3 \) sends request for \( g_1 \) to \( \{1,2,4\} \). The request reaches at sites \( \{1,2,4\} \), however, \( P_2 \) still in CS.

(d) \( P_4 \) sends request for \( g_3 \) to \( \{1,2,3\} \). The request reaches at sites \( \{1,2,4\} \), however, \( P_2 \) still in CS.

(e) \( P_2 \) comes out of CS; \( P_2 \) adds 1 and 3 in its request set, selects \( P_1 \) as new captain, sends token to \( P_1 \). \( P_1 \) on receiving token sends start message to \( P_4 \).

Table I describes the changes in \( token,queue \) and Request sets with the occurrence of above mentioned events.

<table>
<thead>
<tr>
<th>event</th>
<th>token,queue</th>
<th>Request sets</th>
</tr>
</thead>
<tbody>
<tr>
<td>After event (a)</td>
<td>empty</td>
<td>( RS_1={2}, RS_2=\emptyset, RS_3={1,2,4}, RS_4={1,2,3} )</td>
</tr>
<tr>
<td>After event (b)</td>
<td>( g_3)</td>
<td>( RS_1={2}, RS_2=\emptyset, RS_3={1,2,4}, RS_4={1,2,3} )</td>
</tr>
</tbody>
</table>

### V. PROOF OF CORRECTNESS

In this section, we prove that DRS_GME satisfies the requirements of GME problem namely safety, Starvation freedom, and concurrent occupancy. Let, \( type(i) \) = type of resource being used by \( P_i \) and \( session(i) \) = latest session number executed or being executed by \( P_i \).

Following invariants hold in the system:

1. \( session(captain)=session(i) \)
2. \( type(captain)=type(i) \)

We take the help of the following boolean functions to prove the properties of our algorithm.

**Lemma 1.** There exists at most one valid token in the system.

**Proof:** We assume, initially \( P_1 \) has the token, hence, \( holds\_valid\_token(1)=true \) and \( holds\_valid\_token(i)=false \) for sites \( i \neq 1 \). This token is transferred from one captain to another captain as the algorithm progresses. In response to \( gen\_token(i,X,SN,session) \), a process \( P_i \) generates a token, only if the condition \( session<old\_token,session \) is satisfied. \( P_i \) transfers this newly generated token to the site to which it has sent the token most recently. A token received by a process \( P_i \) is valid only if \( old\_token,session < token,session \). All the invalid tokens are deleted immediately. The condition \( old\_token,session < token,session \) can be true for at most one token, which is generated by the site that executed in its CS as a captain most recently. Only one such site may exist in the system. Therefore, only one valid token will be retained.

**Safety:** If two processes are executing in their CS simultaneously then both the CS is of the same type.

**Proof:** Let us assume the contrary. The two processes \( P_i \) and \( P_j \) are in CS having their type as \( t_i \) and \( t_j \) (\( t_i \neq t_j \) respectively). Since \( P_i \) and \( P_j \) are in CS, \( state=EC \) or \( EF \) and similarly \( state=EC \) or \( EF \). Now, four cases are possible:

- **Case1:** \( state=state=EC \). This implies that both captain(i) and captain(j) are true. From lemma 1 we conclude that this is not feasible.
Case 2: state=state=EF. From lemma 1 we know that there exists only one captain. Therefore, captain = captain. On applying type function, we get type(captain) = type(captain). Now, from invariant (2) we can write type(i) = type(j). This contradicts the assumption.

Case 3: state=EC and state=EF. From state=EC, we observe that captain(i) true. Now, from lemma 1, only one captain exists in the system. Therefore, captain = i

On applying type function, we get type(captain) = type(i)

Now, from (2) we get type(j) = type(i), which contradicts the assumption.

Case 4: state=EF and state=EC. The proof is similar to case 3.

Therefore, it is proved that if two processes are executing in their CS then both the CS are of the same type.

Starvation Freedom: To show that a request will eventually be served following three conditions must be satisfied.

A request will eventually reach the site holding the valid token.

A request that reach the token holding site will be issued a ‘start’ or ‘token’ message to enter CS as follower or will be added in token.queue.

A request that is added in token.queue will eventually be served.

Lemma 2: \( \forall i, j : i \in RS_i \) or \( j \in RS_j \)

Proof: Initially \( RS_i = \Phi \) and for all \( i = 2 \) to \( n \), \( RS_i \) contains all other sites except itself. Hence, for any two sites \( i \) and \( j \), the condition is satisfied. Now, the request set of a site \( i \) changes in following conditions:

(i) Site \( i \) receives valid token: \( RS_i \) is emptied.

(ii) Site \( j \)'s request or message \( \text{gen}_j \) token reaches site \( i \) and site \( i \) is not holding token: \( j \) is added in \( RS_i \), if \( j \) is not in \( RS_i \).

(iii) Site \( j \) transfers token to new captain \( j \): In this case site \( i \) adds node \( j \) and other possible token holders in \( RS_i \), whose requests are in token.queue.

The entries from a request set are deleted only when condition (i) holds. However, at this time the site \( i \) will be in the request set of all other sites. Therefore, in all above three cases, the request sets changes in such a manner, that the condition \( \forall j : i \in RS_j \) or \( j \in RS_i \) remains true for any two nodes \( i \) and \( j \).

Lemma 3: A request will reach the valid token holding site, if \( \forall i, j : i \in RS_j \) or \( j \in RS_i \)

Proof: Suppose when site \( i \) makes a request, the valid token is held at site \( j \). Now, \( RS_i = \Phi \) because site \( j \) is holding the valid token; therefore, site \( j \) should be an element of \( RS_i \). Hence, site \( i \)'s request will reach at site \( j \). When node \( i \)'s request reach site \( j \), there are two possibilities: (i) \( j \) still holds the token and (ii) \( j \) has transferred the token to next captain, say \( k \). In case (i) the request of site \( i \) will reach the site holding valid token. In case (ii) if \( k \) is in \( RS_i \), site \( i \)'s request will reach site \( k \). However, if site \( i \) is in \( RS_k \), site \( k \) must have sent a request message to site \( i \). Consequently, site \( i \) will add site \( k \) in \( RS_i \), if site \( k \) is not in \( RS_i \). Furthermore, site \( i \) will send a request message to \( k \). Subsequently, site \( i \)'s request will reach the valid token holding site \( k \).

From lemma 2 and lemma 3 the first part of the starvation freedom is proved.

Now, we prove the second part of the starvation freedom. When a request \( (j, SN, X) \) reaches the token holding site \( i \), which may be in any one of the three states \( HI, EC \) or \( HS \).

Case 1: \( P_i \) is in state \( HI \): when \( P_i \) receives request from site \( j \) it will send a token message to \( j \).

Case 2: \( P_i \) is in state \( EC \): \( P_i \) will issue a ‘start’ message to \( j \) if \( token.type=X \); otherwise, the request is added in token.queue.

Case 3: \( P_i \) is in state \( HS \): If \( token.type=X \) and \( token.queue=\Phi \), a ‘start’ message is issued to \( j \) by \( i \); otherwise, the request is added in token.queue.

Now, we prove part three of the starvation freedom. In our algorithm token.queue is an FCFS queue and when a session terminates the token is transferred to the process at the front of the token.queue. Therefore, a request that is added in token.queue will eventually be served. Thus, part three of the starvation freedom will always be satisfied.

Hence, the algorithm ensures starvation freedom.

Concurrent Occupancy and Smooth Admission: In our algorithm, when a process starts execution in its CS as a captain, it sends ‘start’ message to the processes whose requests are stored in token.queue and requesting the same resource. When a captain process executing in its CS receives a request of the same type it issues a ‘start’ message to allow the requesting process to enter in its CS as follower and hence the algorithm satisfies ‘smooth admission’ property. However, if captain is in state \( HS \), it sends a ‘start’ message in response of a request of the same type only if \( token.queue=\Phi \) (no conflicting pending requests). A requesting process immediately enters in its CS as follower upon receiving a start message. Further if the token holding process is in state \( HI \), it will transfer the token as soon as it receives a request message. This implies that, the algorithm satisfies concurrent occupancy property.

VI. PERFORMANCE OF THE ALGORITHM

In this section we discuss the performance of our algorithm based upon following parameters: message complexity per CS request, average message size, forum switch complexity, maximum concurrency, synchronization delay. First, we analyze the performance of our algorithm in fault free scenario.

In the worst case \( n+1 \) messages needs to be exchanged \((n-1 \text{ ‘request’, one ‘start’ and one ‘complete’ message}) \) per CS entry. However in the best case no message needs to be exchanged. Among the messages used in the algorithm, only
the token has the size $O(n)$. Therefore, in the best case (all processes requesting for the same session), the average message size will be $O(1)$, because one token, $n-1$ ‘complete’ and some ‘request’ messages (depending upon the cardinality of the request sets at each site), will be exchanged. However, in the worst case (all processes requesting for a different session); $n$ token messages will be exchanged, besides the ‘request’ messages. Therefore, in this case the average message size will be $O(n)$.

In our algorithm all $n$ processes could be executing in their CS concurrently, if the system does not has any conflicting request pending. Hence, maximum concurrency of our algorithm is $n$. The requests for the same session are grouped together and treated as one entry in the $token.queue$. Therefore, at any point of time there can be at most $min(n,m)$ entries in $token.queue$. Therefore, the forum switch complexity of the algorithm is $min(n,m)$.

The synchronization delay of a distributed algorithm generally considered when the system is heavily loaded. Under heavy load conditions, there will always be some request pending, in $token.queue$. Hence, immediately, after captain comes out of its CS and no follower is in its CS, the token is passed to the next captain. Therefore, the heavy load synchronization delay is $t_w$. However, if the last process exited from CS is a follower, it would send a ‘complete’ message to the captain that, in turn, terminates the session passing the token to next captain. Therefore, the synchronization delay would be $2t_w$.

Performance in case of message loss: If a token regeneration process has been initiated by site $i$, it sends a ‘gen_token’ message to all sites including itself. If site $j$ satisfies the condition $session \subseteq old_token.session$, it would generate a token and forward it to the site to which $j$ had sent the token most recently. In the worst case, $n$ such tokens may be generated and $2n$ ($n$ ‘gen_token’ and $n$ token) extra messages are exchanged for token generation. However, in the best case, only one site may satisfy the above mentioned condition and only $n+1$ ($n$ ‘gen_token’ and one token) extra messages need to be exchanged.

In case, loss of ‘complete’ or ‘start’ message is suspected, the captain sends ‘is_complete’ message to all members of $follower$, after timer $T_2$ expires (value of $T_2$ exceeds $T_{sw}$). $follower$, stores id of the processes to which ‘start’ message has already been sent and ‘complete’ message is yet to be received from them. Therefore, after expiry of timer $T_2$, $follower$, will contain id of only those processes whose ‘complete’ message is lost or which could not finish their CS in time. In our scheme, two extra messages are required for each ‘complete’ message that was lost, and one extra message for the sites, which are not able to send ‘complete’ message in time.

VII. EXTENSION OF THE ALGORITHM TO SOLVE EXTENDED GME PROBLEM

Manabe and Park [10] suggested a modification of the GME problem and named it the Extended GME problem, in which a process is allowed to specify more than one resource type, while making a request. The request made by a process is serviced if the process can be allowed to join any one of the requested sessions. The Extended GME problem removes the possibility of unnecessary blocking.

The proposed algorithm can be modified to solve the Extended GME problem. The ‘request’ message is modified, and a process $P_i$, specifies a set of resource types $SX$ in its ‘request’ message instead of specifying only one type. The process sends such ‘request’ message to all processes whose $id$ is in its request set. When ‘request’ message reaches at the token possessing process $P_j$, $P_j$ checks whether the current session $X$ is in $SX$, and $token.queue$ is empty. If so, $P_j$ sends start$(j,X)$ message to $P_i$. Otherwise, $P_j$ creates multiple entries of $P_i$ in $token.queue$, one for each member of $SX$. When a process $P_i$ receives token, it deletes all entries of $P_i$ in the $token.queue$. Similarly, when a process $P_i$ sends start$(i,X)$ message to process $P_j$, $P_j$ deletes all entries related to process $P_i$ from $token.queue$.

VIII. CONCLUSION

The proposed scheme satisfies the strongest fairness requirement, i.e. FCFS, in addition to the properties like safety and concurrent occupancy. The algorithm satisfies another desirable property called smooth admission. The maximum concurrency of the algorithm is $n$ and the forum switch complexity is $min(n,m)$. Due to its fault tolerant feature, the scheme is of practical significance rather than being only of theoretical interest. More importantly, the scheme can be applied to another, more complex problem, that is, the extended GME problem. The concept of dynamic request sets has appeared earlier in the literature, nevertheless, its application to handle GME and extended GME problem, is the novelty of the present work. Due to the use of dynamic request sets the algorithm performs better than the algorithms using static request sets when the system is lightly loaded. The comparative performance analysis of the proposed algorithm with other existing schemes is being postponed for the full paper.

APPENDIX

A. The Pseudo Code of the Algorithm DRS_GME

Initialization:

For $i = 1$ to $n$

state,$=$N; captain,$=$NULL
$RS_i=$ {ids of all processes except $P_i$}
follower,$=$Ø; TG$[i]$=false
old_token/session,$=$Ø;
old_token/queue,$=$Ø;
old_token/type=$NULL;
old_token/followers,$=$0

For $j = 1$ to $n$

$SV[j]$=0
state,$=$HI; $RS_j=$Ø
token/type=$NULL$; token/queue,$=$Ø
token/followers,$=$0; token/session,$=$0
Event 1: \( P_i \) request for a forum \( X \)

\[ \text{Switch}(\text{state}) \]

Case HI:

- \( \text{token.type}=X; \) \( \text{state}=\text{EC} \)
- \( ++\text{token.session} \)
- \( \text{token.followers}=0; \) Enter CS

Case HS:

- If (\( \text{token.queue}=\emptyset \)) \&\& (\( \text{token.type}=X \)) \( \text{state}=\text{EC} \)
- Enter CS

Else

- Add request \((i, \text{SN}[i], X)\) to \( \text{token.queue} \)
- Start timer \( T1 \)

Default:

- \( \text{state}=R; \) Start timer \( T1 \)
- Send request \((i, \text{SN}[i], X)\) to all members of \( RS_i \)

Event 2: \( P_i \) receives request \((j, \text{SN}, X)\)

If \( \text{SN}=\text{SN}[j] \) \(/\!*\!\text{otherwise old request}*/\)

\[ \text{SN}[j]=\text{SN} \]

Switch (state)

Case R:

- If \(( j \notin RS_j \))
  - Add \( j \) to \( RS_j \)
  - Send request \((i, \text{SN}[i], Y)\) to \( P_j \)

Case EC:

- If \( \text{token.type}=X \)
  - \( ++\text{token.followers} \)
  - Reset timer \( T2 \)
  - Add \( j \) to \( \text{follower}_i \)
  - Send start \((i)\) to \( P_j \)

Else add request \((j, \text{SN}, X)\) to \( \text{token.queue} \)

Case HI:

- Add \( j \) to \( RS_i \)
- Add request \((j, \text{SN}, X)\) to \( \text{token.queue} \)
- \( \text{old_token}=\text{token} \)
- Send \( \text{token}(\text{token.queue}, \text{token.type}, \text{token.followers}, \text{token.session}) \) to \( P_j \)

Case HS:

- If \( \text{token.type}=X \) \&\& (\( \text{token.queue}=\emptyset \))
  - \( ++\text{token.followers} \)
  - Reset timer \( T2 \)
  - Add \( j \) to \( \text{follower}_i \)
  - Send start \((i)\) to \( P_j \)

Else Add request \((j, \text{SN}, X)\) to \( \text{token.queue} \)

Default:

- If \(( j \notin RS_j \)) Add \( j \) to \( RS_j \)

Event 3: \( P_i \) receives start \((j)\)

If \((TGI=\text{true}) \text{TGI=\text{false}}\)

Close timer \( T1 \)

- \( \text{captain}=j; \) \( \text{state}=\text{EF}; \) Enter CS

Event 4: \( P_i \) exits from CS:

If \( \text{state}=\text{EF} \)

- Send complete \((i)\) to \( \text{captain} \)
- \( \text{captain}=\text{NULL}; \) \( \text{state}=\text{N} \)

Else

- If \( \text{token.followers}=0 \) \&\& (\( \text{token.queue}=\emptyset \))
  - Close timer \( T2 \)
  - \( \text{state}=\text{HI}; \) \( \text{token.type}=\text{NULL} \)
  - \( \text{old_token}=\text{token} \)
  - If \( \text{token.followers}=0 \) \&\& (\( \text{token.queue}=\emptyset \))

Close timer \( T2 \)

- \( \text{state}=\text{N} \)
- \( \text{old_token}=\text{token} \)
- \( RS_i = \{\text{id’s of all processes which are in} \)
- \( \text{token.queue} \) \&\& \( \text{will work as captain in future} \)

- \( P_j \) at the front of \( \text{token.queue} \) is selected as captain
- Send \( \text{token}(\text{token.queue}, \text{token.type}, \text{token.followers}, \text{token.session}) \) to \( P_j \)

Event 5: \( P_i \) receives complete \((j)\)

If \((j \text{ is in follower})\)

- \( \text{-- token followers} \)
- Remove \( j \) from \( \text{follower}_i \)
- If \( \text{follower}_i \)
  - Close timer \( T2 \)
  - If \( \text{token.followers}=0 \) \&\& (\( \text{state}=\text{HS} \))
    - If \( \text{token.queue}=0 \) \( \text{state}=\text{HI} \)

Else

- If \((j’s \text{ request in} \text{token.queue}) \text{state}=\text{R} \)
- Else \( \text{state}=\text{N} \)
- \( RS_i = \{\text{id’s of all processes which} \)
- \( \text{are in} \text{token.queue} \) \&\& \( \text{will work as} \)
- \( \text{captain in future} \)

- \( P_j \) at \( \text{front of} \text{token.queue} \) is selected as captain

- \( \text{old_token}=\text{token} \)
- Send \( \text{token}(\text{token.queue}, \text{token.type}, \text{token.followers}, \text{token.session}) \) to \( P_j \)

Event 6: \( P_i \) receives token

If \( \text{(\text{old_token}.session)}<\text{\text{token}.session} \) \(/\!*\!\text{otherwise invalid}*/\)

If \((TGI=\text{true}) \text{TGI=\text{false}}\)

Close timer \( T1 \)

- \( \text{delete}(\text{token.queue}) \) \(/\!*\!\text{delete} P_i \) \&\& \( \text{its followers} \)
  - if \( \text{token.type}=X \) \(/\!*\!X \text{is the type of deleted entry}*/\)
  - \( \text{token.followers}=\text{number of followers of} P_i \)
  - \( \text{Add all followers of} P_i \) \( \to \text{follower}_i \)
  - Send start \((j)\) to \( \text{followers of} P_i \)
  - \( \text{state}=\text{EC}; \text{enter CS}; \text{RS}_i=\emptyset \)

Event 7: Timer \( T1 \) at \( P_i \) exceeds the value \( T_{\text{req}} \)

Reset timer \( T1 \)

- \( TGI=\text{true} \)
- Send \( \text{gen_token}(i, \text{X}, \text{SN}[i], \text{old_token}.session) \) to all sites

Event 8: \( P_i \) receives \( \text{gen_token}(j, \text{X}, \text{SN}, \text{session}) \)

If \( \text{(SN)}<\text{SN}[j] \)

- \( \text{SN}[j]=\text{SN} \)
- \( \text{If}(\text{state}=\text{N/R}) \)
  - If \((j \notin RS_j \)) Add \( j \) to \( RS_j \)
  - \( \text{If}(\text{state}=\text{R}) \) Send \( f’s \text{ request message} \) to \( P_j \)
  - \( \text{If}(\text{session}<\text{old_token}.session) \)
    - \( P_i \) process at the front of \( \text{old_token.queue} \)
    - \( \text{Send token}(\text{token.queue}, \text{token.type}, \text{token.followers}, \text{token.session}) \) to \( P_i \)
  - Else \( \text{If}(\text{state}=\text{EC}) \)
    - \( \text{If}(\text{token.type}=X) \)
      - \( \text{Reset timer} T2 \)
      - \( \text{Send start}(i) \) to \( P_j \)
      - \( \text{If}(j \text{ not in follower}) \)
        - \( ++\text{token.followers} \)
        - Add \( j \) to \( \text{follower}_i \)
Else Add request \((j,SN,X)\) to token.queue
Else If \((state=HF)\)
Add \(j\) to RS,
Add request \((j,SN,X)\) to old_token.queue
old_token=token
Send token \((token.queue, token.type, token.followers, token.session)\) to \(P_f\)
Else If \((state=HS)\)
If \((token.type=X) \&\& (token.queue=\emptyset)\)
Reset timer \(T_2\);
Send \(start(i)\) to \(P_i\)
If \((j \notin token.followers)\)
Add \(j\) to follower,
++token.followers
Else Add request \((j,SN,X)\) to token.queue

Event 9: Timer \(T_2\) exceeds value \(2*tm+tc\) at \(P_i\)
Send is_complete \((i,X)\) to all processes in follower,

Event 10: \(P_i\) receives is_complete \((j,X)\)
If \(P_i\) is requesting for session \(X\)
If \(TGI_i=\text{True} \&\& TGI_j=\text{False}\)
Close timer \(T_1\);
captain=j
state=EF; enter CS
If \((state \neq EF)\) send complete \((i)\) to \(P_j\)

REFERENCES