Development of Scratching Monitoring System Based On Mathematical Model of Unconstrained Bed Sensing Method

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Abstract—We propose an unconstrained measurement system for scratching motion based on mathematical model of unconstrained bed sensing method which could measure the bed vibrations due to the motion of the person on the bed. In this paper, we construct mathematical model of the unconstrained bed monitoring system; and we apply the unconstrained bed sensing method to the system for detecting scratching motion. The proposed sensors are placed under the three bed feet. When the person is lying on the bed, the output signals from the sensors are proportional to the magnitude of the vibration due to the scratching motion. Hence, we could detect the subject’s scratching motion from the output signals from ceramic sensors. We evaluated two scratching motions using the proposed system in the validity experiment as follows: 1st experiment is the subject’s scratching the right side cheek with his right hand, and; 2nd experiment is the subject’s scratching the shin with another foot. As the results of the experiment, we recognized the scratching signals that enable the determination when the scratching occurred. Furthermore, the difference among the amplitudes of the output signals enabled us to estimate where the subject scratched.

Keywords—Unconstrained bed sensing method, scratching, body movement, itchy, piezoceramics.

I. INTRODUCTION

FEELING itchy can be occurred as a symptom of various skin diseases affecting patients, who scratch the itchy parts to decrease the itch. Skin inflammation, however, can become worse from the scratching [1] and the patients hardly to sleep well. The gravity of skin diseases accompanied by itching is related to the frequency of the itch [2]. So the more severe the disease is, the longer the scratching time by the patient. The scratching time information is compiled into an index referred to as TST%, which is the ratio of total scratching time (TST) to total measurement time during sleep. The data is correlated to the degree of pruritus in skin diseases such as atopic dermatitis [3], [4]. Therefore, measurement of the scratching is effective in diagnosing skin diseases. Moreover, since the itch occurs irregularly, the patient unconsciously scratches while sleeping. Since patients can control the scratching while they are awake, a more accurate evaluation would be made by monitoring the scratching motion while they are asleep. In clinical practice, an infrared video camera is generally used to monitor the location, pattern, and frequency of scratching during sleep. Using camera, however, is not suitable for daily monitoring, since it infringes on the patients’ privacy and it also requires a large-scale system.

Given these circumstances, various smaller-scale methods have been proposed for evaluating scratching motion during sleep. For the most part, they are aimed at recording the motion or the sound of scratching, or the acceleration of wrist movement and its angular velocity. An electromyograph can be used to measure the electrical activity of the muscles in the forearm. Other devices can be used to measure the change in pressure at the back of the hand, the expansion and contraction motions of the finger [1]-[12]. Furthermore, RF-ID can be used to measure limbs’ monitoring in sleep diseases [13]. These methods, however, are somewhat bothersome as the sensors must be attached directly to the patient’s arms or feet.

One of the effective approaches for daily biosignals monitoring is measuring patients’ biosignals without having to wear any sensors on their body. So, in this paper, we describe an unconstrained measurement system for scratching motion based on mathematical model of unconstrained bed sensing method. Furthermore, proposed system can estimate where subject scratch during sleep.

II. MATHEMATICAL MODEL OF UNCONSTRAINED BED SENSING METHOD FOR SCRATCHING MONITORING SYSTEM

A. System of Unconstrained Bed Sensing Method

Fig. 1 shows the proposed unconstrained bed sensor system by piezoceramics. The piezoceramics bonded to stainless steel plates are set beneath each of the three feet of the bed to prop the weight of the bed including the person on it. Since piezoceramics have capacitive characteristics, the output voltage in the steady state is zero-biased and changes from zero voltage.
We defined the variables and constants for the piezoceramics and the unconstrained bed sensing system shown in Fig. 1 as follows:

**[Piezoceramics]**

- \( A \) [C/m] or [N/V]: force part of the piezoceramic device
- \( M \) [kg]: mass of bed including person on it
- \( k \) [N/m]: stiffness constant of the metal stainless steel plate
- \( d \) [Ns/m]: damping coefficient of the metal plate
- \( C \) [F]: capacitance between the piezoceramic
- \( R \) [Ω]: input resistance of the processor
- \( t \) [s]: time
- \( \alpha(t) \) [m]: resultant displacement of stainless steel plate
- \( f(t) \) [N]: force generated by the devices
- \( q(t) \) [C]: electric charge generated by external strain or bend to the ceramics
- \( \theta \) [rad]: sinking angle of the bed from the head to foot direction due to change in position of person on the bed
- \( \theta_{\text{h}}(t), \theta_{\text{d}}(t) \): sinking angle of the bed from the head to foot direction and from the left to right direction, respectively

**[Bed]**

- \( G, G' \): center of gravity (CG)
- \( F_{\text{h}}(t) \) [N]: forces pushing the bed by heartbeat
- \( F_{\text{d}}(t) \) [N]: forces pushing by respiration motion
- \( g \) [m/s²]: magnitude of acceleration due to gravity
- \( M \) [kg]: weight of the bed with a person on it
- \( L \) [m]: length of the bed
- \( L_{\text{f}} \) [m]: length from CG to foot side of the bed
- \( L_{\text{h}} \) [m]: length from CG to head side of the bed
- \( W \) [m]: width of the bed
- \( W_{\text{f}} \) [m]: length from CG to left side of the bed
- \( W_{\text{r}} \) [m]: length from CG to right side bed of the bed
- \( d(t) \) [m]: displacement of CG of the bed by change in position of person on the bed
- \( w(t) \) [m]: displacement of CG of the bed from the left to right direction due to change in position of person on the bed
- \( d_{\text{h}} \) [m]: distance from the heart to CG
- \( d_{\text{d}} \) [m]: distance from the diaphragm for respiration to CG

From the system shown in Fig. 1, we measured the heartbeat and respiration from output \( e_{\text{d}}(t), e_{\text{h}}(t) \) or \( e_{\theta}(t) \). Furthermore, in order to detect changes in position and scratching motions, we integrated the difference between two outputs \( e_{\text{d}}(t), e_{\text{h}}(t) \) from the left side and \( e_{\text{h}}(t), e_{\text{h}}(t) \) as follows:

\[
P_{\text{h}}(t) = \int [e_{\text{h}}(t) - e_{\text{h}}(t)] dt
\]

\[
P_{\text{d}}(t) = \int [e_{\text{d}}(t) - e_{\text{h}}(t)] dt
\]

**B. Theoretical Model of the System**

Here, we describe mathematical model of unconstrained bed sensing method shown in Fig. 1. Fig. 2 shows a situation where a person is lying on the bed. The location of the heart is at distance \( d_{\text{h}} \) from the CG and the diaphragm for respiration is at distance \( d_{\text{d}} \) from the CG. The heartbeat and respiration motions push the bed via forces \( F_{\text{h}}(t) \) and \( F_{\text{d}}(t) \) at these positions, respectively. Furthermore, the person moves toward the foot side of the bed as well as toward the right side of the bed and the CG shifts from \( G \) to \( G' \) for displacement \( \theta(t) \) and \( \theta(t) \), and the foot side sinks at angle \( \theta_{\text{d}}(t) \) and the right side sinks at angle \( \theta_{\text{h}}(t) \), respectively, as shown in Fig. 2.
First, we considered the bed motion and piezoceramic output from the foot and head side. Suppose the shift \( h(t) \) is very short and \( l(t) \ll L_f, L_h, L_s \), thus the sinking angle \( \theta_h(t) \) around \( G \) and \( G' \) is the same. Assuming uniform mass for the bed with a person on it, the inertia moment \( G' \) is the same. Assuming uniform mass for the bed with a

\[
G_{i}(s) = \frac{L}{C}, \quad G_{s}(s) = \frac{sCR}{1+sCR}, \quad G_{s}(s|L_{s}) = \frac{L_{s}}{s^{2} + \frac{D}{L_{s}} s + \frac{1}{L_{s}} \left[ K_{h} + \frac{1}{sBRLL_{L}A} \right]} \tag{6}
\]

Then, output \( e_t \) with respect to input forces \( Mgl + d_{hf}F_{hf} + d_{h}F_{h} \) is given:

\[
e_t = G_t(s) \cdot G_s(s) \cdot G_{s}(s|L_{s})(Mgl + d_{hf}F_{hf} + d_{h}F_{h}) \tag{7}
\]

Similarly, from (4) and (7), the output voltage from the head side is given by:

\[
e_s = -G_t(s) \cdot G_s(s) \cdot G_{s}(s|L_{s})(Mgl + d_{hf}F_{hf} + d_{h}F_{h}) \tag{8}
\]

These outputs correspond to the outputs of \( e_{0}(t) \), \( e_{d}(t) \) and \( e_{d}(t) \) in Fig. 1.

C. Measurement of Heartbeat, Respiration and Body Movement

Since we could select a large input resistance \( R \) such as 1 to 10 \( \text{M} \Omega \), which is usual, the cut-off frequency \( \frac{1}{2\pi CR} \) of \( G_t(s) \) is sufficiently lower than the frequency range of the fundamental and higher components of the heartbeat. Furthermore, we could also select a resonance frequency

\[
f = \frac{1}{2\pi} \sqrt{\frac{K_{h}}{I_{h}} + \left( L_{L}, A^{2}/R \right)} = \frac{1}{2\pi} \sqrt{\frac{3Lk[A_{L}^{2} + A_{L}^{2}]}{I_{h}}} \tag{9}
\]

of the transfer function \( G_t(s) \) around the components of the heartbeat, so that output voltages \( e_{t}(t) \) and \( e_{d}(t) \) include the enhanced heartbeat signals. For the low-frequency range where \( f < \frac{1}{2\pi CR} \), from (2), (6), (7) and (8) in the time domain, we obtained the following approximations:

\[
e_{t}(t) = AR \frac{L_{s}}{k(L_{s} + L_{h})} d \{ Mgl + d_{hf}F_{hf} + d_{h}F_{h} \} \tag{10}
\]

\[
e_{s}(t) = -AR \frac{L_{s}}{k(L_{s} + L_{h})} d \{ Mgl + d_{hf}F_{hf} + d_{h}F_{h} \}
\]

Similarly, output voltages \( e_{t}(t) \) and \( e_{d}(t) \) due to shifting of the body to the left or right side and heartbeat and respiration, can be obtained as follows:

\[
e_{t}(t) = AR \frac{W_{r}}{k(W_{r}^{2} + W_{h}^{2})} d \{ Mgw(t) + d_{hf}F_{hf}(t) + d_{h}F_{h}(t) \}
\]

\[
e_{d}(t) = -AR \frac{W_{r}}{k(W_{r}^{2} + W_{h}^{2})} d \{ Mgw(t) + d_{hf}F_{hf}(t) + d_{h}F_{h}(t) \} \tag{11}
\]

Thus, (12) can be derived.
\[ P_a(t) = \int [e_x(t) - e_n(t)] dt = AR \frac{L}{k(L_1^2 + L_2^2)} \{Mg(t) + d_n F_n(t) + d_a F_a(t)\} \]
\[ P_a(t) = \int [e_y(t) - e_n(t)] dt = AR \frac{W}{k(W_1^2 + W_2^2)} \{Mgw(t) + d_n F_n(t) + d_a F_a(t)\} \]  
(12)

when body movements occur, because

\[ Mg(t) >> d_n F_n(t) + d_a F_a(t) \]
and

\[ Mgw(t) >> d_n F_n(t) + d_a F_a(t) \]  
(12) can simply be rewritten as:

\[ P_a(t) = \frac{ARLMg}{k(L_1^2 + L_2^2)} l(t) \]
\[ P_a(t) = \frac{ARWMg}{k(W_1^2 + W_2^2)} w(t) \]  
(13)

where each is linearly proportional to the shift in the CG at the foot to the head side and at the left to the right side, from which we can estimate the movement of the person on the bed.

III. VALIDITY EXPERIMENT

A. Experimental Settings

Fig. 3 shows the experimental system and structure of piezoceramic sensor used for the proposed unconstrained bed sensing system. The ceramics in this sensor is 20mm in diameter and is firmly affixed to a brass metal plate, which is 25mm in diameter. This device is typically used for a buzzer. The device is bonded to a stainless steel plate of 1mm in thickness and 50mm in diameter. Under the stainless steel plate is a washer with an inner radius of 15mm, outer radius of 25mm, and thickness of 2mm. The bottom is covered with an aluminum plate that is the same size as the stainless steel plate.

The sensor has the following characteristics: \(1 \times 10^{-7} \, \text{C/m}\), which is the displacement of electrical charge by piezoelectricity. The capacitance is 0.01\(\mu\text{F}\). Due to the capacitive characteristics of piezoceramics, the output voltage in the steady state is zero-biased and changes from zero voltage. The bed used in Fig. 4 is a coil cushion type weighing 60kg and measuring 1.0 \times 2.1 \, \text{m}. Three piezoceramic sensors are placed under the three legs of the bed. The outputs \(e_x(t)\), \(e_y(t)\), and \(e_d(t)\) measured using the piezoceramic sensors go through the low-pass filter to remove the high-frequency noise component. The cutoff frequency \(f_l\) of the low-pass filter is set to 12 Hz.

The output signals from the low-pass filters are A/D-converted, in which the sampling interval is set to 1 ms and the scale range to \(\pm 1 \, \text{V}\) using a data logger (NR-2000, Keyence Co. Ltd.). The subject in this experiment was male, approximately 172cm in height and 63kg in weight, and did not suffer from any sleep disorders.

B. Experimental Procedures

As the starting position, the subject is lying on back at the center of the bed with the arms and legs straight, as shown in Fig. 4. The subject scratches two cases as follows.

(1\(^{st}\) Experiment)

The subject scratches his cheek 20 times. He then returns the arm back to the starting position. After a 5sec. pause, the subject once again scratches his cheek 20 times in a row. The set of scratching motions is repeated 35 times.

(2\(^{nd}\) Experiment)

The subject scratches his left shin 10 times by his right foot. He then returns his right foot back to the starting position. After a 5sec. pause, the subject once again scratches his left shin 10 times in a row. The set of scratching motions is repeated 5 times. Similarly, subject scratches his right shin 10 times by left foot. And subject repeated the scratching motion 5 times.

Since scratching is a reciprocating motion of the fingers, the sensor extracts the cyclically changing periods as scratching time in its data output.
IV. EXPERIMENTAL RESULTS

A. Results of 1st Experiment

Fig. 5 shows the results of one period of scratching of right cheek. From top to bottom in the Fig. 5 (a) shows $e_d(t)$, $e_a(t)$, and $e_h(t)$, and in Fig. 5 (b) shows $P_d(t)$ and $P_a(t)$.

The subject scratched his cheek from about 4 s to 7.5s. At the beginning and end, from about 3 to 4s and 7.5 to 9s, the subject had been moving his right arm, which occurred a large change in the output from all sources. When the subject was resting quietly, the output signal from piezoceramic was hardly changed. While scratching motion, all sensors show a cyclic change in signal simultaneously.

From 0 to 3s in Fig. 5 (a), because the subject’s hand is stationary beside his body, the sensors $e_h(t)$, $e_d(t)$ and $e_a(t)$, therefore measure the heartbeat signal. The waveform from 3 to 4s corresponds to the 20 times of scratching motion, and $e_h(t)$, $e_d(t)$ and $e_a(t)$ is synchronized with the scratching motion and shows large cyclical fluctuations. The comparison among $e_h(t)$, $e_d(t)$ and $e_a(t)$ shows that the outputs from $e_h(t)$ and $e_a(t)$, which are closer to the head, have a larger-amplitude wave shape than those from $e_d(t)$, which are closer to the feet. Moreover, the output from $e_h(t)$, which is positioned beneath the right side of the head, becomes the largest among the three, since the subject scratches his right cheek. Therefore, the more distant the piezoceramics sensors are from the scratching point, the smaller their output signals are.

The length of the scratching period can be confirmed as the transfer of the center of gravity, either.

B. Result of 2nd Experiment

Fig. 6 shows the results of one period of scratching of the left side shin by right foot. From top to bottom in the Fig. 6 (a) shows $e_d(t)$, $e_a(t)$, and $e_h(t)$, and in Fig. 6 (b) shows $P_d(t)$ and $P_a(t)$.

As with the scratching motion above, cyclical output signals corresponding to the feet movements can be confirmed. When the feet move, the outputs from the sensors near the feet become larger than those from the ones near the pillow. The integral results showed the amplitude of $P_h(t)$ was larger than that of $P_d(t)$. Since the scratching motion of the foot is in the head-foot direction, the output of $P_d(t)$ largely changed corresponding with the motion. As there was little movement toward right or left, there was little change in $P_a(t)$ due to the transfer of the center of gravity, either.

DISCUSSION

The measurement results from the scratching motions all showed cyclical signals with relatively large amplitude, which
enables the measurement of the length of the scratching motions. The length of the scratching motion is correlated with the gravity of the skin disorders, and its index, TST%, can be obtained as shown below.

Let the total measurement time and the total scratching time be $T_m$ and $T_r$ respectively. The TST% is calculated as follows:

$$TST\% = \frac{T_r}{T_m} \times 100$$

This enables the unconstrained measurement and evaluation of the scratching motions while the patients are asleep.

The sensors are set beneath the bed, so there is less awareness of their presence compared to conventional bed sensing and scratching monitoring systems [1]-[12].

In the case of skin diseases characterized by itching, this method enables contact-free measurement of scratching frequency during sleep, which is normally very difficult to ascertain. This system can measure the period of scratching motion, and calculate the TST% for monitoring and the acquisition of detailed information.

The $P_{rl}(t)$ and $P_{fh}(t)$ in (1) enables the acquisition of the data on the transfer of patient’s center of gravity on the bed due to the body movements. The data can be applied to the estimation of the scratched area from the body movement before the scratching.

The positive and negative output of $P_{rl}(t)$ correspond to the head-foot direction and the foot-head direction of the transfer of the center of gravity: The positive and negative output of $P_{fh}(t)$ correspond to the left-right direction and the right-left direction of the transfer of the center of gravity. If the $P_{rl}(t)$ is larger than the $P_{fh}(t)$, the scratching is with a foot; and if not, it is with a hand.

The amplitude of $P_{rl}(t)$ while the foot is in a scratching motion is larger than that of $P_{fh}(t)$, because the output signals from the sensors near the feet are larger than the output signals from those near the pillow. Further enhancing the difference in the amplitude are the facts that: 1) there is little transfer of the center of gravity to the right or the left, and; 2) in (1), $P_{fh}(t)$ only uses the output signals only from the sensors near the pillow for the calculation, while $P_{ml}(t)$ applies the output signals from those near the feet.

As the experiment in 2nd experiment shows, the proposed system not only enables the measurement of the itching through the scratching motions, but can be applied to observe abnormal motions of the limbs such as those accompanying the restless legs syndrome, which can cause insomnia. The proposed system has great advantage in its capability to carry out such measurements without directly touching the sleeping subject.

VI. CONCLUSIONS

In this paper, we proposed a novel sensing device using piezoceramic sensors to measure scratching motions based on mathematical model of unconstrained bed sensing method. This device consists of a piezoceramic sandwiched between metal plates and placed under the legs of the bed. This device can measure micro-vibrations produced by the scratching motion of the subject on the bed. The TST%, an important index for evaluating the scratching motions, could be calculated from the signals measured with the ceramic sensor devices. Furthermore, using the integrated value of the difference of output signals from three ceramic sensor devices, a change in position of the person on the bed could be detected.

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REFERENCES


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