On Methodologies for Analysing Sickness Absence Data: An Insight into a New Method

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Abstract—Sickness absence represents a major economic and social issue. Analysis of sick leave data is a recurrent challenge for analysts because of the complexity of the data structure which is often time dependent, highly skewed and clumped at zero. Ignoring these features to make statistical inference is likely to be inefficient and misguided. Traditional approaches do not address these problems. In this study, we discuss model methodologies in terms of statistical techniques for addressing the difficulties with sick leave data. We also introduce and demonstrate a new method by performing a longitudinal assessment of long-term absenteeism using a large registration dataset as a working example available from the Helsinki Health Study for municipal employees from Finland during the period of 1990-1999. We present a comparative study on model selection and a critical analysis of the temporal trends, the occurrence and degree of long-term sickness absences among municipal employees. The strengths of this working example include the large sample size over a long follow-up period providing strong evidence in supporting of the new model. Our main goal is to propose a way to select an appropriate model and to introduce a new methodology for analysing sickness absence data as well as to demonstrate model applicability to complicated longitudinal data.

Keywords—Sickness absence, longitudinal data, methodologies, mix-distribution model.

I. INTRODUCTION

The increasing direct costs of work absences have challenged government's policymakers, public authorities, insurance companies and employers to find ways to reduce the heavy economic and social burdens. In Europe, sick leave policy is one of the top policy priorities [1]. The literature of sickness absence is increasing. Socio-economic, demographic, occupational status, and work-related and economic factors are important determinants of sickness absences [2]-[10].

Musculoskeletal and stress-related disorders cause a large proportion of sickness absences [11]-[17]. Lifestyle-related risk factors of sickness absences such as obesity, tobacco use, alcohol intake, and physical inactivity have also been identified [18]-[21].

A systematic review of earlier studies on the association between risk factors and sickness absence was presented in [22]. The review concluded that the knowledge of the causes and consequences of sick leave is still limited. In addition, it is difficult to generalize the overall results across studies from different countries because of the large differences in economic and social environments which affect both the studied predictors and the sick leave outcomes. Indeed, sickness absence is a dynamic temporal behavior and many risk factors vary over time. Much of the literature on this topic, however, lacks information on such aspects of the phenomenon of sickness absences and influential factors.

In this paper, we are going to particularly address some methodological difficulties in terms of statistical models with complicated sick leave data. We also demonstrate a new method by performing a longitudinal assessment of long-term absenteeism using a large registration dataset as a working example, available from the Helsinki Health Study for municipal employees from the City of Helsinki in Finland during the period of 1990-1999. The strengths of the material include a large sample size and a long follow-up period with ten waves of data collection.

II. COMMONLY USED MODELS AND MODEL APPLICABILITY

To date, in the literature on sickness absences, cross-sectional studies prevail. Such a data design is not always appropriate for analyzing sickness absenteeism. Moreover, in both cross-sectional and longitudinal studies, sick leave data are often highly skewed and clustered at zero. In rare cases in which the dependent variable, for example the duration of absences, has a normal distribution, linear regression model is often a first choice.

In this section, we shall discuss some of the widely used statistical models employed for sick leave analysis. We provide a brief outline of the model equations without going into details. Since it is out of the scope of this paper to give a thoroughly review of these methods, we have chosen to focus on introducing representative models to highlight some
important methodological issues we may face with sick leave data. However, we should, whenever possible, bear in mind that the model chosen is always dependent upon the problem specification and data at hand.

A. Linear Regression

Let the observation \( y_i \) be a realization of dependent variable \( Y_i \) which has a normal distribution with mean \( \mu_i \) and variance \( \sigma^2 \) as

\[
y_i \sim N(\mu_i, \sigma^2)
\]

Suppose we have data on predictors \( x_{i1}, \ldots, x_{ip} \) which take values \( x_{i1}, \ldots, x_{ip} \) for the \( i \)th unit. Then a linear model refers to a simple mapping between \( \mu_i \) and the predictors as

\[
\mu_i = x_i' \theta
\]

where \( x_i \) is a vector with the values of the \( p \) predictors for the \( i \)th unit and \( \theta \) a vector containing the \( p \) regression coefficients. The maximum likelihood (ML) parameter estimates \( \theta \) can be obtained with well-known least squares method.

To examine the trends in socio-economic differences in long sickness absence spells, a linear regression model was adopted for analyzing longitudinal sick leave data [23]. Serial correlation due to the repeated observations over the years was not taken into account in their studies.

B. Logistic Regression

We only illustrate the case where the observation \( y_i \) is the binary coded as zero or one for convenience. Then the dependent variable \( Y_i \) takes the values zero and one with probabilities \( \pi_i \) and \( 1-\pi_i \). The distribution of \( Y_i \) is a Bernoulli as

\[
y_i \sim B(\pi_i)
\]

The logistic model supposes further that the logit of the probability \( \pi_i \) is a linear function of the predictors expressed as

\[
\text{logit}(\pi_i) = x_i' \theta
\]

where vectors of predictors and regression coefficients are \( x_i \) and \( \theta \).

Note that the logistic model is a generalized linear model with link function logit. Hence the regression coefficients can be interpreted along the same lines as in linear model. However, as the left-hand-side of (4) is a logit but not a mean, \( \theta \) presents the change in the logit of the probability associated with a unit change in the \( j \)th predictor if all other predictors are held constant. Logistic regression is a useful way of describing the relationship between risk factors and occurrences or incidences of sick leave [12], [16].

In examining the long and short-term economic incentives inherent in the sickness and unemployment insurances, sickness duration was modelled with a linear regression and the outcome of healthy and non-healthy was modelled with a logistic regression. These two models were not linked statistically [9].

This type of model is often employed for studies on cross-sectional or pooled sick leave data in most of the published research reports. Obviously, some interesting and, possibly, important time series issues involved in sick leave data can not be properly studied with cross-sectional or pooled data which can be an important risk factor. For example, in the study of absenteism costs for 1284 hourly workers from a manufacturing company, the best single predictor of future absenteism was claimed to be the past absenteism [24]. Furthermore, there are strong heterogeneties among individuals for some risk factors as described in Introduction and found in literature review. These suggest that a longitudinal design is more appropriate. Longitudinal analysis becomes even more difficult when analyzing sickness absence data. Very often, the data have a large number of values centered at zero and skewing of the rest of the values. Furthermore, the observations are likely correlated as the data are collected over time for the same samples.

With regard to the above-described concerns, Poisson regression and zero-inflated Poisson models are often applied when the outcome of sick leave counts is the focus.

C. Poisson Regression and Zero-inflated Poisson Regression

Suppose a sample of observation \( y_i \) is a realization of the dependent Poisson variable \( Y_i \) which takes the integer values as 0, 1, 2… and has Poisson distribution with both mean and variance \( \mu_i \) as

\[
y_i \sim P(\mu_i)
\]

The Poisson regression models the mean or variance as

\[
\log(\mu_i) = x_i' \theta
\]

where vectors of predictors and regression coefficients are \( x_i \) and \( \theta \).

Note that the Poisson model is again another type of generalized linear model with link function log. In the model, the regression coefficient \( \theta \) presents the expected change in the log of the mean per unit change in the predictor \( x_i \). Increasing \( x_i \) by one unit is associated with an increase of \( \theta \) in the log of the mean.

Using a register-based cohort of all live-born in Norway between 1967 and 1976, the extent to which musculoskeletal sickness absence was influenced by a range of circumstances concerning family background and health in early life was investigated with Poisson regression model [11]. In accounting for non-normal distribution of the dependent variable of absence spells in most of the cases, Poisson regression has been found to be superior to linear regression in sick leave absence studies [25]-[26].

Indeed, the often encountered non-normal distribution of the outcome is also a threat to the validity of the commonly adopted statistical analysis as we mentioned before. Treating the data as they were normally distributed is inappropriate which may lead to the wrong conclusions. One obvious and simple way to avoid such difficulty is to use distribution-free
or nonparametric approaches. Therefore, many studies performed logistic regression models as cited before (e.g. [3], [17], [27]). Note that this model discards the important ‘duration’ information of sick leave counts which is obviously important for us to understand sick leave behaviors.

As a result, zero-inflated Poisson (ZIP), zero-inflated binomial (ZIB) and zero-inflated negative binomial (ZINB) models are often the best way to model zero-clustered sick leave data. A literature review shows that only ZINB model has been employed to study sick leave data. Using cross-sectional data, the associations between self-reported health problems and sickness absence from work were analyzed [2].

The link functions of the models of ZIP, ZIB, ZINB are the same as that of Poisson regression model. The only difference among these models is the count probability distributions in which ZIP, ZIB and ZINB allow for over-dispersion. Such feature can be modified further to best suit particular data structures and study aims. We previously tried ZIP and ZINB models for our data (see below for description) with the WinBUGS software. Unfortunately, WinBUGS could not handle such an oversized dataset.

III. A NEW MODEL: TWO-PART MIXED-DISTRIBUTION MODEL

Here we propose a more flexible model: the two-part mixed-distribution model originated in econometrics studies [28]-[29]. The original model presented one part for the probability of occurrence of nonzero observations (a probit or logit model) and one part for the probability distribution of the nonzero observations. The two parts were assumed to be not connected. Recently, the model has been extended as a mixed-distribution model for longitudinal data. Random effects have been included in the two parts which are allowed to be linked [30]-[32]. Tooze et al. also implemented the model in a SAS Macro called MIXCORR (available from the first author) [32].

The dependent variable $Y_i$ has continuous distribution and takes the observed value $y_{it}$ for subject $i$ at time $t$. Let $R_{it}$ denote the occurrence variable defined as

$$R_{it} = \begin{cases} 0, & \text{if } Y_{it} = 0 \\ 1, & \text{if } Y_{it} > 0 \end{cases}$$

with conditional probabilities

$$\Pr(R_{it} = r_{it} | \theta_i) = \begin{cases} 1 - p_d(\theta_i), & \text{if } r_{it} = 0 \\ p_d(\theta_i), & \text{if } r_{it} = 1 \end{cases}$$

where $\theta_i = (\beta_i, u_{it})'$ is a vector of fixed ($\beta_i$) and random occurrence ($u_{it}$) effects.

One part of the two-part mixed-distribution model, logistic model, for occurrence takes the form

$$\logit(p_d(\theta_i)) = X_{it}^{'}\beta_i + u_{it}$$

where $X_{it}$ is a vector of covariates for occurrence.

Another part of the two-part mixed-distribution model, log-normal model, for duration variable $Y'^{'}_{it} = [Y_{it} | R_{it} = 1]$ takes the following form

$$\log(Y'^{'}_{it} | \theta_2) \sim N(\mu_{Z_{it}}, \sigma^2_{\theta_2})$$

where $X_{Z_{it}}$ is a vector of covariates for duration and $\theta_2 = (\beta_2, u_{Z_{it}})'$ is a vector of fixed ($\beta_2$) and random intensity ($u_{Z_{it}}$) effects.

The two-part models are assumed to be correlated with the following correlation matrix as

$$\begin{bmatrix} u_{1i} \\ u_{2i} \end{bmatrix} \sim \text{BVN} \left( \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \sigma_1^2 & \rho \sigma_1 \sigma_2 \\ \rho \sigma_1 \sigma_2 & \sigma_2^2 \end{bmatrix} \right)$$

through the coefficient $\rho$. If $\rho = 0$, the two parts are not correlated.

It is easy to verify that the p.d.f., $f(y_{it} | \theta_i)$, has mixed distributions. The likelihood is maximized to get the estimated $\beta_1, \beta_2, \sigma_1, \sigma_2, \rho$. Akaike’s Information Criterion (AIC) can be used to compare the model’s goodness of fit which is constructed by penalising the log-likelihood for the number of parameters [33].

IV. WORKING EXAMPLES

A. Data

Since our main goal is to propose a way to select an appropriate model and to introduce a new methodology for analysing sickness absence data as well as to demonstrate model applicability to such complicated longitudinal data, we choose a large registration sick leave dataset with long-term outcomes as a working example to demonstrate the effectiveness of our proposed new model. The follow-up consists of ten waves of data collection. From a methodological point of view, our focus is to show superior performance of the introduced new model. Based on this argument, the data, data variables and analysis results will be reported briefly. More details about the data background can be found in [23].

Data are from the Helsinki Health Study on health and well-being for municipal employees from the City of Helsinki in Finland which cover all employees’ information on sickness absence and other individual level information. Spells of sickness absences are grouped as short-term sickness absences with 0–3 days and medically confirmed long-term sickness absences with over 3 days. We select long-term sickness absence as an outcome which is further processed as a continuous variable in order to meet the requirements of two-part mixed-distribution model in the following way: The annual sickness absence rate is expressed as a percentage of total working days less holidays, including public holidays, i.e. the percentage of the number of absence days (short or long-term) due to work divided by total possible working days (maximum value is 100). Socio-economic, demographic and occupational characteristics of the employees are selected as independent variables. In particular we investigate weather
differences in socio-economic and occupational characteristics are important explanatory factors.

Table I briefly describes the selected variables studied in this analysis. Fig. 1 shows average temporal changes for long-term sickness absences, indicating that the changes are nonlinear. Therefore we add \( \text{YEAR}^2 = \text{YEAR} \times \text{YEAR} \) as an extra predictor.

The following notations are adopted in the model: \( i \) denotes the \( i \)th individual; \( t \) denotes the \( t \)th year. We shall assess the accuracy of the proposed model by comparing prediction performances from these three models. The models are fit separately to each gender.

- **Model 1:** General linear model:

\[
\log(\text{ABSENCE}_it) = \beta_0 + \beta_1 \text{YEAR}_it + \beta_2 \text{YEAR}^2_it + \beta_3 \text{AGE}_it + \beta_4 \text{SES}_it + \beta_5 \text{EDU}_it + \beta_6 \text{INCOME}_it + \beta_7 \text{CONTRACT}_it + \epsilon_i
\]

where \( \epsilon_i \sim N(0, \sigma^2) \) (12)

- **Model 2:** Uncorrelated model:

Denote

\[
Y_{it} = \text{ABSENCE}_it \quad (13)
\]

\[
X_{1it} = (\text{YEAR}_it, \text{YEAR}^2_it, \text{AGE}_it, \text{SES}_it, \text{EDU}_it, \text{INCOME}_it, \text{CONTRACT}_it) \quad (14)
\]

\[
X_{2it} = (\text{YEAR}_it, \text{YEAR}^2_it, \text{AGE}_it, \text{SES}_it, \text{EDU}_it, \text{INCOME}_it, \text{CONTRACT}_it) \quad (15)
\]

The logistic equation is presented in (9) and log-normal equation in (10) with \( \rho = 0 \) in (11).

- **Model 3:** Correlated model:

Equations of both the logistic part and the log-normal part are the same as (13)-(15) but \( \rho \neq 0 \) in (11).

The comparison results are displayed in Table II for male staff. We only show some of the most relevant results here.

### Table I

<table>
<thead>
<tr>
<th>Variables</th>
<th>Total sample number = 50256</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABSENCE</td>
<td>annual rate of long-term absence (0-100), continuous</td>
</tr>
<tr>
<td>YEAR</td>
<td>year (1990-1999), continuous</td>
</tr>
<tr>
<td>AGE</td>
<td>age (18-64), continuous</td>
</tr>
<tr>
<td>GENDER</td>
<td>gender, categorical</td>
</tr>
<tr>
<td></td>
<td>M: male</td>
</tr>
<tr>
<td></td>
<td>F: female</td>
</tr>
<tr>
<td>SES</td>
<td>socio-economic class (1-4), categorical</td>
</tr>
<tr>
<td></td>
<td>1: managers and professionals</td>
</tr>
<tr>
<td></td>
<td>2: semi-professionals</td>
</tr>
<tr>
<td></td>
<td>3: routine non-manuals</td>
</tr>
<tr>
<td></td>
<td>4: manual worker</td>
</tr>
<tr>
<td>EDU</td>
<td>educational background (1-5), categorical</td>
</tr>
<tr>
<td>INCOME</td>
<td>logarithm of annual income, continuous</td>
</tr>
<tr>
<td>CONTRACT</td>
<td>employment contract type (1-4), categorical</td>
</tr>
</tbody>
</table>

Fig. 1 Average rates of short and long-term sickness absences from 1990 to 1999

Because many employees did not have any absenteeism, the dependent variables have many zero observations. Take the year 1999 as an example, the percentages of zeroes are 55% and 66% for male and female, respectively.

### Model Comparison and Statistics for Long-Term Sickness Absences

<table>
<thead>
<tr>
<th>Variables</th>
<th>Model 1 Parameter value (SE)</th>
<th>Model 2 Parameter value (SE)</th>
<th>Model 3 Parameter value (SE)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \sigma^2 )</td>
<td>2.3398 (0.0822)</td>
<td>2.3318 (0.0809)</td>
<td>2.3318 (0.0809)</td>
</tr>
<tr>
<td>(-2 \text{ Res Log AIC} )</td>
<td>110932.0</td>
<td>110974.0</td>
<td>110974.0</td>
</tr>
<tr>
<td>( \rho, \sigma^2 )</td>
<td>0.5655 (0.0246)</td>
<td>0.5655 (0.0246)</td>
<td>0.5655 (0.0246)</td>
</tr>
</tbody>
</table>

Table II illustrates that the AIC estimates of log-normal models for Model 2 is smaller than that of the general linear Model 1 indicating that Model 2 fits the data better. Note that
Model 1 is also a log linear regression. So the comparison is valid. The value ‘Diff in -2LL 666.91 \( p < 0.0001 \)' shown in the right down column in Table II indicates that the two-part mixed-distribution Model 3 fits the data significantly better than the uncorrelated Model 2 does. This claim can be also concluded from the value \( \rho_{12} \sigma_2 (0.5655^{**}) \) also, reporting that the two-part logistic and log-norm models are significantly correlated. Overall, we demonstrate significantly better performance of the proposed new model. It is worth noting that similar model comparison results as Table II are also obtained for female employees.

C. Analysis Results

<table>
<thead>
<tr>
<th>Variables</th>
<th>Uncorrelated model</th>
<th>Correlated model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>YEAR(^2)</td>
<td>–**</td>
<td>–**</td>
</tr>
<tr>
<td>Female</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intercept</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>YEAR(^2)</td>
<td>–**</td>
<td>–**</td>
</tr>
<tr>
<td>Male</td>
<td>Intercept</td>
<td>–</td>
</tr>
<tr>
<td>Intercept</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>YEAR(^2)</td>
<td>–**</td>
<td>–**</td>
</tr>
<tr>
<td>Male</td>
<td>Intercept</td>
<td>–</td>
</tr>
<tr>
<td>Intercept</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>YEAR(^2)</td>
<td>–**</td>
<td>–**</td>
</tr>
</tbody>
</table>

Table III illustrates some fit statistics using our three candidate models. For simplicity, only inconsistent results with respect to male and female employees are displayed with only signs. The consistent results are presented in the following paragraph. A positive sign (+) indicates a positive association and a negative sign (−) indicates a negative association of the predictors.

Table III illustrates in general that the incidence and duration of long-term sickness absences for male and female follow different temporal trends linearly or nonlinearly. It also demonstrates that inexact predictions are obtained in Model 1: no significant correlation of YEAR with long-term sickness duration is claimed from Model 1 for male staff for example, however Model 2 and Model 3 conclude differently. This shows that statistical inference can be inefficient and misguided if inappropriate model is adopted.

Finally, let's briefly summarize the consistent results we get for both male and female municipal employees. Considering the associations of the covariates with the probability of long-term sickness absences, younger staff had significantly lower absence probabilities. Higher-income subjects tended to have less probability of long-term sickness absences. Employees' socio-economic class had significantly effect on the long-term absence incidences. Manual worker had the highest absence incidence. The descending order of long-term absence incidence according to the category of socio-economic class is: manual worker, routine non-manuals, semi-professionals, managers and professionals, which indicates that employees performing technical-manual work had higher incidence of long-term work absence than those performing mental work. There is an association between employment contract types and the incidence of long-term sickness absences. Employees who had a temporary working contract had a significantly lower incidence of work absence.

Turning to the associations of the covariates with the duration of long-term sickness absences (i.e. employees who did have long-term work absences or long-term absence rates were positive). All covariates are significant predictors. The accumulative absence days increased according to the following category of employees' socio-economic class: managers and professionals, semi-professionals, routine non-manuals, and manual workers.

V. Conclusion

Absenteism is a major concern in our society. Even though extensive research has focused on relevant risk-based investigations, knowledge of the causes and consequences of sick leave is still limited. In addition, sickness absence is a dynamic temporal behavior and many influential factors vary over time. It is obvious that analysis of cross-sectional data, which is the most common technique in sick leave studies, is not enough for understanding the dynamic performances of sickness absences. There is a lack of studies on the dynamic process of sickness absence behaviors in literature. The hampering factors exist in both data surrounding and analysis methodologies. In this paper, we have focused on addressing these difficult issues.

Firstly, we have identified common data characteristics of sickness absence such as time dependent, highly skewed and clumped at zero, which challenges the traditional models. Ignoring these features to make statistical inference is likely to be inefficient and misguided. Take the example of long-term sickness absence rates referring to Table III, the time variable YEAR is predicted differently and errily by general linear model.

Secondly, we have discussed commonly employed approaches used in sickness absence research to empirically address the methodology issues and proposed a way for selecting proper models. We have introduced the two-part mixed-distribution model for analysing longitudinal sickness absence data. This is one of the main purposes of this paper. An application of the model has been presented by using a large registration dataset from the Helsinki Health Study for municipal employees during the period of 1990-1999. Calculation results have demonstrated that the proposed model perform superior to other commonly adopted models in the literature.
Finally, to summarize and conclude the analysis results, the basic conclusion is that there is strong relationship between socio-economic and occupational background and long-term sickness absences. The revealed findings, through an application of the proposed two-part mixed-distribution model, are consistent with the literature.

REFERENCES


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