Abstract—This paper presents modeling and analysis of 12-phase distribution static compensator (DSTATCOM), which is capable of balancing the source currents in spite of unbalanced loading and phase outages. In addition to balance the supply current, the power factor can be set to a desired value. The theory of instantaneous symmetrical components is used to generate the twelve-phase reference currents. These reference currents are then tracked using current controlled voltage source inverter, operated in a hysteresis band control scheme. An ideal compensator in place of physical realization of the compensator is used. The performance of the proposed DTATCOM is validated through MATLAB simulation and detailed simulation results are given.

Keywords—DSTATCOM, Modeling, Load balancing, Multi-phase, Power factor correction.

I. INTRODUCTION

MULTI-PHASE (phase order higher than three) system: such as electrical generation, transmission and drives are the focus of research recently due to their inherent advantages compared to their three-phase counterparts [1]-[6].

Multi-phase inverter fed induction motor drives has been found to be quite promising for high power ratings and other specialized applications. The use of such drives and devices presents multi-phase load circuits that may get subjected to phase outages and unbalanced as well as non-linear loading similar to their three-phase counter parts. Such conditions may lead to variety of undesirable effects on the supply system such as additional losses in connecting lines and interfacing devices, oscillatory torques in ac machines, saturation in transformers, increased ripple in rectifiers, malfunctioning in sensitive equipments, harmonic and excessive neutral currents etc. It is therefore desired to have the balanced power system operation with minimum lower order harmonics even in the presence of such operations. A number of methods based on the instantaneous reactive power theory [7]-[9], theory of symmetrical components [10]-[15] and reference frame theory [16]-[18] have been evolved for the compensation of harmonics and unbalances for three phase system. However, instantaneous symmetrical components theory is preferred. Based on this theory the compensator reference currents are generated, which are then realized by hysteresis band control of the inverter circuit and are injected at point of common coupling. The inverter circuit has 12 bridge arms connected to a split capacitor, controlled by chopper. It has been shown that the instantaneous power in the electrical system containing an unbalanced load has an oscillating component that ride a dc value [10]. The objective of the compensator is to supply zero mean oscillating power such that the dc component can be supplied by the source. This paper introduces modeling and analysis of twelve-phase DTATCOM based on instantaneous symmetrical components for balancing the unbalanced multi-phase load and power factor correction on supply side. The detailed simulation results are given and discussed for verification.

II. THE PROPOSED TWELVE-PHASE COMPENSATOR

A. PRINCIPLE OF DSTACOM

The basic compensation scheme for 12-phase (multi-phase) load supplied from a balanced stiff multi-phase source is shown in Fig. 1

![Fig. 1 Schematic diagram of the compensator for star connected load (12-phase 13-wire system)](image_url)
scheme is to extract the compensator currents,

\[ i_{ep} (p = a, b, c, d, e, f, g, h, i, j, k & l) \]

denoted by

\[ i_{ep}^* (p = a, b, c, d, e, f, g, h, i, j, k & l) \]

from the measure circuit variables, which make the unbalanced loads on the supply side balanced. The proposed scheme can be applied to a 12-phase, 12-wire system or a 12-phase, 13-wire system by isolating or connecting the common points N or n respectively. The reference currents are generated using the theory of the instantaneous symmetrical components [11] and these currents by inclusion of loss term \( P_{loss} \) in the power are given as follows:

\[
\begin{align*}
&i_{ea}^* = i_{ia} - \frac{\{v_{sa} + \xi(v_{sa} - v_{sd})\}}{4(v_{sa}^2 + v_{se}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{eb}^* = i_{ib} + \frac{\{v_{sb} + \xi(v_{sb} - v_{sd})\}}{4(v_{sb}^2 + v_{se}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{ec}^* = i_{ic} - \frac{\{v_{sc} + \xi(v_{sc} - v_{sd})\}}{4(v_{sc}^2 + v_{se}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{ed}^* = i_{id} + \frac{\{v_{sd} + \xi(v_{sd} - v_{sb})\}}{4(v_{sd}^2 + v_{se}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{ee}^* = i_{ie} - \frac{\{v_{se} + \xi(v_{se} - v_{sc})\}}{4(v_{se}^2 + v_{se}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{ef}^* = i_{ig} + \frac{\{v_{sf} + \xi(v_{sf} - v_{se})\}}{4(v_{sf}^2 + v_{se}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{eg}^* = i_{ih} + \frac{\{v_{sh} + \xi(v_{sh} - v_{se})\}}{4(v_{sh}^2 + v_{se}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{eh}^* = i_{ij} + \frac{\{v_{si} + \xi(v_{si} - v_{sh})\}}{4(v_{si}^2 + v_{sh}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{ei}^* = i_{il} - \frac{\{v_{si} + \xi(v_{si} - v_{sh})\}}{4(v_{si}^2 + v_{sh}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{ej}^* = i_{ij} + \frac{\{v_{sj} + \xi(v_{sj} - v_{sh})\}}{4(v_{sj}^2 + v_{sh}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{ek}^* = i_{ik} + \frac{\{v_{sk} + \xi(v_{sk} - v_{sh})\}}{4(v_{sk}^2 + v_{sh}^2 + v_{sl}^2)}(P_{lavg} + P_{loss}) \\
i_{el}^* = i_{il} - \frac{\{v_{sl} + \xi(v_{sl} - v_{sh})\}}{4(v_{sl}^2 + v_{sh}^2 + v_{sl}^2)}(P_{lavg} + P_{loss})
\end{align*}
\]

where \( \xi = \tan \frac{\phi}{\sqrt{3}} \), \( \phi \) is the desired phase angle between supply voltages and compensated sources currents in the respective phases. \( P_{lavg} \) is the dc value of load power and is determined by employing moving average filter having mean time of half cycle. The term \( P_{loss} \) is account for losses in the inverter. To generate \( P_{loss} \) a suitable closed-loop dc-link voltage controller is used, which regulate the dc voltage to the reference value. Conventionally a proportional-plus-integral (PI) controller is used to maintain the dc-link voltage.

### B. TOPOLOGY OF TWELVE-PHASE DSTATCOM

The topology of the proposed twelve-phase DSTATCOM has been derived from its three-phase counterpart where an inverter circuit is employed with a self-charged capacitor as DC source and unbalanced load circuit connected at point of common coupling (PCC) as load to the inverter. The proposed twelve-phase compensator consists of twelve arms of a single-phase H-inverter circuits as shown in Fig. 2 with split capacitor for providing the neutral point \( n^* \) of the compensator.

A single capacitor instead of two capacitors can be used if neutral point of the converter is not required as 12-phase 12-wire system. In case of two-capacitor topology, it has been reported in literature that capacitor voltages becomes unbalanced and therefore may lead to unstable operation in a three-phase circuit. To avoid the unbalanced operation of capacitors, a chopper can be used to balance the capacitor voltage. The chopper is controlled in such a way that capacitor voltages are dynamically regulated to have equal average voltage. It is to be noted that like any inverter circuit, this...
converter circuit has the same switching constraint, i.e. any switch pair \( S \) and \( \overline{S} \) of the bridge arm are never be closed together to avoid shoot through fault across the charged capacitors. The converter can be operated as inverter by switching a pair of switching elements of this circuit. One of the simplest ways is pulse width modulated switching where a reference voltage is compared with a fixed amplitude and frequency carrier voltage and the switching instants of the switching elements are decided. This technique is however employed if the converter is desired to be operating as voltage source inverter. The proposed circuit is required to be operating as current controlled voltage source inverter and this may be achieved by hysteresis band control of the inverter or converter current.

In a hysteresis band control, the converter current is forced to remain in a hysteresis band around the reference current. The reference currents for all the twelve phase for a twelve-phase compensator are given by (15-26).

\[
S_a = \begin{cases} 
1 & \text{if switch is on} \\
0 & \text{otherwise} 
\end{cases}
\]  

The state space equations for the circuit shown in Fig. 3. Let \( i_1 \) and \( i_2 \) be the currents in circuit of the chopper (Fig. 3), then (27) and (28) represents the relation of these in terms of switching function and the converter current.

\[
\begin{align*}
\frac{di_{ca}}{dt} & = -\frac{R}{L}i_{cb} + S_a V_{cl} - \overline{S_a} \frac{V_{c2}}{L} - \frac{v_{sa}}{L} \\
\frac{di_{ch}}{dt} & = -\frac{R}{L}i_{cb} + S_h \frac{V_{c1}}{L} - \overline{S_h} \frac{V_{c2}}{L} - \frac{v_{sh}}{L} \\
\frac{di_{ce}}{dt} & = -\frac{R}{L}i_{ce} + S_a \frac{V_{c1}}{L} - \overline{S_a} \frac{V_{c2}}{L} - \frac{v_{sc}}{L} \\
\frac{di_{cf}}{dt} & = -\frac{R}{L}i_{cf} + S_f \frac{V_{c1}}{L} - \overline{S_f} \frac{V_{c2}}{L} - \frac{v_{sf}}{L} \\
\frac{di_{cg}}{dt} & = -\frac{R}{L}i_{cg} + S_g \frac{V_{c1}}{L} - \overline{S_g} \frac{V_{c2}}{L} - \frac{v_{sg}}{L} \\
\frac{di_{ch}}{dt} & = -\frac{R}{L}i_{ch} + S_h \frac{V_{c1}}{L} - \overline{S_h} \frac{V_{c2}}{L} - \frac{v_{sh}}{L} \\
\frac{di_{ci}}{dt} & = -\frac{R}{L}i_{ci} + S_i \frac{V_{c1}}{L} - \overline{S_i} \frac{V_{c2}}{L} - \frac{v_{si}}{L} \\
\frac{di_{ci}}{dt} & = -\frac{R}{L}i_{ci} + S_i \frac{V_{c1}}{L} - \overline{S_i} \frac{V_{c2}}{L} - \frac{v_{si}}{L}
\end{align*}
\]
\begin{align}
    i &= S_u * i_{a} + S_b * i_{b} + S_c * i_{c} + S_d * i_{d} + S_e * i_{e} + S_f * i_{f} + S_g * i_{g} + S_h * i_{h} + S_j * i_{j} + S_k * i_{k} + S_l * i_{l} + S_m * i_{m} + S_n * i_{n} + S_o * i_{o} + S_p * i_{p} + S_q * i_{q} + S_r * i_{r} + S_s * i_{s} + S_t * i_{t} + S_u * i_{u} + S_v * i_{v} + S_w * i_{w} + S_x * i_{x} + S_y * i_{y} + S_z * i_{z} \\
    \frac{dV}{dt} &= -S_u * \frac{i_{a}}{L} - S_b * \frac{i_{b}}{L} - S_c * \frac{i_{c}}{L} - S_d * \frac{i_{d}}{L} - S_e * \frac{i_{e}}{L} - S_f * \frac{i_{f}}{L} - S_g * \frac{i_{g}}{L} - S_h * \frac{i_{h}}{L} - S_j * \frac{i_{j}}{L} - S_k * \frac{i_{k}}{L} - S_l * \frac{i_{l}}{L} - S_m * \frac{i_{m}}{L} - S_n * \frac{i_{n}}{L} - S_o * \frac{i_{o}}{L} - S_p * \frac{i_{p}}{L} - S_q * \frac{i_{q}}{L} - S_r * \frac{i_{r}}{L} - S_s * \frac{i_{s}}{L} - S_t * \frac{i_{t}}{L} - S_u * \frac{i_{u}}{L} - S_v * \frac{i_{v}}{L} - S_w * \frac{i_{w}}{L} - S_x * \frac{i_{x}}{L} - S_y * \frac{i_{y}}{L} - S_z * \frac{i_{z}}{L} \\
    \frac{dV}{dt} &= -S_u * \frac{i_{a}}{L} - S_b * \frac{i_{b}}{L} - S_c * \frac{i_{c}}{L} - S_d * \frac{i_{d}}{L} - S_e * \frac{i_{e}}{L} - S_f * \frac{i_{f}}{L} - S_g * \frac{i_{g}}{L} - S_h * \frac{i_{h}}{L} - S_j * \frac{i_{j}}{L} - S_k * \frac{i_{k}}{L} - S_l * \frac{i_{l}}{L} - S_m * \frac{i_{m}}{L} - S_n * \frac{i_{n}}{L} - S_o * \frac{i_{o}}{L} - S_p * \frac{i_{p}}{L} - S_q * \frac{i_{q}}{L} - S_r * \frac{i_{r}}{L} - S_s * \frac{i_{s}}{L} - S_t * \frac{i_{t}}{L} - S_u * \frac{i_{u}}{L} - S_v * \frac{i_{v}}{L} - S_w * \frac{i_{w}}{L} - S_x * \frac{i_{x}}{L} - S_y * \frac{i_{y}}{L} - S_z * \frac{i_{z}}{L} \\
    \frac{dV}{dt} &= -S_u * \frac{i_{a}}{L} - S_b * \frac{i_{b}}{L} - S_c * \frac{i_{c}}{L} - S_d * \frac{i_{d}}{L} - S_e * \frac{i_{e}}{L} - S_f * \frac{i_{f}}{L} - S_g * \frac{i_{g}}{L} - S_h * \frac{i_{h}}{L} - S_j * \frac{i_{j}}{L} - S_k * \frac{i_{k}}{L} - S_l * \frac{i_{l}}{L} - S_m * \frac{i_{m}}{L} - S_n * \frac{i_{n}}{L} - S_o * \frac{i_{o}}{L} - S_p * \frac{i_{p}}{L} - S_q * \frac{i_{q}}{L} - S_r * \frac{i_{r}}{L} - S_s * \frac{i_{s}}{L} - S_t * \frac{i_{t}}{L} - S_u * \frac{i_{u}}{L} - S_v * \frac{i_{v}}{L} - S_w * \frac{i_{w}}{L} - S_x * \frac{i_{x}}{L} - S_y * \frac{i_{y}}{L} - S_z * \frac{i_{z}}{L} \\
    \frac{dc}{dt} &= \frac{R_{ch}}{L_{ch}} + S_u \frac{V_{c1}}{L_{ch}} - S_u \frac{V_{c2}}{L_{ch}} \\
\end{align}

The final expressions (29)-(31) can be obtained by applying the principle of KCL and KVL.

The variables used in the expressions (29)-(31) are indicated in the circuit diagrams. The capacitor voltages reduce if not compensated for the losses in the connecting transformer/ inductor, which can be accounted by changing the duty cycle of the chopper. The change in duty of the chopper is based on the change in the capacitor voltage from the set reference voltage. The difference in the capacitor voltage and set voltage (i.e. the error voltage) is put forward to the set reference voltage. The difference in the capacitor voltage and set voltage (i.e. the error voltage) is put forward to the set reference voltage. The sources for compensator to work satisfactorily. All the simulation results will be presented and discussed.

### III. STUDIES OF SIMULATION

The simulation study has been carried to validate the performance of the proposed 12-phase DSTATCOM for unbalanced linear loading and phase outages. It is desired that the source current be balanced and source operate at unity power factor. In this section, the simulation results will be presented and discussed.

#### A. Compensation for Unbalanced Loads

The system as shown in Fig.1 has the following specifications namely voltages and impedances.

\[ v_{sl} = 325 \times 0.26 \sin (100 \pi t - i * \pi / 6) \]

where \( t = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 \text{ and } 12 \) corresponds to phase a, b, c, d, e, f, g, h, i, j, k & l respectively.

\[
\begin{align*}
    Z_a &= 20 + j10; \\
    Z_b &= 30 + j25; \\
    Z_c &= 45 + j45; \\
    Z_d &= 25 + j5; \\
    Z_e &= 30 + j15; \\
    Z_f &= 30 + j30; \\
    Z_g &= 10 + j25; \\
    Z_h &= 5 + j5; \\
    Z_i &= 15 + j0.0; \\
    Z_j &= 25 + j25; \\
    Z_k &= 30 + j65; \\
    Z_l &= 30 + j30
\end{align*}
\]

The isolation transformer parameters are as follows:

\[ R = 2 \quad \Omega \quad L = 200 \quad mH \]

The control parameters for regulating capacitor voltage of the chopper are adjusted heuristically and are given as follows:

\[ K_p = 50 \quad K_i = 1000 \]

In the simulation results, the system works with unbalanced load for one cycle (0.02sec) and run for another three cycle 0.08sec) with the proposed compensator. It can be seen from Fig 4 (b) and Fig. 4 (c) that the source currents and load currents are equal and unbalanced when compensator is off. After 0.02sec, the compensator is turned on the source currents become perfectly balanced as shown in Fig. 4 (c). In order to compensate unbalanced load currents, the instantaneous compensator currents become unbalanced accordingly as shown in Fig. 4 (d).
The instantaneous powers (source, load and compensator powers) and neutral currents (source and load neutral currents) are depicted in Fig. 5. It can be seen from Fig. 5 (a) that before compensation, that is, when compensator is switched off, source power \( P_s \) and load power \( P_l \) are equal in magnitude and oscillating in nature due to unbalance in load currents. But after compensation when compensator is turned on the oscillating component of power in source attains a steady state value as can be seen from Fig. 5 (a) while load power is oscillating in nature as shown in Fig. 5 (a). Moreover, the source neutral current \( i_{SN} \) attains zero value when the compensator is turned on and can be seen from Fig. 5 (b) as it balances the source currents. It can thus be inferred that the sum of the instantaneous compensator currents is equal to load neutral \( i_{NB} \).

The co-phasors variation of voltage and current shows unity power factor operation with compensator on as evident from Figs. 6 (a)-(l). It can be seen from (10b) that impedances are

![Fig. 4 Variation of source voltages, load currents and compensator currents for 12-phase 13-wire supply system (diagram)](image4)

![Fig. 5 Variation of powers and neutral current for 12-phase 13-wire supply system (diagram)](image5)

![Fig. 6 (a)-(l) (1:18) scaled source voltages (solid line), source currents (dashed line), load currents (hard solid line) and variation of compensator currents, portraying u.p.f. operation for 12-phase 13-wire supply system (diagram)](image6)

unbalanced and have reactive elements, but the currents are not only balanced but also operate at unity power factor.

The D.C. link capacitor maintains the constant voltage through the PI controller. The voltage variation of individual capacitor is shown in Fig. 7. Please note that the capacitor voltage is assumed to be initially charged or recharged.
B. Load Compensation for Phase Outages

As stated earlier that advantage of multiphase loads like motor is in its capability to operate with phase outages. The motor operates with degraded performance and source sees an unbalanced operation and therefore other loads connected to such a source get affected. The proposed compensator has also been tested with various combination of phase outages and it has been found that it works satisfactorily even with six phases open (with phase outages (a, b, c, d, e, and f)) in a 12-phase source. The results are shown in Fig. 8 to Fig. 11 where entire source currents are balanced with compensator on.

Fig. 7 Capacitor voltage variation

Fig. 8 Variation of load currents, source currents and compensator currents when six phases (a, b, c, d, e, f) are out (from load side) from 12-phase 13-wire supply system

Fig. 9 Variation of power and current when six phases (a, b, c, d, e & f) are out in 12-phase13-wire supply system

Fig. 10 (a)-(l) (1:18) Scaled source voltages (solid line), source currents (dashed line), load currents (hard solid line) and variation of compensator currents for the phase outage (a, b, c, d, e, f) of load for12-phase 13-wire supply system
In this paper, a current-controlled VSI topology for 12-phase DSTATCOM is presented for load compensation of 12-phase systems. The mathematical model of the DSTATCOM used in simulations is derived by means of a three-phase space vector model. The DSTATCOM has an attractive design with a unity power factor, a fast dynamic response, and an easy control process. The DSTATCOM provides a good control of reactive power, leading and lagging power factor, harmonic compensation, and load balancing.

The proposed configuration of the DSTATCOM is validated through simulation using MATLAB/SIMULINK. The results obtained with the DSTATCOM are compared with those obtained with the 6-phase DSTATCOM. The results show that the DSTATCOM has better performance compared to the 6-phase DSTATCOM.

The effectiveness of the proposed DSTATCOM is demonstrated through simulations of a 12-phase transmission system. The results show that the DSTATCOM is able to compensate for the reactive and harmonic currents and improve the power factor of the system.

REFERENCES


