Comparative Evaluation of Adaptive and Conventional Distance Relay for Parallel Transmission Line with Mutual Coupling

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Abstract—This paper presents the development of adaptive distance relay for protection of parallel transmission line with mutual coupling. The proposed adaptive relay, automatically adjusts its operation based on the acquisition of the data from distance relay of adjacent line and status of adjacent line from line circuit breaker IED (Intelligent Electronic Device). The zero sequence current of the adjacent parallel transmission line is used to compute zero sequence current ratio and the mutual coupling effect is fully compensated. The relay adapts to changing circumstances, like failure in communication from other relays and non-availability of adjacent transmission line. The performance of the proposed adaptive relay is tested using steady state and dynamic test procedures. The fault transients are obtained by simulating a realistic parallel transmission line system with mutual coupling effect in PSCAD. The evaluation test results show the efficacy of adaptive distance relay over the conventional distance relay.

Keywords—Adaptive relaying, distance measurement, mutual coupling, quadrilateral trip characteristic, zones of protection.

I. INTRODUCTION

The constraints in obtaining new right of ways have led to a number of parallel lines, as well as multi-terminal lines.

In transmission systems throughout the world, it is common to find double circuit towers transmitting power in narrow physical corridors. There are also the places in power systems where single circuit towers are run in parallel in wide corridors. This trend will increase due to continuing growth of load centers.

Distance protection is a commonly preferred over other line protection schemes. Its operation can rely only upon the local measurement and it is easy to extend functionality of a pilot type protection by the use of communication links. It can easily provide a staged remote backup protection for adjacent lines. However, when applied to parallel lines, the performance of conventional distance relays is adversely affected by the mutual coupling effects between the parallel lines, which vary with the line operating condition and bus configuration. Therefore, relays must be configured to avoid overreach / under reach operation under the worst-case scenarios. This results in sub optimal performance of a relay under other operating conditions.

Several researchers have proposed solutions to enhance the performance of the distance relay [1]-[4]. An adaptive distance scheme was suggested in [1], in which a correction factor, based on the information of the surrounding system of the protected line under different operating status, was used in the impedance calculation. In [2], an adaptive distance protection scheme is proposed which accesses multiple locally available signals and automatically adapts its operation to the signal availability. A traveling-wave based parallel line protection scheme was investigated in [3]. In [4], the phase current comparison between two circuits and positive sequence current level detection were used in conjunction with parallel line’s zero sequence current compensated impedance calculation. In [5], loadability of transmission lines is discussed extensively, and useful in simulation of fault conditions.

The implementation of adaptive distance relaying scheme to compensate mutual coupling effect and its elaborate evaluation procedure is not reported in the published literature. This paper presents the development of adaptive distance relay for protection of parallel transmission line with mutual coupling. The proposed adaptive relay automatically adjusts its operation based on the acquisition of data from distance relay of adjacent line and status of adjacent line from line breaker IED. When data from the adjacent line relay are available, zero sequence current of the adjacent parallel transmission line is used to compute zero sequence current ratio and the mutual coupling effect is fully compensated. On the other hand, the conventional distance relay would cause false tripping of healthy lines, due to undesirable compensation incorporated in relay logic program of distance relay of the adjacent healthy line. When the parallel line’s zero sequence current is not available from its communication channel, the adaptive distance relay uses line operating status to select the appropriate zero sequence current compensation factor in impedance calculation. Under severe circumstances, when line status as well as signal data are not available, the adaptive relay uses default compensation factor as minimum mode operation. The sections that follow explain the operating
principle of the proposed adaptive relaying scheme and evaluation of its performance using steady state and dynamic test procedures.

II. DISTANCE PROTECTION OF A DOUBLE-CIRCUIT LINE WITH MUTUAL COUPLING

The mutual coupling effect between lines, which varies with the line operating conditions and fault conditions is the main problem faced by conventional distance relays in distance measurement when applied on the parallel lines. The mutual coupling effects of zero sequence currents between parallel lines will be significant. Fig. 1 illustrates the conventional distance as applied to protect the parallel lines with mutual coupling.

For a line to ground fault on a single transmission line, the measured phase impedance seen by the conventional distance relay is given by using conventional zero sequence current compensation method.

The measured impedance in phase ‘a’ when the fault impedance is zero is,

$$Z_{m-a} = \frac{V_a}{I_a + K_0 I_0} = mZ_{1L}$$

where $K_0$ is the line zero sequence current compensation factor; $Z_{0L}$ and $Z_{1L}$ are the zero and positive sequence impedance of the line; $V_a$ and $I_a$ are the post-fault phase voltage and current at the relay location, $m$ is the per-unit distance between the relay and the fault location and $I_0$ is the post-fault zero sequence current at the relay location.

Generally, the mutual coupling effects between parallel lines caused by positive and negative sequence currents are very small and are considered to be negligible. However, the mutual coupling effects of zero sequence currents between parallel lines could be significant [2].

The post-fault voltage of phase at the relay location for a phase-a-to-ground fault when fault impedance is zero is given by

$$V_a = mZ_{1L} (I_a + K_0 I_0 + mZ_{0M} I_{0p})$$

Where, $Z_{0M}$ is the total zero sequence mutual coupling line impedance and $I_{0p}$ is the parallel line’s zero sequence current.

The measured fault impedance of a distance relay using conventional zero sequence current compensation will contain errors since

$$Z_{1m-a} = \frac{V_a}{I_a + K_0 I_0} = mZ_{1L} + \zeta Z_{1L}$$

Where, the per unit error $\zeta$ in terms of $Z_{1L}$ is

$$\zeta = \frac{m(Z_{0M} / Z_{1L})I_{0p}}{I_a + K_0 I_0}$$

This error may cause the relay either to overreach or underreach depending upon the relative direction of the parallel line’s zero sequence current, $I_{0p}$, versus the compensated current, $I_a + K_0 I_0$. If they are in the opposite direction, the relay will overreach. If in the same direction, the relay will underreach.

The above overreach or underreach effect of conventional distance relays, caused by the mutual coupling may be compensated by selecting proper relay settings provided the bus configuration, system impedance and line operating condition of a parallel line do not change during the normal operation.

Due to various reasons like load dispatch, forced outage, scheduled maintenance etc, operating condition of a parallel line could change from one to the other during the normal operations. Fig. 2(a) and 2(b) show such two typical operating conditions of a double-circuit line.

The mutual coupling effects on zone reach are different for these two operating conditions. Generally, the line operating condition shown in Fig. 2(a) will cause conventional distance relay to underreach and the line operating condition shown in Fig. 2(b) will cause conventional distance relay to overreach for remote end faults. There are other line operating conditions and/or the bus configurations combinations that could be encountered in the field, which further complicates the problem.

Note that a parallel line in most cases is operated under the operating condition in Fig. 2(a); reduced Zone 1 coverage.
reduces the chance of fault isolation by Zone 1 relay from both ends of the protected line. The situation could become even worse when the impact of fault resistance is considered, which may under certain conditions to cause the protected line’s middle section to lose the zone 1’s coverage altogether. Prolonged fault clearing reduces the system stability level and may lead to severe stability problems under constrained system operating conditions. The common practice in parallel line distance protection is to select relay settings to avoid possible false operation under the worst-case scenario [2].

Hence to minimize the effect of incorrect settings the system calls for the Adaptive protection, which covers the wide range of power system condition thus increasing the accuracy and selectivity of the protection system.

III. DEVELOPMENT OF ADAPTIVE DISTANCE RELAY

The proposed adaptive relaying scheme on each protected line accesses the three-phase voltage and current signals of the protected line. In addition, the zero sequence current and line operating status of the paralleled lines at the substation where the distance relay is located will be used by the scheme. The parallel line’s zero sequence current could be obtained either through additional cabling, direct communication link between relays, or substation local networks. The parallel line’s operating status could be obtained by accessing the circuit breaker’s auxiliary contacts and/or parallel line’s voltage/current level detection or substation PLC (programmable logic controller). The scheme automatically adapts its operation based on the signal availability from the parallel lines to achieve an optimal performance by using the best available signals.

If the parallel line’s zero sequence current is available the scheme uses it first to compensate the mutual coupling effect in impedance measurement on faulted line. For a phase-a-to-ground fault on the protected line, the correct fault impedance on the faulted line is:

\[ Z_{m\rightarrow a} = \frac{V_a}{I_a + K_0 I_0 + K_{0M} I_{op}} = mZ_{1L} \]  

Where \( K_{0M} = \frac{Z_{0M}}{Z_{1L}} \).

The distance measurement on the faulted line will always be correct under any line operating condition and/or bus configuration, since errors in distance measurement caused by the mutual coupling effect of \( I_{op} \) is fully compensated. Normal 80% zone coverage for zone 1 thus can be used, which will provide consistent zone coverage under all conditions for parallel lines.

When Parallel line’s zero sequence current compensation is applied on both faulted line and healthy line in the impedance computation, the relay placed in healthy line will also operate with the relay placed in faulted line. To avoid such possible false operation, the compensation should be adapted to the line fault status. In the proposed scheme it is achieved by using a zero sequence current ratio criterion.

The zero sequence current ratio for a protected line is defined as a magnitude ratio of paralleled line’s zero sequence current over the zero sequence current measured on the protected line [2].

For example, the zero sequence current ratio for the faulted line in the system in Fig. 1 is defined as (note that its inverse will define the zero sequence current ratio on the healthy line).

\[ \alpha_m = \frac{I_{0p}}{I_0} \]  

By setting a proper threshold equal to 1.0 plus some margin so that the compensation will not be performed when the ratio on the protected line is above the threshold, the relay false operation on the healthy line for close-in faults on an adjacent parallel line could be effectively prevented [2].

when the parallel line’s zero sequence current is not available due to local technical problems to the relay for various reasons, the proposed adaptive scheme adopts to use parallel line’s operating status signal, for an improved performance. A relay could make proper zone setting and/or zero sequence compensation factor adjustment to take into account of the mutual coupling effect corresponding to each line operating status.

The sequence network in Fig. 3 corresponds to the line operating condition in Fig. 2(a).

\[ Z_0S = \frac{mZ_{0L}}{1 - mZ_{1L}} \]

\[ Z_{GR} = \frac{mZ_{GR}}{1 - mZ_{1L}} \]

Fig. 3. Phase-To Ground Fault in One of Two Parallel Lines with Zero Sequence Mutual Coupling.

In Fig. 3, \( Z_{ab0} = Z_{ld0} \) is assumed, the accurate zero sequence compensation factor in (1) at \( m \) the fault location under this condition is,

\[ K_m = \frac{1 + Z_{ab0} Z_{0S}}{Z_{ab0} - Z_{0L} - 2Z_{0S} - 1} \]

This is a function of the fault location, system, and line impedance. Using \( k_{0L} \) with \( I_a \) in the fault impedance
calculation will result in overestimate of fault distance for faults close to and beyond the remote end \((m = 1.0)\) since

\[
K_0 < |K_1(m = 1.0)| = \left| \frac{Z_{oL} - Z_{oL} + Z_{oM}}{Z_{oL}} \right| \tag{8}
\]

The value for zone 1 could be determined at the zone setting boundary (80\%) using (7) for more accurate compensation of the mutual coupling effect. It should be selected to also consider the system parameter variations (mainly system impedance variations) during system operation, plus certain margins to ensure that relay will not overreach under all these variations.

Similarly, the zero sequence current compensation factor for one parallel line switched off and grounded at both ends could be derived. The zero sequence network for one parallel line switched off and grounded at both ends is shown in Fig. 4.

\[
I_0 - Z_{oS} \quad mZ_{oL} \quad (1 - m)Z_{oL} \quad Z_{oR} \\
I_D \\
(1 - m)Z_{oL} \quad Z_{oL} \quad (1 - m)Z_{oM} \\
I_P \quad Z_{0L} \quad \text{Fig. 4. Zero Sequence Network Connection for One Line Switched Off and Grounded Condition in A Single-to-Ground Fault}
\]

From Fig. 4, if \(Z_{oL} = Z_{oAB}\) is assumed, the accurate zero sequence compensation factor in (1) at the fault location \(m\) under this condition is given by

\[
K_2(m) = K_0 \left\{ 1 + \frac{Z_{oM}}{Z_{oL} - Z_{oL}} \frac{Z_{oU}(1 - m)Z_{oS} - mZ_{oK}}{Z_{oU}(1 - m)Z_{oU} + Z_{oK} - (1 - m)Z_{oM}} \right\} \tag{9}
\]

And it is also a function of the fault location, system, and line impedance. From the above equation, using \(K_0\) with \(I_0\) in the fault impedance calculation will result in an underestimate for remote end faults \((m = 1.0)\) since

\[
|K_2(m) > |K_2(m = 1.0)| = \left| \frac{Z_{oL} - Z_{oL} - \left( \frac{Z_{oM}^2}{Z_{oL}} \right)}{Z_{oL}} \right| \tag{10}
\]

The value for zone 1 should also be determined at the zone setting boundary (80\%) using (9) for more accurate compensation of the mutual coupling effect taking into account of system parameter variations, plus certain margins to avoid overreach operations.

Though not as effective as using parallel line’s zero sequence current, adapting zero sequence compensation factor to line operating status still achieves the performance improvement by compensating main underreach and overreach effect under each line operating condition.

In the case that both parallel line’s zero sequence current and line operating status signals are not accessible, a default zero sequence compensation factor \((K_3)\), based on the worst-case scenario, will be used by the new adaptive relay to ensure a reliable operation of the relay. This operation mode achieves the same performance level as conventional distance relays operating on the parallel lines.

An exemplary flowchart illustrating how the new adaptive scheme works is shown in Fig. 5. In this flowchart, the adaptive scheme first ascertains whether the parallel line’s zero sequence current is available. If available, the zero sequence current ratio is used to determine the line fault status. The parallel line’s zero sequence current will be used for faulted line impedance computation, but will not be used in healthy line’s impedance calculation.

When the adjacent parallel transmission line’s current is not available, the parallel line’s operating status at the relay location is used to select the proper zero sequence compensation factors. The relay logic program follows the sequence shown in flowchart, for both line in operation condition, and for one line switched off condition. In the case that both the parallel line’s current and operating status are not accessible, the scheme uses the default zero sequence current compensation factor.

Fig. 5. Adaptive Distance Protection logic Scheme Flow
IV. COMPARATIVE EVALUATION OF CONVENTIONAL AND ADAPTIVE DISTANCE RELAY BY DYNAMIC TEST

Comparing its performance with conventional distance relay carries out the evaluation of the simulated adaptive distance relay. For this purpose both relays are subjected to dynamic test.

The dynamic tests essentially determine the operating time and reach settings of the relay, when subjected to various fault conditions. This requires the simulation of transient fault dynamic conditions of the power transmission line. For this purpose EMTDC/PSCAD software package is used. The parallel transmission system considered is a 400KV, 200km long Transmission system as shown in Fig.6.

The system parameters are as follows:

**Line Impedance:**

\[
Z_{L0} = 0.297 + 1.1842i \, \Omega / km
\]
\[
Z_{L1} = Z_{L2} = 0.0352 + 0.4028i \, \Omega / km
\]
\[
Z_{Lm} = 0.262 + 0.7814i \, \Omega / km
\]

**Equivalent System Impedance:**

\[
Z_{S0} = 23.459 + 108.31i \, \Omega
\]
\[
Z_{S1} = 8.561 + 20.24i \, \Omega
\]
\[
Z_{S2} = 17.53 + 70.795i \, \Omega
\]
\[
Z_{S1} = 8.36 + 15.57i \, \Omega
\]

In this development, frequency dependent (Phase) model is selected in EMTDC/PSCAD for transmission line model. The adaptive relay is developed for zone 1 protection as shown in Fig. 7. Zone1 covers the 80% of the line L2. The quadrilateral trip characteristic will change automatically obtaining the parallel line’s operating status through substation PLC.

In order to conduct the evaluation test, two configurations of parallel transmission line are considered, they are i) One Line is Switched Off and grounded at Both Sides, ii) Two Parallel Lines are in Operation.

The test signals are obtained under various fault locations for the above configurations using PSCAD. They are i) 10% inside the zone1 ii) 10% outside the zone2, and iii) 10% before the relay location. Table 1 shows the case numbers for different fault conditions. In subsequent discussion these case numbers are used for referring to each case.

The evaluation tests were conducted on conventional distance relay in order to compare its performance with that of adaptive distance relay. The fault data sets that are used in evaluating the adaptive distance relay has been used for comparing the performance of the conventional distance relay.

The table II indicates the comparative performance of both the relays. The impedance trajectories of Fig. 8 and Fig. 9 for both adaptive relay and conventional relay show clearly that the conventional relay overreaches. On the other hand the proposed adaptive relay operated correctly. In some cases, for example in the cases (a.2) and (a.4), the operating time of the adaptive relay is more, but it is operating correctly compare to conventional relay. We can also observe when the two lines are in operation, the conventional distance relay of zone 1 mal operated in zone2 (case (b.2)). This can be found by observing the R-X plots of Fig. 10. In some cases like case (b.4), where the trip count is fixed, even though the conventional relay operated but the impedance computed is erroneous [since it not compensated], thus final impedance value lies outside the reach of the relay. Thus relay under-reaches. This can be observed in the R-X plot of Fig. 11.
### Table I
Differential Cases Considered for Comparative Evaluation

<table>
<thead>
<tr>
<th>Line status</th>
<th>Location of fault war. t.</th>
<th>Load applied</th>
<th>Inception of fault at voltage</th>
<th>Case no.</th>
</tr>
</thead>
<tbody>
<tr>
<td>One line in operation</td>
<td>10% inside the zone 1 end</td>
<td>10% FL</td>
<td>Zero</td>
<td>a.1</td>
</tr>
<tr>
<td></td>
<td></td>
<td>90% FL</td>
<td>Peak</td>
<td>a.2</td>
</tr>
<tr>
<td></td>
<td></td>
<td>10% outside the zone 1 end</td>
<td>10% FL</td>
<td>Zero</td>
</tr>
<tr>
<td></td>
<td></td>
<td>90% FL</td>
<td>Peak</td>
<td>a.6</td>
</tr>
<tr>
<td>Two lines in operation</td>
<td>10% inside the zone 1 end</td>
<td>10% FL</td>
<td>Zero</td>
<td>b.1</td>
</tr>
<tr>
<td></td>
<td></td>
<td>90% FL</td>
<td>Peak</td>
<td>b.2</td>
</tr>
<tr>
<td></td>
<td></td>
<td>10% outside the zone 1</td>
<td>10% FL</td>
<td>Zero</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>90% FL</td>
<td>Peak</td>
</tr>
</tbody>
</table>

### Table II
Results of Comparison Between Adaptive and Conventional Distance Relay

<table>
<thead>
<tr>
<th>Fault condition (fault location)</th>
<th>R-X plot (Fig)</th>
<th>Operating Time</th>
<th>Operating Status</th>
<th>Correct operation</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Conversely (Tripped in)</td>
<td>Adaptive Relay</td>
<td>Zone Relay</td>
</tr>
<tr>
<td>a.1 (Zone 1)</td>
<td>13</td>
<td>27ms, (Zone 1)</td>
<td>28ms</td>
<td>✓</td>
</tr>
<tr>
<td>a.2 (Zone 1)</td>
<td>31ms, (Zone 1)</td>
<td>33ms</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>a.3 (Zone 1)</td>
<td>27ms, (Zone 1)</td>
<td>26ms</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>a.4 (Zone 1)</td>
<td>32ms, (Zone 1)</td>
<td>40ms</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>a.5 (Zone 2)</td>
<td>27ms, (Zone 1)</td>
<td>Zone 2</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>a.6 (Zone 2)</td>
<td>25ms, (Zone 1)</td>
<td>Zone 2</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>a.7 (Zone 2)</td>
<td>26ms, (Zone 1)</td>
<td>Zone 2</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>a.8 (Zone 2)</td>
<td>24ms, (Zone 1)</td>
<td>Zone 2</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>b.1 (Zone 1)</td>
<td>5</td>
<td>25ms</td>
<td>25ms</td>
<td>✓</td>
</tr>
<tr>
<td>b.2 (Zone 1)</td>
<td>17</td>
<td>(Zone 2)</td>
<td>28ms</td>
<td>✓</td>
</tr>
<tr>
<td>b.3 (Zone 1)</td>
<td>25ms</td>
<td>24ms</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>b.4 (Zone 1)</td>
<td>8</td>
<td>21ms</td>
<td>21ms</td>
<td>✓</td>
</tr>
<tr>
<td>b.5 (Zone 2)</td>
<td>(Zone 2)</td>
<td>Zone 2</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>b.6 (Zone 2)</td>
<td>(Zone 2)</td>
<td>Zone 2</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>b.7 (Zone 2)</td>
<td>(Zone 2)</td>
<td>Zone 2</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>b.8 (Zone 2)</td>
<td>(Zone 2)</td>
<td>Zone 2</td>
<td>✓</td>
<td>✓</td>
</tr>
</tbody>
</table>

Fig. 8. R-X Diagrams of Adaptive and Convention Relay for the case (a.6).

Fig. 9. R-X Diagrams of Adaptive and Convention Relay for the case (a.7).

Fig. 10. R-X Diagrams of Adaptive and Convention Relay for the case (b.2).
V. CONCLUSION

The adaptive distance relay described in this paper provides an enhanced distance protection for parallel lines. No remote signals like parallel line zero sequence current are required for the proposed scheme. The proposed adaptive relay access the operating status of the parallel line through the substation PLC. The adaptation to the signal availability provides a built-in fallback scheme, which ensures the reliable operation under all conditions.

The developed quadrilateral trip characteristic with directionality feature is tested for the three-zone protection. The performance improvement of the proposed adaptive relaying has been verified on the simulated example system in PSCAD/EMTDC in comparison with conventional distance relay. The evaluation test results show the efficacy of adaptive distance relay over the conventional distance relay. Application of the new adaptive distance relay would provide an enhanced performance for distance protection on parallel lines with mutual coupling.

REFERENCES