C-V Characterization and Analysis of Temperature and Channel Thickness Effects on Threshold Voltage of Ultra-thin SOI MOSFET by Self-Consistent Model

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Abstract—The threshold voltage and capacitance voltage characteristics of ultra-thin Silicon-on-Insulator MOSFETs are greatly influenced by the thickness and doping concentration of the silicon film. In this work, the capacitance voltage characteristics and threshold voltage of the device have been analyzed with quantum mechanical effects using the Self-Consistent model. Reduction of channel thickness and adding doping impurities cause an increase in the threshold voltage. Moreover, the temperature effects cause a significant amount of threshold voltage shift. The temperature dependence of threshold voltage has also been observed with Self-Consistent approach which are well supported from experimental performance of practical devices.

Keywords—C-V characteristics, Self-Consistent Analysis, Silicon-on-Insulator, Ultra-thin film.

I. INTRODUCTION

In nanotechnology and microelectronics where low power consumption and high speed are desired, devices with nano and submicron dimensions are essential. Silicon-on-insulator (SOI) technology is an attractive choice for these applications. In recent years, SOI MOS devices have received great attention due to their advantages over conventional bulk MOSFETs [1]–[4] such as: lower parasitic capacitance, improved subthreshold characteristics and reduced short-channel effects. So to gain insight into the physics of the device and evaluate their performance, an accurate model of the device parameters is essential. The threshold voltage ($V_{th}$) and Capacitance-Voltage (C-V) characteristics are important features for characterization of the performance of SOI MOSFETs. However, these characteristics are dependent on a wide range of parameters such as: thickness of the channel, front and buried oxide thickness, channel and substrate doping, temperature etc. As device dimensions are scaling down, quantum mechanical effects have become significant specially for SOI with ultrathin channel [1], [4]. A SOI MOSFET having nearly or below 40nm gate length and 20nm of top silicon layer thickness can be referred to as ultra-thin film device [5]. The classical analysis of ($V_{th}$) of SOI can not be applied in such a thin region of silicon film thickness ($t_{si}$) for $t_{si} < 10$ nm [6]. So quantum mechanical study is of great importance for analyzing behavior of nano scale SOI MOSFETs.

Besides, in ultrathin channel devices, the threshold voltage is influenced by operating temperature of the environment. The temperature dependence of $V_{th}$ of accumulation-mode SOI devices has been reported in literature [7], [8] where a semi-classical and quantum mechanical analysis have been performed in [2].

The main contribution of this work is to analyze $V_{th}$ of SOI MOSFETs in an efficient way. Towards this goal, the analysis utilizes the Self-Consistent solver as a newer variant to study the effect of operating temperature on the threshold voltage. Along the way, the effect of doping and channel thickness on $V_{th}$ and C-V characteristics have been studied, which also have independent significance. Self-consistent analysis has been widely used in literature for the analysis of nanoscale bulk MOSFETs [9]–[11]. However, its application for SOI MOSFETs can also provide efficient results as observed from this work. The simulated results with Self-Consistent solver have been compared to experimental device performances and with the results of [2]. The model of [2] produced large deviation with experimental results when $t_{si}$ was increased from 6 nm to 10 nm. But the proposed approach predicted a good agreement with the experimental results compared to the simulated results of [2] irrespective of film thickness. Moreover, C-V characterization is also well established mean for characterizing the strong inversion condition i.e. the $V_{th}$ of SOI devices [12]–[14]. Hence, C-V characteristics have been analyzed with Self-Consistent model to validate the effectiveness of the approach.

II. ANALYSIS TECHNIQUE: SOI CHARACTERIZATION

A. SOI Structure and Analysis Assumptions

In this paper, the SOI MOSFET on $<100>$ Si surface shown in Fig. 1(a) has been considered. Three interface regions can be identified in the structure such as: gate oxide-silicon film interface, Silicon-film-buried oxide interface (BOX) and the interface of buried oxide and silicon substrate. The buried oxide is thicker compared to other layers. The channel silicon film is ultra-thin with thickness $t_{si}$ ≤ 10 nm For both the film and substrate, p-type doping is considered. For the thin dimension, the silicon film approaches complete depletion and hence, it works as Fully depleted device [14].
from Poisson’s equation as, 

\[ V \text{ density respectively, } E \]

Energy band diagram at inversion 

Poisson and Schrödinger’s equation. For the MOSFET, the Schrödinger’s equation (1) is used to estimate the new depletion charge density \( \rho_{\text{dep}} \) and \( \rho_{\text{inv}} \) respectively. A potential profile is obtained from Poisson solver using equation (1). This potential profile is used to generate an energy band profile for the Schrödinger’s solver. Then the inversion carrier concentration is calculated using the eigen energy values obtained as a solution of the one dimensional Schrödinger’s solution. The inversion carrier concentration is estimated according to the following expression [15]: 

\[ n_{\text{inv}} = \sum_{ij} n_{ij} |\psi_{ij}(x)|^2 \]  

where \( n_{ij} \) is total inversion carrier concentration, \( n_{ij} \) is carrier concentration in the \( j \)th subband of the \( i \)th valley, \( E_{ij} \) is the corresponding eigen energy, \( E_F \) is the Fermi energy, \( n_{vi} \) is valley degeneracy and \( m_{di} \) is density-of-states effective mass in \( i \)th valley. The energy eigen \( E_{ij} \) is obtained solving the one dimensional Schrödinger’s equation,

\[-\frac{\hbar^2}{2m^*} \frac{d^2}{dx^2} + qV(x) \psi_{ij}(x) = E_{ij} \psi_{ij}(x) \]  

where \( \psi_{ij}(x) \) is the corresponding wavefunction of \( E_{ij} \). \( V(x) \) is the potential obtained from (1) and \( m^* \) is the effective mass. For \(<100> \) oriented silicon surfaces, quantization effective masses are 0.916\( m_o \) for longitudinal valley and 0.19\( m_o \) for transverse valley (\( m_o \) is rest mass of electron), \( n_{vi} = 2 \) and \( n_{vi} = 4 \) for longitudinal and transverse valleys respectively. The density-of-states effective mass \( m_{di} \) is 0.19\( m_o \) for longitudinal valley and 0.417\( m_o \) for transverse valley. For holes, the effect of heavy hole and light holes are more significant than the split-off holes and are taken into account for evaluating hole quantization. The quantization effective masses of light and heavy holes are 0.20\( m_o \) and 0.29\( m_o \) respectively. The density-of-states effective mass \( m_{di} \) is 0.169\( m_o \) for light holes and 0.43\( m_o \) for heavy holes. For both heavy holes and light holes \( n_{vi} = 1 \). Effective mass in oxide is considered to be 0.4\( m_o \).

C. Numerical Analysis

The depletion width \( x_d \) is updated while solving the Poisson’s equation (1) that is used to estimate the new depletion charge density \( \rho_{\text{dep}} \). As a new inversion charge density \( \rho_{\text{inv}} \) is obtained from Schrödinger’s solution, these two updated charge density are substituted in (1) to solve Poisson’s and Schrödinger’s equations (1 and 5) iteratively until two successive solution produce result within the given convergence limit.
For solution of Schrödinger’s equation in the \( n \)-th iteration, the updated potential profile is given by,

\[
V_n = V_{n-1} + f(V_p - V_{n-1}) \tag{6}
\]

where \( V \) denotes potential and \( n \) is the index of iteration. \( V_p \) is the solution from the Poisson’s equation using the updated charge densities and \( f \) is the relaxation factor to control the speed of convergence. Extensive simulation has been carried out and the best performance for the proposed method has been obtained with \( f = 0.05 \).

Here, \( V_{th} \) has been defined as the gate voltage at which carrier concentration per unit area, \( N_{inv} \), reaches a value \( N_{th} = 2 \times 10^{14} \text{cm}^{-2} \), adequate to achieve the device turn on condition (Fig. 2). \( N_{inv} \) is obtained by integrating \( n_{inv} \) over the total device thickness, \( t_{total} \) i.e.

\[
N_{inv} = \int_{t_{total}} n_{inv} dx \tag{7}
\]

where, \( t_{total} = t_{ox f} + t_{si} + t_{ox b} + t_{sub} \) (Fig. 1b).

### III. ANALYSIS OF THRESHOLD VOLTAGE

In fully depleted (FD) SOI, the body is thinner than channel depletion width and body voltage effect on \( V_{th} \) can be neglected [16]. So the dependence of \( V_{th} \) on some other factors such as-silicon film thickness, channel doping and operating temperature have been analyzed in this paper to observe their quantum mechanical effects on \( V_{th} \).

#### A. Effect of Doping and Energy Quantization

In ultrathin body devices, channel doping concentration has significant effect on controlling the threshold voltage. In the absence of channel dopants, impurity scattering effect is minimized and depletion charge can not exist in the channel [17]. So band bending is negligible and the potential well is almost of rectangular shape. Hence, the undoped ultrathin-film device will behave mostly like intrinsic and the 1-D Poisson’s equation yields a linear potential distribution across the channel. Since \( \rho_{dep} = 0 \) for undoped channels (from (1)), there is less charge density and hence, there occurs a smaller electric field compared to heavily-doped channel devices in the inversion region. The small electric field results in a lowering of the ground state energy and reduced carrier confinement [17]. This effectively causes a lower \( V_{th} \) for undoped SOI devices than the heavily doped ones. Fig. 2 shows the effect of doping on \( V_{th} \) for SOI structure considering all other parameters same. The device has the following dimension: front oxide thickness \( t_{ox f} = 5 \text{nm} \), buried oxide thickness \( t_{ox b} = 40 \text{nm} \) and acceptor doping level \( N_a = 10^{17} \text{cm}^{-3} \) for doped structure. For similar device structure, the doped SOI shows higher threshold voltage \( V_{th} \) compared to the undoped one.

Table I shows the effect of doping concentration on \( V_{th} \) with four values of \( N_a \). It reveals that \( V_{th} \) increases as \( N_a \) is increased.

![Graph showing the effect of channel thickness on V_th](image)

**Fig. 2:** Effect of channel doping on threshold voltage (a) for undoped film (b) for doped film with doping concentration \( N_a = 10^{17} \text{cm}^{-3} \)

<table>
<thead>
<tr>
<th>Si thickness ( t_{si} ) (nm)</th>
<th>Doping Concentration ( N_a ) (cm(^{-3}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>( 10^{16} ) ( 5 \times 10^{16} ) ( 10^{17} ) ( 5 \times 10^{17} )</td>
</tr>
<tr>
<td>1</td>
<td>1.1996 1.2448 1.2621 1.3198</td>
</tr>
</tbody>
</table>

**TABLE I:** Values of \( V_{th} \) for different doping concentrations

#### B. Effect of Channel Thickness

\( V_{th} \) depends greatly on Si film thickness for SOI MOSFETs. The \( V_{th} \) increases as \( t_{si} \) is reduced. With decreasing \( t_{si} \), the distance between ground state energy and conduction band \( E_c \) becomes larger. So the carriers have to go in higher energy sub-band. The Fermi level \( (E_F) \) also moves towards ground state energy. These results in a higher \( V_{th} \) [6]. This has been realized for both doped and undoped SOI.
IV. TEMPERATURE DEPENDENCE ON THE THRESHOLD VOLTAGE

$V_{th}$ is sensitive to operating temperature. The Fermi energy level in the SOI layer remains below the ground state energy about $kT/q$ at the threshold condition [2] and hence affects $V_{th}$. The dependence of $V_{th}$ with respect to temperature can be expressed from the following equation [1]:

$$\frac{dV_{th}}{dT} = \frac{d\phi_F}{dT} = \frac{q}{kT \ln (N_a/n_i)} \left[ 1 + \frac{\epsilon_{si}}{C_{ox}} \ln \frac{N_a}{n_i} \right]$$

(8)

where $\epsilon_{si}$ is dielectric constant of Si, $N_a$ is acceptor doping concentration, $C_{ox}$ is oxide capacitance, $k$ is Boltzman’s constant, $n_i$ is intrinsic carrier concentration and $\phi_F$ is potential difference between the Fermi level ($E_F$) and intrinsic level ($E_{Fi}$) expressed as [18]:

$$E_{Fi} - E_F = kT \ln \frac{N_a}{n_i}$$

(9)

From (8), the inverse relationship with temperature and threshold voltage dominates to increase threshold voltage with decreasing temperature. The temperature dependence of $V_{th}$ has been evaluated for a wide range of temperatures. In the Self-Consistent analysis, temperature effects have been incorporated in the calculation of Fermi level, silicon bandgap and intrinsic carrier concentration. The temperature effect on the Fermi level has been analyzed using (9) where $E_{Fi}$ has been considered at the center of the bandgap of silicon. However, silicon bandgap decreases with temperature according to the following equation [18]:

$$E_g(T) = E_g(0) - \frac{\alpha T^2}{\beta + T}$$

(10)

where $E_g(T)$ and $E_g(0)$ refer to the bandgap of silicon at the operating temperature T and 0 K respectively. The parameters $\alpha$ and $\beta$ have been obtained for silicon as $4.9 \times 10^{-4}$ ev/K and 655 K respectively [18].

The simulation has been performed in the range from 150 K to 300 K where Boltzman’s approximation is clearly valid [19]. The intrinsic carrier concentration at different temperatures has been evaluated utilizing the Fermi-Dirac Integral [19]. Fig. 3 shows the $V_{th}$ shift with temperature. The threshold shift has been plotted for $V_{th}(T) - V_{th}(300K)$. The temperature dependence from the simulation results has been compared with experimental results from [2] and also with the simulation results from [2]. For experimental devices, the dimension was as follows- front oxide thickness $t_{oxf} = 3$ nm or 5 nm, silicon film thickness $t_{si} = 6$ nm or 10 nm, buried oxide thickness $t_{box} = 110$ nm and doping concentration $N_a = 10^{16}$cm$^{-3}$. Fig. 3 shows that the simulated curves of $V_{th}$ shift with temperature using Self-Consistent model follow more closely the experimental data compared to the simulated results from [2]. The model of [2] although predicted near to experimental results [2] for $t_{si} = 6$ nm, showed large deviation when $t_{si}$ is increased to 10nm. Hence, it performs poorly as the film thickness is raised. The proposed Self-Consistent analysis, on the other hand, has performed with good agreement with experimental result for both film thicknesses. Actually, the Self-Consistent approach performs quantum mechanical analysis with 1Å$^3$ grid size and convergence error has been maintained as 0.001 which have increased its accuracy. However, the presence of interface states might have increased the $V_{th}$ shift for experimental device beyond the simulation results. Also the temperature effect on poly-Si gate electrode work function $\phi_{ms}$ has not been considered. These might have been the cause of discrepancies with the experimental result [2].

V. ANALYSIS OF C-V CHARACTERISTICS

SOI C-V analysis is more complicated due to presence of two oxide-semiconductor interfaces compared to conventional
bulk MOSFETs. The total capacitance is the combination of the oxide and film capacitances, expressed as [12], [14]:

\[
C_{oxf} = \frac{\epsilon_{oxf}}{t_{oxf}} \\
C_{oxb} = \frac{\epsilon_{oxb}}{t_{oxb}} \\
C_{gs} = \frac{dQ_{film}}{dV_{gs}} \\
C_{sb} = \frac{dQ_{sub}}{dV_{sb}}
\]

(11) (12) (13) (14)

where \( \epsilon_{oxf} \) and \( \epsilon_{oxb} \) are permittivity of front and buried oxide and \( t_{oxf} \) and \( t_{oxb} \) are the respective oxide thickness. \( C_{gs} \) is per unit area capacitance in the film for gate voltage and \( C_{sb} \) is capacitance between film and substrate. \( V'_{gs} \) and \( V_{sb} \) are the gate voltage and and film to substrate voltage and \( Q_{film} \) and \( Q_{sub} \) are the corresponding charges of film and substrate. Throughout the analysis carried out here, the voltage at the end of substrate has been taken as reference (0V). Moreover, the SOI device considered here has thick buried oxide layer, so there is few probability of confinement of inversion carriers in the substrate. So the effect of \( C_{sb} \) is negligible. The gate and buried oxide capacitances \( C_{oxf} \) and \( C_{oxb} \) are constant. So the only significant voltage dependent capacitance is \( C_{gs} \).

The capacitance \( C_{gs} \) Vs \( V_{gs} \) characteristic has been shown in the Fig. 4 for both doped and undoped structure. So this capacitance can be evaluated in the following way [14]:

\[
C_{gs} = \int_{film} \frac{\partial \rho(x)}{\partial V_{gs}} dx
\]

(15)

where \( \rho(x) \) is the space charge distribution in the film. For intrinsic film, the space charge distribution \( \rho(x) \) is the contribution of \( \rho_{inv} \) alone where for doped film, \( \rho(x) \) is obtained from, \( \rho_{dep} \) and \( \rho_{inv} \) respectively. Strong inversion condition occurs when the C-V curves start to rise. Note that increasing the film thickness causes reduction of the strong inversion voltage for both doped and undoped film. Thus the C-V characteristics further substantiate the \( V_{th} \) dependence on silicon film thickness showing increasing thickness provides achieving faster inversion condition.

VI. CONCLUSION

The C-V characteristics and threshold voltage dependence on various factors have been observed in this work using the Self-Consistency model for ideal cases. The simulated results showed threshold voltage decreased with temperature although the shifted threshold values had some deviation from experimental results for non-idealities. However, nonideal effects can be easily incorporated in the model such as: fixed charges, trapped charges in oxides and non-zero semiconductor-metal or poly-Silicon barrier heights. Fixed charges and the metal-semiconductor barrier height do not depend on gate voltage and hence, they only lead to a shift of threshold voltage which can be included in the flat band voltage \( V_{FB} \). As verified by the experimental results, this work will enhance the field of research of numerical analysis of device characterization by Self-Consistent Model.

REFERENCES


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