Productive Design and Calculation of Intermittent Mechanisms with Radial Parallel Cams

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Abstract—The paper deals with the kinematics and automated calculation of intermittent mechanisms with radial cams. Currently, electronic cams are increasingly applied in the drives of working link mechanisms. Despite a huge advantage of electronic cams in their re-programmability or instantaneous change of displacement diagrams, conventional cam mechanisms have an irreplaceable role in production and handling machines. With high frequency of working cycle periods, the dynamic load of the proper servomotor rotor increases and efficiency of electronic cams strongly decreases. Though conventional intermittent mechanisms with radial cams are representatives of fixed automation, they have distinct advantages in their high speed (high dynamics), positional accuracy and relatively easy manufacture. We try to remove the disadvantage of firm displacement diagram by reducing costs for simple design and automated calculation that leads reliably to high-quality and inexpensive manufacture.

Keywords—Cam mechanism, displacement diagram, intermittent mechanism, radial parallel cam

I. INTRODUCTION

Intermittent mechanisms are important elements in manufacturing systems fixed and flexible automation. These are often the manipulation movements in the various forms of rotary tables in production lines, packaging machinery, machine tools, etc. Mechanisms with radial cams are interesting because of a very precise manufacturing process. Despite the strong expansion of electronic cam mechanisms, there are still many tasks where it is not possible and even in the foreseeable future it will not be possible to replace mechanical cams with electronic cam mechanisms. In particular, they stand out for their dynamic properties that are improved with the advent of new materials.

Design of these mechanisms can be divided into two steps. In the first step a displacement diagram, which forms the starting point in the synthesis of cam mechanisms, is assembled. A displacement diagram is in principle an input-output function that defines the movement of the follower depending on the rotation drive shaft, resp. cam.

The second step, which will be given the most attention, is the synthesis of cams; cam profile is calculated according to the defined displacement diagram. The calculation of course is affected by other parameters (distance axis of rotation cam and follower, follower length, roller radius and number of rollers) that determine the actual dimensions and dynamic characteristics of the resulting mechanism. Based on these data the active surface (contour) of the actual cam, resp. production coordinates of contour, is calculated. In the case of symmetrical displacement diagrams (more precisely displacement diagrams, whose working part is symmetrical to its center) the resulting parallel cams mechanism, which is composed of two identical cams that are rotated each other mirrored, is created. This fact allows the production of both parts at once with inverse accuracy two cams to 0.01 mm.

However, a synthesis algorithm does not require these symmetries and thus allows creating also mechanisms based on unsymmetrical displacement diagrams and mechanisms with unsymmetrical initial rotation rollers. The disadvantage of these intermittent mechanisms is the different shape of the cams, which are needed to be produced individually. These results in significantly lower manufacturing precision compared with symmetric mechanisms.

II. DESIGN OF DISPLACEMENT DIAGRAM

A displacement diagram can be defined as a function assigning the position of another element of the cam mechanism to the position of a specific element. For conventional cam mechanisms, it is thus a function assigning a specific location of the driven element (follower) \( v \) to a certain position \( \varphi \) of the drive shaft. Along with the displacement diagrams, its first and second derivatives with respect to position, which is often called as first and second transfer function, are usually defined. A displacement diagram itself, which means zeroth derivation, is often called only as a displacement. For the clear definition of shape displacement diagrams, their description in the form of unit displacement diagram is used. This diagram is defined by the displacement of size 1. The size of interval of independent variable varies depending on the category of displacement diagram (from -1 to 1, or from -0.5 to 0.5). The example of a simple displacement diagram in the unit form is on the figure below.

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The first inevitable step was the creation of a tool that will be able to create these functions. The software tool is named KINzz 2 and includes a library of about 60 analytically given displacement diagrams taken from [1]. KINzz 2 is universally designed software, so the resulting displacement diagram is created by the composition of any number of elementary displacement diagrams and dwell intervals. The reusability of this tool is enhanced by adding options to import displacement diagrams of numerically specified displacement diagrams and ability to modify some basic types of displacement diagrams by the German standard VDI 2143 [2]. More detailed analysis of this issue transcends the scope of this article and is not necessary for the introduction of the research. Of course, there are options to save, load project and export into the data file for spreadsheet programs.

III. THE SYNTHESIS OF CAM

The second tool that has been developed for the purpose of synthesis of the radial parallel cams is named KINy 2. The diagram below represents a block structure of the implementation of the program. Individual blocks will be discussed in the following paragraphs.

1) The program KINy 2 accepts as an input any of a symmetric or unsymmetrical displacement diagrams. From a user it also requires dimensional parameters for the cam mechanism: \( a, b, c \) and the number of rollers. The chart below graphically illustrates the meaning of the first two parameters and other important variables.
In the center of the coordinate system there is the axis of cam rotation. The axis of rotation of the follower is located on the x-axis at a distance of \( a \). The coordinate z-axis is not shown because it is parallel to the axis of the cam and follower, and should not make sense. Point \( A \) indicates the position of the axis of roller follower that moves the active cam surface. The trajectory center of the roller is then only converted to the polar coordinates where \( u \) represents the length of vector and \( \phi \) angle against zero point.

\[
e(\phi) = i \cos \phi + j \sin \phi
\]

(1)

\[
p = u(\phi)e(\phi)
\]

(2)

The reverse expression of the function \( u(\phi) \) and \( \varphi(\phi) \) comes from the classical notation

\[
p(\phi) = ix(\phi) + jy(\phi)
\]

(3)

It is possible to obtain a general expression using the basic formulas of the goniometric functions

\[
u(\phi) = \sqrt{x^2(\phi) + y^2(\phi)}
\]

(4)

\[
\varphi(\phi) = \psi(\phi) + S \arccos \frac{x(\phi)}{u}
\]

(5)

After substituting the general function \( x(\phi) \) and \( y(\phi) \)

get the basic relations for the synthesis of the pitch profile.

\[
u(\phi) = \sqrt{a^2 - 2ab \cos \psi + b^2}
\]

(6)

\[
\varphi(\phi) = \psi(\phi) + S \arccos \frac{a-b \cos \nu}{u}
\]

(7)

For the calculation of the angle \( \varphi \), the general relationship is supplemented by the sign function \( S \), which provides a correct calculation for the full 360°. It removes the restriction that cycloidal functions brought into the calculation. The function takes the values 1 and -1 depending on which half-plane (defined by the x-axis) is point A.

\[
S(\psi) = sgn \ y(\nu)
\]

(8)

To obtain the actual cam profile, it is necessary to express the angle of the normal, which is denoted by the Greek letter \( \psi \). The contact point of the roller and cam for any radius of the roller always lies on the line determined by the normal vector, as shown in the figure below.

The derivation of the analytical relationship for the normal angle is a fairly complicated procedure, which is detailed in [1], so here only the final relationship is mentioned.

\[
v(\psi) = -\arctg \frac{\nu a b \sin \psi}{a^2 - 2ab \cos \psi + b^2 + \nu b (a \cos \psi - \nu)}
\]

(9)

In the relation two time derivatives appear, which do not present a problem. \( v \) represents the angular velocity of the rotation of the cam, which is constant for our purposes. Due to this consideration, the time derivative \( v' \) can be converted to the derivative according to the position of the cam \( \psi' \), which is given by displacement diagram (first transfer function). With the knowledge of the normal angle, the equations for the recalculation of the pitch profile of the actual cam profile can be found using the goniometric equations and the law of cosines. The radius of the roller in the relationship acts as a parameter.
The last no less important parameter is the number of rollers. To determine the final cam profile, it is necessary to first determine the paths of all the rollers of which the smallest profile is then "cut out". The paths are closed curves, after which the individual rollers move. Before the calculation it is necessary to determine their count and length. Firstly it is important to define the total displacement, which defines the angle by which the follower rotates per one revolution of the cam. It is necessary to determine the minimum number of revolutions, after which a given roller returns to its initial position.

$$\text{minimum number of revolutions} = \frac{\text{least common multiple (360, total displacement)}}{\text{total displacement}}$$

$$\text{number of paths} = \frac{\text{number of rollers}}{\text{minimum number of revolutions}}$$

2) Using the above equations for $u$ and $\phi$ and substituting $v$ as a function of time $\tau$ (at constant revolutions $v$ can be as well considered as the function of cam rotation $\psi$); we get the paths of the rollers centers, as the following figure demonstrates.

3) For the purposes of further analysis and transfer to the production coordinates, it is required that the resulting coordinates were calculated with a constant step $\phi$. The creation of cubic interpolation spline, which represents the relationship between $\phi$ and $\tau$, proved to be the best solution in the end. With its help there are backward interpolated values $\tau$ to achieve a constant step $\phi$. If the cam is well specified (it is geometrically feasible) the deviations of the calculated values $\phi$ from the desired values are lower by several orders of magnitude than the precision of the manufacturing process.

4) With the newly obtained values of $\tau$ a similar calculation as in step 2 is done. After calculating the paths of individual rollers, the minimum profile that will represent a real cam will be cut off, as demonstrated in the figure below.
5) For the completion of the whole mechanism it is necessary to produce a second cam. As mentioned in the introduction, when all the above mentioned symmetries are complied, the second cam is created from the same profile, just made after the mirror rotates. For the correct connection of both cams, a hole, the “zero pin”, is created in the profile so to connect two profiles and ensure the correct mutual position. For the right determination of this point the center of the working part of displacement diagram must be found. Since the displacement diagrams entering into the synthesis are specified numerically, it may not be the real center directly included in the data. Therefore, the interpolation by cubic spline is used again. To find a specific value quickly, Newton’s method of tangents [3], which was adapted for this type of function, is used. The figure below shows the assembly of the cam mechanism from the previous images. For the better illustration of the function, the cam is rotated by 165°.

In the case of the violation of the symmetry of displacement diagram or symmetry of the initial rotation of the rollers, the resulting mechanism is composed of two different cams. The disadvantage of these mechanisms is a greater inaccuracy of production; however, they bring a huge amount of new possibilities in the construction of intermittent mechanisms. It is easy to implement mechanisms adapted to constant forceful exertion in one direction, which will have significantly better dynamic performance than the symmetrical arrangement.

IV. CONCLUSION

Based on the real requirements of industry practice, there have been developed two software tools for automated design intermittent mechanisms with radial parallel cams. The first one allows very free design displacement diagrams, which allows its use for the design of various cam mechanisms or electronic cams. The second is directed towards the synthesis of radial parallel cams mechanisms. It also allows an easy and quick comparison of mechanisms with the different input parameters of cam profiles, and also selected kinematic-static parameters (angle of normal and pressure angle). Both tools are still being developed and improved according to the current requirements. Another aim is to implement advanced algorithms such as automated unloading cam profiles to improve the dynamic parameters of the mechanism.

Both tools are being developed in Microsoft Visual Studio 2010 in C# language and compiled for .Net Framework 4. Besides the standard Visual Studio libraries, two free accessible libraries were used, too. For advanced mathematical functions library “Math.NET Iridium” [4] and a library for graphs A simple C# library for graph plotting [5].

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