Power System Damping Using Hierarchical Fuzzy Multi-Input PSS and Communication Lines Active Power Deviations Input and SVC

Mohammad Hasan Raouf, Ahmad Rouhani, Mohammad Abedini, Ebrahim Rasooli Anarmarzi

Abstract—In this paper the application of a hierarchical fuzzy system (HFS) based on MPSS and SVC in multi-machine environment is studied. Also the effect of communication lines active power variance signal between two $\Delta P_{\text{Tie-line}}$ regions, as one of the inputs of hierarchical fuzzy multi-input PSS and SVC (HFMPSS & SVC), on the increase of low frequency oscillation damping is examined. In the MPSS, to have better efficiency an auxiliary signal of reactive power deviation ($\Delta Q$) is added with $\Delta P + \Delta \omega$ input type PSS. The number of rules grows exponentially with the number of variables in a classic fuzzy system. To reduce the number of rules the HFS consists of a number of low-dimensional fuzzy systems in a hierarchical structure. Phasor model of SVC is described and used in this paper. The performances of MPSS and $\Delta P_{\text{Tie-line}}$ based HFMPSS and also the proposed method in damping inter-area mode of oscillation are examined in response to disturbances. The efficiency of the proposed model is examined by simulating a four-machine power system. Results show that the proposed method is performing satisfactorily within the whole range of disturbances and reduces the cost of system.

Keywords—Communication lines active power variance signal, Hierarchical fuzzy system (HFS), Multi-input power system stabilizer (MPSS), Static VAR compensator (SVC).

I. INTRODUCTION

ONE of the problems that electrical engineers are always facing with them is Power System oscillations. Power system stability is essential to reliable operation of power system. Power System Stabilizer is developed to improve damping of low frequency oscillations in Power System [1].

In the last two decades, several types of PSS are investigated. Classic PSS is one of the earliest types of methods to increase damping of low frequency oscillations. PSS is used based on different control methods in power systems, such as neural networks [2], fuzzy control [3], and genetic algorithm [4]. Also, FACTS devices are used for damping the low frequency oscillations [5]. MPSS has been developed to improve damping of low frequency power swing by adding reactive power signal to Classic PSS input [6], [7].

The dimension of the system variables is one of the most important problems in a classic fuzzy system. If there are $k$ input variables and $c$ membership functions are defined for each of these, then the number of rules in the fuzzy system is $c^k$. In fact the number of rules grows exponentially with the number of variables in a standard fuzzy system. The hierarchical fuzzy system (HFS) structure is used to solve this problem [8]-[11].

Static Var Compensator (SVC) is one of the most common Flexible AC Transmission Systems (FACTS) devices that behave like a variable shunt susceptance. SVC devices are used to improve voltage and reactive power conditions in power systems and also can be used as a reactive power supply. In fact SVC can consume the spare inductive reactive power from the grid or supply capacitive reactive power to the grid. In previous work the performances of CPSS&SVC and MPSS&SVC and also HFMPSS&SVC under similar transient conditions were studied [13].

In this paper, the effect of communication lines active power variance signal between two $\Delta P_{\text{Tie-line}}$ regions, as one of the inputs of HFMPSS & SVC on the increase of low frequency oscillation damping of the system and also the increase of capability of the system by variation in its working situation is studied. The effectiveness of the proposed method is then demonstrated through digital computer simulation. Also, its performance is compared with a MPSS and $\Delta P_{\text{Tie-line}}$ based HFMPSS. It is shown that, by application of proposed method, good dynamic performance can be obtained. MATLAB/SIMULINK is used for simulation.

II. EFFECT OF REACTIVE POWER DEVIATIONS AUXILIARY SIGNAL ON THE POWER SYSTEM STABILIZER

Stabilizers based on $\Delta \omega$ signal are used widely in different types of power plants, especially water units, since middle of 1960s. This kind of stabilizer damps rotor oscillations, but it may cause instability in torsional modes. Therefore, the main problem of this stabilizer is using the torsional filter. Also in order to weakening the torsional components of the stabilizer signal, the filter causes some phase lag in low frequencies. The occurred phase lag has a destroying effect on the stability of exciting mode and limits the total efficiency of stabilizer on the damping of system oscillation [13]. $\Delta P + \Delta \omega$ stabilizer is used to solve the above problem. Torsional components in the integral of signal $\Delta P$ are weakened and therefore, there is no need to torsional filter [9]. But by increasing $\delta$, sensitivity of...
∆P to oscillation is reduced. Thus, the efficiency of ∆P+∆W stabilizer is decreased. A system contain of a synchronies generator connected to an infinite bus by Xs impedance is shown in Fig. 1.

![Fig. 1 Model of machine connection to the infinite bus system where X’d transient reacance of machine, V system voltage, E generator voltage and Ea generator bus voltage](image)

By linearizing the above equations around working point δ = δ0, one has:

\[ \Delta P = \frac{\partial P}{\partial \delta} \Delta \delta = \frac{EV}{X_d' + X_e} \cos \delta_0 (\Delta \delta) \]

(3)

\[ \Delta Q = \frac{\partial Q}{\partial \delta} \Delta \delta = -\frac{EV}{X_d' + X_e} \sin \delta_0 (\Delta \delta) \]

(4)

Equations (3) and (4) are plotted in Fig. 2.

![Fig. 2 Variations of ∆P and ∆Q vs. δ](image)

As it can be seen in Fig. 2 by increasing δ; ∆P and ∆Q decreases and increases respectively in the range of 0-90 degrees. Therefore, sensitivity of ∆P to rotor angle variation decreases and sensitivity of reactive power to rotor angle variation increases. Since ∆P is the signal input of stabilizer type ∆P+∆W, its sensitivity decrease reduces stabilizer efficiency. To compensate this defect and increase the stabilizer efficiency, an auxiliary signal of reactive power deviation (∆Q) is used. It is expected that the reactive power input of the MPSS is effective to damp the lower frequency power swing. Thus, in angles 45°≤δ, increase of reactive power sensitivity to δ variation can be used to increase the efficiency of PSS.

### III. MULTI-INPUT STABILIZER STRUCTURE

MPSS is introduced to increase robustness for changing system conditions and to increase damping of power low frequency oscillations in power system. In conventional PSS, ∆P and ∆W signals are used as input. In MPSS, reactive power deviation (∆Q) is an additional signal added to conventional PSS input. MPSS structure is shown in Fig. 3. Two lead-lag compensators are used for every input signal [14]. But determining the compensator parameter is difficult.

![Fig. 3 Configuration of the MPSS](image)

In this paper, the proposed ∆Ptie-line based HFMPSS & SVC is used. In this type of stabilizer, hierarchical fuzzy controller is used instead of lead-lag compensators and static VAR compensator that have better efficiency than multi-input power system stabilizer (MPSS).

### IV. HIERARCHICAL FUZZY CONTROLLER

Fuzzy system does not require mathematical model. It can cover a wide range of operating conditions and it is attractive for nonlinear systems applications [15].

The aim of fuzzy control systems is to reduce the number of iterations and decrease computation time by using fuzzy logic. [16], [17].

In a standard fuzzy logic system the total number of involved rules grows exponentially whereas it is only linearly in a hierarchical form. In fact in a hierarchical fuzzy system the number of rules is altered by decomposing the fuzzy system to a set of simpler fuzzy subsystem connected in a hierarchical manner [18] as shown in Fig. 4.

The hierarchical fuzzy logic controller (HFLC) structure consists of a number of low-dimensional fuzzy systems in a hierarchical form. The most influential system variables are chosen in the first level, the next most important variables are chosen in the second level, and so on [19].

In fact, in the hierarchical fuzzy structure, each input variable is used in a two-input FLC and the input variables are put into a collection of low-dimensional fuzzy controller structure instead of single high-dimensional fuzzy structure.
units. It could be found that the total number of rules is greatly reduced under hierarchical fuzzy logic controller structure [20].

![Hierarchical FLC structural representation](image)

Fig. 4 Hierarchical FLC structural representation

V. HIERARCHICAL FUZZY MULTI-INPUT POWER SYSTEM STABILIZER

Three input variables (ΔP + Δω + ΔQ) are used as inputs of the HFMPSS. A fuzzy set with seven elements are defined as Table I. They are PB (Positive Big), PM (Positive Medium), PS (Positive Small), ZE (Zero), NS (Negative Small), NM (Negative Medium) and NB (Negative Big).

In this paper, Hierarchical control structure is constructed by two fuzzy subsystems where each subsystem has only two inputs. The ΔQ and Δω are the input variables of the first subsystem. The output of the first subsystem and the variable ΔP are the input variables of second subsystem as shown in Fig. 5.

![Detailed HFC structure](image)

Fig. 5 Detailed HFC structure

The triangular membership functions are used to define the degree of membership as shown in Fig. 6. Mamdani-minimum inference system and centroid defuzzification are used in this paper to design the fuzzy system. The adopted fuzzy rules are reported in Tables I and II.

The triangular membership functions are normalized using the following factors:

- \( K_p = 34.33 \), is the Speed change input coefficient;
- \( K_q = 0.0592 \), is the Reactive power change input coefficient;
- \( K_r = 0.53 \), is the Active power change input coefficient;
- \( K_{ui} = 1 \), is the Output coefficient (in subsystem 1); and
- \( K_{upS} = 1 \), is the Output coefficient (in subsystem 2).

![Membership Function Scaled from –1 to 1](image)

Fig. 6 Membership Function Scaled from –1 to 1

\[
\begin{array}{cccccccc}
\text{ΔP} & \text{ΔQ} & \text{Δω} & \text{Δu_1} & \text{Δu_pS} & \\
\text{NB} & \text{NB} & \text{NB} & \text{NB} & \text{NB} & \\
\text{NM} & \text{NB} & \text{NM} & \text{NM} & \text{NM} & \\
\text{NS} & \text{NB} & \text{NM} & \text{NS} & \text{NS} & \\
\text{ZE} & \text{NB} & \text{NM} & \text{NS} & \text{ZE} & \\
\text{PS} & \text{NM} & \text{NS} & \text{ZE} & \text{PS} & \\
\text{PM} & \text{NS} & \text{ZE} & \text{PS} & \text{PM} & \\
\text{PB} & \text{ZE} & \text{PS} & \text{PM} & \text{PB} & \\
\end{array}
\]

Table I

TABLE I

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<th>ΔP</th>
<th>ΔQ</th>
<th>Δω</th>
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<tbody>
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<tr>
<td>NM</td>
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</tr>
<tr>
<td>NS</td>
<td>NS</td>
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<td>ZE</td>
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<tr>
<td>PS</td>
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<td>PB</td>
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</table>

VI. STATIC VAR COMPENSATOR (SVC)

One of the SVC main advantages is to compensate the reactive power [12]. Also this device can be used to regulate the voltage at a chosen bus by suitable control of its equivalent reactance. To study the transient stability in this paper, a fuzzy model of SVC is used to regulate the busbar voltage. Since the important task of SVC is to increase transmission capacity as result of power oscillation damping the auxiliary control signal can be used in fuzzy model of SVC [21]. The proposed fuzzy model for SVC devices is shown in Fig. 7.

![Schematic of SVC](image)

The slope or droop of the V-I characteristic can be calculated as:

\[
X_{sd} = \frac{\Delta V}{\Delta I}
\]

where \( \Delta V \) is the ratio of change in voltage magnitude and \( \Delta I \) is...
the ratio of change in current magnitude.

$$V_{\text{max}}$$

+ -
$$\text{SVC Current}$$

$$B_{af} +$$

$$G_{1}(s)$$

$$B_{ SVC}$$

$$V_{i}$$

$$V_{ref}$$

$$V_{meas}$$

$$\text{Voltage Regulator}$$

$$\text{Auxiliary Control}$$

Fig. 7 SVC Controller

The common value of slope is 3-5% [21]. The SVC current can be calculated by multiplying $$B_{ref}$$ and $$V_{meas}$$. The proposed fuzzy model in this paper does not consist of any thyristor, synchronizing system or Gate Pulse Generator (GPG). The below transfer function for the proposed fuzzy model can also be obtained as [20]:

$$G_{1}(s) = \frac{e^{-sT_d}}{1 + sT_b}$$  \hspace{1cm} (6)

In this transfer function $$T_d$$ is the thyristor dead time, that is equal to one-twelfth cycle time, and $$T_b$$ is the thyristor firing-delay time caused by sequential switching of thyristors, that is approximately equal to one-quarter cycle time.

VII. SYSTEM MODEL

A. Power System Model

To simulating by the proposed idea in this paper, the Kundur’s Two-area Test System having 4 power plants and 11-bus is used [14]. Since the power system stability must be existed under all sequences after faults, the transmission line is shunt compensated at its center by a 1Mvar SVC. This system is shown in Fig. 8.

B. AVR and PSS

The excitation system is a dc exciter similar to described in [22] without the saturation function. The basic components that form the excitation system block are the voltage regulator and the exciter.

The conventional power system stabilizer (CPSS) method is a common approach to improve damping of low frequency oscillations but in a multi-machine power system, CPSS components need to be optimized to coordinate with other machines and devices such as FACTS devices. CPSS is modeled by the nonlinear system as shown in Fig. 9. The optimization method of this CPSS is same as that of [14]. The values of $$\Delta\omega$$ are given in Table V (see Appendix: Fuzzy Controller Data).

Fig. 9 Block diagram of the PSS

VIII. RESULTS

To evaluating the performance of the proposed method, two kinds of disturbances, small and large signal, are examined. The results are described as follows:

A. Small Disturbance

To study the efficiency of the proposed method in the case of small signal disturbance, 5% disturbance is applied to the reference voltage of machine 1 with both parallel transmission lines connected. The simulation results for rotor angle, terminal voltage and transmitted active power from area 1 to area 2 are shown in Figs. 10 to 12.

Fig. 10 Rotor angle deviation of machine 1 w.r.t. machine 4

Fig. 11 Terminal voltage of machine 1

Fig. 12 Transmitted active power from area 1 to area 2
These simulations results show the superiority of the proposed method (HFMPSS+Tie Line+SVC) compared to MPSS. Figs. 10-12 show that the proposed method and $\Delta P_{Tie\text{-}line}$ based HFMPSS (HFMPSS+Tie Line) have almost the same overshoot and settling time. It can be seen from Figs. 10-12 that the proposed design may rapidly damp out oscillation.

**B. Large Disturbance**

In this section to study the efficiency of the proposed method, first three-phase to earth error is created at the middle of one of the Tie-Lines. The performances of MPSS and HFMPSS+Tie Line and the proposed method under these transient conditions are shown in Figs. 13-15. As seen, the proposed method in this paper has better damping effectiveness and control performance in comparison with MPSS and HFMPSS+Tie Line in terms of settling times and damping effects.

**IX. CONCLUSION**

In this paper, the proposed design is studied for test system is given in [14]. MPSS increases the system stability in the low frequency oscillation for rotor angles $45^\circ \leq \delta$. In a standard fuzzy logic system the total number of rules grows exponentially whereas it is only linearly in a hierarchical structure. SVC is one of the most effective devices which are used primarily for the purpose of voltage and reactive power control. The objective of this paper is to increase damping of power system oscillations by using $\Delta P_{Tie\text{-}line}$ based HFMPSS&SVC. Active power deviation input of communication lines between two regions ($\Delta P_{Tie\text{-}line}$) is used to reduce cost of the system. Simulation results illustrate the better efficiency of proposed method to damp low frequency power oscillations compared to the MPSS, $\Delta P_{Tie\text{-}line}$ based HFMPSS and also the mentioned design in [23], which shows clearly the robustness of the proposed strategy in multi-input power system stability without changing any parameters.
APPENDIX

TABLE III

<table>
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<tr>
<th>Param</th>
<th>No. of Gen</th>
<th>G1,G2</th>
<th>G3,G4</th>
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<tr>
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<td>T''d0 (sec)</td>
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TABLE IV

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TABLE V

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<tr>
<td>T4 (sec)</td>
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Transmission Lines Data:

\[ V_{base} = 230kV, S_{base} = 100MVA \]

\[ R = 0.0001 \text{ pu/km}, X = 0.001 \text{ pu/km}, B_C = 0.00175 \text{ pu/km} \]

AVR Data:

\[ K_A = 200, T_A = 0.001 \text{ sec} \]

REFERENCES