Abstract—In this paper a three dimensional thermal model of a sliding contact system is proposed for both steady-state or transient conditions. The influence of contact force, electric current and ambient temperature on the temperature distribution, has been investigated. A thermal analysis of the different type of the graphite material of fixed electric contact and its influence on contact system temperature rise, has been performed. To validate the three dimensional thermal model, some experimental tests have been done. There is a good correlation between experimental and simulation results.

Keywords—Sliding electric contact, temperature distribution, thermal analysis.

I. INTRODUCTION

SLIDING electrical contacts are found in many electromechanical devices, such as relays, switches, current-collection brushes in electrical machines and in special applications, such as pantograph-catenary system or electromagnetic rail launcher. Sliding electrical contacts involve complex phenomenon and their understanding needs large researches to estimate the thermal aspects, the contact resistance, the wear or the material transfer. Temperature rise due to the friction and electrical current may be a major source of sliding electrical contacts deterioration. The contact resistance is largely studied [1], including thermal analysis as in [2]-[5]. Model for temperature estimation of de-contactors are well developed, as in [6]. The current distribution and thermal effects of the sliding contact arrangement used in high voltage circuit breaker are also studied [7]. It is considered the influence of different factors, such as the size of the contacts and conductors, the structure and resistance of the sliding contact arrangement, the current and temperature distribution and it offers several optimizing measures. Thermal aspects are very important for the sliding contact with lubricants [8], because calculating the contact temperatures between the contacting surfaces makes possible to estimate lubricant degradation and thermal surface failure. It also noticed that for low sliding velocities it can be used the steady state estimation, but for higher sliding velocities there are necessary other methods to estimate the thermal aspects. Specific for the sliding contacts is the difficulty to estimate the temperature variation in the moving contact (because at least one of the contacts is moving). A wireless temperature monitoring with miniature temperature sensors in correlation with the load current provides the means to evaluate physical condition of electrical contacts and detect abnormality and prevent possible disruption of electrical service, [9]. Other thermal measurements possibility is presented in [10], which found the best measurement location as downstream of the nominal contact zone in the moving body. A special area application with sliding electrical contacts is the contact between the pantograph strip and the contact line for the electric vehicles as tramways or electric locomotives, supplied from a pantograph-catenary system, where the contact is realized between two different materials. Mathematical models and simulations for the sliding contact between the pantograph and the contact line are well developed for electrical and mechanical aspects [11], but less with thermal aspects [12]. The sliding electrical contact of pantograph-catenary system in correspondence with the contact force and the electric current is studied in order to estimate the contact resistance [13] and also the damages of the pantograph-catenary system due to the electrical faults in real conditions [14]. The temperature range over the pantograph-catenary system is also studied, as in [15]. Another special application, the electromagnetic launcher, is a short operating time at high currents, pressures and temperatures and the phenomenon occurring at the interface between conductors involved in sliding contacts have been investigated by the introduction of an auxiliary electric network [16]. The control of the interface tribology in sliding electrical contacts requires an understanding of the Joule heating in the vicinity of the interface. In some situations [17], the maximum temperature rise occurs in the bulk of the contacts rather than at the interface and sliding can have a significant effect on the temperature field even for low speed.

This study attempts to achieve and validate a three dimensional thermal model for a sliding contact system with different geometries of fixed and moving contact.

II. THERMAL MODEL

The aim of this study is to develop a three dimensional thermal model of a sliding electric contact system. The basic equation of heat transfer has the following expression for each volume element dV:

\[ Q_r = Q_t - Q_f + Q_a \]  

(1)

The left term of the equation is the heating power from the current flow, \( Q_t \). It is in balance with the heat stored by temporal change of temperature \( Q_o \), the power removed from the element by thermal conduction \( Q_f \), and the thermal power dissipated to the surrounding area by the surface convection,
For the above thermal power quantities, the following equations can be written:

\[
\begin{align*}
Q_c &= \iiint \rho j^2 \, dV; \\
Q_t &= \iiint \kappa \frac{\partial \theta}{\partial t} \, dV; \\
Q_e &= \iiint \lambda \cdot \text{grad} \theta \, dV; \\
Q_a &= \iiint k \frac{l}{S} (\theta - \theta_a) \, dV
\end{align*}
\]

where:
- \(\rho\) means the electrical resistivity;
- \(j\) – current density;
- \(\gamma\) – material density;
- \(c\) – specific heat;
- \(\lambda\) – thermal conductivity;
- \(\theta\) – temperature;
- \(\theta_a\) – ambient temperature;
- \(k\) - convection coefficient;
- \(l\) – perimeter length of the contacts’ cross-section;
- \(S\) – cross-section of the contacts.

Therefore,

\[
\begin{align*}
\iiint \rho j^2 \, dV &= \iiint \kappa \frac{\partial \theta}{\partial t} \, dV - \iiint \lambda \cdot \text{grad} \theta \, dV + \\
&+ \iiint k \frac{l}{S} (\theta - \theta_a) \, dV
\end{align*}
\]

The material density, specific heat and thermal conductivity do not have an important temperature variation; thus they can be regarded as constants. On the other hand, the electrical resistivity has a significant temperature variation and can be estimated through a parabolic variation or a linear one. In general, the difference between these two types of variation is not so important. For the electrical resistivity we may consider a linear variation with the temperature,

\[
\rho = \rho_0 [1 + \alpha (\theta - \theta_a)]
\]

where \(\alpha\) is the coefficient of electrical resistivity variation with temperature. Considering the notation:

\[
\vartheta = \theta - \theta_a
\]

The following relation is obtained:

\[
\begin{align*}
\iiint \rho_0 (1 + \alpha \vartheta) \frac{1}{S^2} \, dV &= \iiint \kappa \frac{\partial \vartheta}{\partial t} \, dV - \\
&- \iiint \lambda \cdot \text{grad} \vartheta \, dV + \iiint k \frac{l}{S} \vartheta \, dV
\end{align*}
\]

Because the sliding electric contact system has not a constant cross section and the physical parameters, especially the electrical resistivity, vary with the temperature, the above equation is a non-linear type with variable coefficients and it demands a numerical procedure to evaluate the temperature distribution. It is desirable to restate the problem by considering various forms of discretization. The discretised form of the problem only requires the solution to be satisfied at a finite number of points in the region; and in the remainder of the region, appropriate interpolations may be used. Thus, this case is reduced to an algebraic form involving only the basic arithmetic operations, which could in turn be solved by numerical methods. These methods have become very accurate and reliable for solving initial and boundary value problems. The basic idea of the finite element method is to discretise the main domain into several subdomains, or finite elements. These elements can be irregular and possess different properties so that they form a basis to discretise complex structures, or structures with mixed material properties.

A three dimensional model for a sliding electric contact system has been developed using specific software like Pro-ENGINEER, which is an parametric, integrated 3D CAD/CAM/CAE solution. Pro-ENGINEER provides a complete set of design, analysis and manufacturing capabilities on one, integral, scalable platform. These required capabilities include solid modelling, surfacing, rendering, data interoperability, routed systems design, simulation, tolerance analysis and tooling design.

An overall view with electric installation including the sliding contact system which has the possibility to use two graphite skate contacts is presented in Fig. 1. The 3D model had taken into consideration all the component parts of the sliding contact system: copper disc, steel pressing piece, gear wheel, main shaft, insulators, graphite skate, spindles, as shown in Fig. 2.
III. THERMAL SIMULATIONS

The Pro-MECHANICA software has been used for all thermal simulations. Pro-MECHANICA uses adaptive p-element technology whereas conventional finite element codes use non-adaptive h-element technology.

The underlying geometry can be followed more precisely. The elements use a polynomial equation to describe the stress shape function, which can vary from 3rd to 9th order. This means that fewer elements are required and they can follow high stress gradients very closely. It also means that an automatic convergence strategy can be employed, whereby the polynomial order of the elements is increased rather than having to re-mesh with smaller elements. Furthermore Pro-MECHANICA has built-in optimisation capabilities, so that designs can be optimised efficiently and automatically.

The material properties of every component part of the sliding contact system, are described in the Table 1, according to Fig. 2. The heat load has been applied on the contact area between copper disc and graphite skate contact. There is a uniform spatial distribution on these elements. The mesh of this 3D sliding contact thermal model has been done using tetrahedron solids element types with the following allowable angle limits (degrees): maximum edge: 170; minimum edge: 5; maximum face: 174.3; minimum face: 5. The maximum aspect ratio was 23.45 and the maximum edge turn (degrees): 95.

The single pass adaptive convergence method to solve the thermal steady-state simulation has been used.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Copper (1)</th>
<th>Iron FE40 (2, 3, 4, 7)</th>
<th>Graphite (6)</th>
<th>Insulation material/textolit (5, 8)</th>
</tr>
</thead>
<tbody>
<tr>
<td>γ (kg/m³)</td>
<td>8900</td>
<td>7190</td>
<td>1900</td>
<td>1350</td>
</tr>
<tr>
<td>c (J/kg°C)</td>
<td>385</td>
<td>420.27</td>
<td>1000</td>
<td>733</td>
</tr>
<tr>
<td>λ (W/m°C)</td>
<td>385</td>
<td>52.028</td>
<td>160</td>
<td>3.2</td>
</tr>
</tbody>
</table>

Fig. 2 Thermal model of the copper disc – graphite skate power assembly (1 – copper disc; 2 – steel pressing piece; 3 – gear wheel; 4 – main shaft; 5 – end insulators; 6 – graphite skate; 7 – spindles; 8 - insulators)

The analyzed graphite contact has the following overall dimensions: 400mm long, 18mm wide, 22 mm high. The copper disc has the diameter of 380mm and the thickness about 5mm. The ambient temperature was about 23°C. From experimental tests it was computed the convection coefficient $k = 15.3\text{W/m}^2\text{°C}$ on the graphite contact. For all metal component parts of the sliding contact system, the convection coefficient was about 19.5W/m²°C.

Fig. 3 Temperature distribution on the sliding contact system at current value of 8A and contact force of 10N
It was considered the convection condition like boundary condition for the outer boundaries such as copper disc, steel pressing piece, gear wheel, main shaft, spindles and it has been applied on surfaces with an uniform spatial variation and a bulk temperature of 23ºC. On the insulators, the convection coefficient was about 12W/m²ºC.

Further on, some steady state thermal simulations have been done. The temperature distribution on the sliding contact system is presented in Fig. 3. In Fig. 4 is shown the temperature distribution at a half cross-section through whole copper disc and the rest of the mechanical system. It is to observe the highest temperatures on the contact area between the copper disc and the graphite skate contact.

The copper disc and graphite contact lengthwise temperature distributions for different electric current and contact force value, are presented from Fig. 5 to Fig. 8. Temperature distribution along the radius of the copper disc and length of the graphite contact for different graphite materials and ambient temperature is shown from Fig. 9 to Fig. 12.

**IV. DISCUSSION OF THE RESULTS**

In Fig. 5, the temperature distribution along the radius of the copper disc for different values of the test current (4, 8 and 12A), is shown. The contact force has been maintained at the constant value of 10N.

As expected, the higher values of the temperature (θsim_12A) correspond to the higher values of the test current (12A). There is a temperature decreasing as we depart the contact area (x = 0). The temperature decreasing is more pronounced at higher test currents (θsim_12A) than lower current values (θsim_4A). A similar temperature variation lengthwise graphite skate contact, is shown in Fig. 6. The contact force was the same 10N. Also in this case, there is a noticeable decrease in temperature as we depart the contact area (x = 0). After approximately 100mm, the temperature values are almost constant. As expected, at higher current values (12A) there are higher temperature values (θsim_12A). The temperature variation along the radius of the copper disc for different values of the contact force (6, 10 and 15N), is presented in Fig. 7. The electric current had the constant value of 8A. In this case, at lower values of the contact force (6N) there are higher temperatures (θsim_6N). When the contact force has higher values (15N), the temperatures are lower (θsim_15N). This is explained by the fact that a higher contact force, the contact resistance is lower and so, the power loss is lower and finally, the local temperatures are lower. The same temperature distribution lengthwise graphite skate contact, is presented in Fig. 8. It can be noticed that the temperature variation at the same contact force, is insignificant after a distance about 100mm from the contact area.
Fig. 6 Temperature variation lengthwise graphite skate contact for different current values (4, 8 and 12A) and the contact force of 10N. Comparison between simulation values ($\theta_{\text{sim}_4A}$, $\theta_{\text{sim}_8A}$ and $\theta_{\text{sim}_12A}$) and experimental results ($\theta_{\text{exp}_4A}$, $\theta_{\text{exp}_8A}$ and $\theta_{\text{exp}_12A}$)

Fig. 7 Temperature variation along the radius of the copper disc for different contact forces (6, 10 and 15N) and the current of 8A. Comparison between simulation values ($\theta_{\text{sim}_6N}$, $\theta_{\text{sim}_10N}$ and $\theta_{\text{sim}_15N}$) and experimental results ($\theta_{\text{exp}_6N}$, $\theta_{\text{exp}_10N}$ and $\theta_{\text{exp}_15N}$)

Fig. 8 Temperature variation lengthwise graphite skate contact for different contact forces (6, 10 and 15N) and the current of 8A. Comparison between simulation values ($\theta_{\text{sim}_6N}$, $\theta_{\text{sim}_10N}$ and $\theta_{\text{sim}_15N}$) and experimental results ($\theta_{\text{exp}_6N}$, $\theta_{\text{exp}_10N}$ and $\theta_{\text{exp}_15N}$)
Fig. 9 Temperature variation along the radius of the copper disc for different graphite thermal conductivity values (55, 160 and 340W/m°C) at the current value of 8A and the contact force of 10N. Comparison between simulation values ($\theta_{\text{sim}}_{55}$, $\theta_{\text{sim}}_{160}$ and $\theta_{\text{sim}}_{340}$) and experimental results ($\theta_{\text{exp}}_{55}$, $\theta_{\text{exp}}_{160}$ and $\theta_{\text{exp}}_{340}$)

Fig. 10 Temperature variation lengthwise graphite skate contact for different graphite thermal conductivity values (55, 160 and 340W/m°C) at the current value of 8A and the contact force of 10N. Comparison between simulation values ($\theta_{\text{sim}}_{55}$, $\theta_{\text{sim}}_{160}$ and $\theta_{\text{sim}}_{340}$) and experimental results ($\theta_{\text{exp}}_{55}$, $\theta_{\text{exp}}_{160}$ and $\theta_{\text{exp}}_{340}$)

Fig. 11 Temperature variation along the radius of the copper disc for different ambient temperature values (10, 23 and 35°C) at the current value of 8A and the contact force of 10N
In Fig. 9, the temperature variation along the radius of the copper disc for different graphite materials with different thermal conductivity values is presented. The thermal simulations have been performed for a constant current of 8A and a constant contact force of 10N. It has been considered three types of the graphite materials: BGR-3, \( \lambda = 55\,\text{W/m}^\circ\text{C} \); EGR-16, \( \lambda = 160\,\text{W/m}^\circ\text{C} \) and MGR-34, \( \lambda = 340\,\text{W/m}^\circ\text{C} \). It can be observed very small differences between temperature variations (\( \theta_{\text{sim}, 55} \), \( \theta_{\text{sim}, 160} \) and \( \theta_{\text{sim}, 340} \)). The same case has been analyzed but with the temperature distribution lengthwise the graphite skate contact, Fig. 10. It can be noticed that for the graphite material with higher thermal conductivity (\( \theta_{\text{sim}, 340} \)), the temperature decreasing is relatively small (under 2\(^\circ\text{C}\)); but for the graphite material with lower thermal conductivity (\( \theta_{\text{sim}, 55} \)), the temperature decreasing is about 6\(^\circ\text{C}\).

The temperature variation along the radius of the copper disc for different ambient temperatures (10, 23 and 35\(^\circ\text{C}\)), is depicted in Fig. 11. The test current and the contact force have been maintained at a constant value. It is to observe that the temperature variation curve is translated on vertical direction depending on the temperature ambient values. The same observation is valid in the case of temperature variation lengthwise the graphite skate contact, Fig. 12, for the same different values of the ambient temperatures (\( \theta_{10} \), \( \theta_{23} \) and \( \theta_{35} \)). The test current has been considered at the constant value of 8A and also the contact force was maintained at a constant value of 10N.

To validate the simulation results, some experimental tests have been made with the same conditions as in the case of thermal simulations. The electric circuit diagram used for experimental tests is shown in Fig. 13. The main switch K, enables the supply with low-voltage for the auto-transformer ATR, which adjusts the input voltage for the current supply device CS. The high current from CS, flows through the copper disc D and graphite skate contact S.

The current value is measured by an ammeter A, through a current transformer CT. The temperature values are recorded by a compact infrared thermal imaging camera type FLIR E40 with a focal plane array detector of 160 x 120 pixels infrared resolution, temperature range: -20\(^\circ\text{C}\) to 650\(^\circ\text{C}\) with \(\pm 2\%\) or 2\(^\circ\text{C}\) accuracy and 0.07\(^\circ\text{C}\) thermal sensitivity. In fig. 14 and 15, an example of the thermal spectra, in steady-state conditions, of the analyzed sliding contact system for the test current of 8A, contact force of 10N, thermal conductivity of the graphite about 160\,\text{W/m}^\circ\text{C} and ambient temperature of 23\(^\circ\text{C}\), are presented. The emissivity coefficient was about 0.95. The comparisons between simulation and experimental results are presented from Fig. 5 to Fig. 10. It can be noticed a good correlation between simulation results and experimental values. The differences between the temperature values resulting from experimental tests and those obtained during simulations are due to various factors: measurement errors, thermal model simplifications and mounting test conditions. Nevertheless, the maximum difference between the experimental and simulation results is less than 2.3\(^\circ\text{C}\).

V. CONCLUSION

The obtained three dimensional thermal models allow analysis of the thermal behaviour of sliding electric contact system. The thermal model provides the sliding contact system temperature distribution at different currents, contact forces, graphite materials and ambient temperature values and could be used as a designing tool for the electric sliding contact systems, especially in the case of electric traction vehicles as trams and trains. Some experimental tests have been made in order to validate the proposed three dimensional thermal model. There is a good correlation between experimental and simulated results. Using the proposed thermal model, the sliding contact design process can be improved and there is the possibility of obtaining new solutions for an optimal power management of different types of sliding contact systems.
This work was supported by CNCSIS – UEFISCDI, project number 610 PNII – CAPACITATI, 2013.

ACKNOWLEDGMENT

This work was supported by CNCSIS – UEFISCDI, project number 610 PNII – CAPACITATI, 2013.

REFERENCES


Adrian Pleșca was born in Iasi, Romania, on April 16, 1972. He graduated from the Gheorghe Asachi Technical University of Iasi and he received the PhD degree in Electrical Engineering in 2001. His employment experience included the Gheorghe Asachi Technical University of Iasi, Power Engineering Department. His special fields of interest included electrical apparatus, special equipment for power semiconductor devices protection and 3D modelling and simulation of the electrical apparatus. Dr. Pleșca received Golden and Silver Medals at World Exhibition of Invention, Research and Industrial Innovation, Brussels, Belgium, EUREKA, 2001, 2004, Special Prize awarded by National Research Council of Thailand for Fundamental Research at The First International Invention’s Day Convention, Bangkok, Thailand 2008, Gold Medal at 4th International Warsaw Invention Show 2010, Diploma and Genius Medal at 2nd International Invention Exhibition, Ljubljana, 2010 and Gold Prize at Seoul International Invention Fair, Korea 2011.